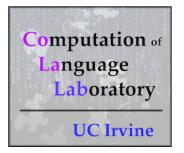
Computational cognitive modeling: How to investigate child language acquisition using math

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About child language acquisition















child language acquisition: extraction of language information by young children













One question: What kind of language information exactly?

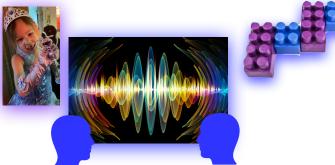






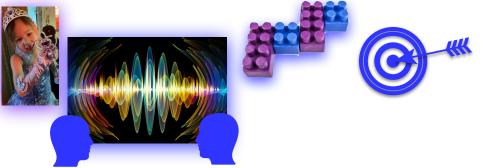






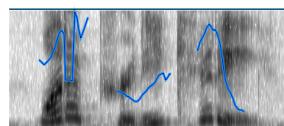


Some examples of target language information



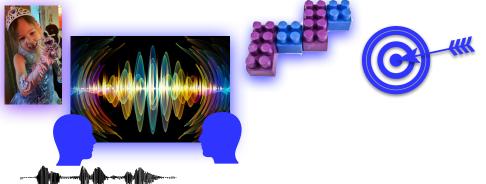
how to identify words in fluent speech (speech segmentation)

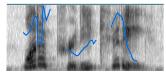




wлrəpлrikıri wлr ə pлri kıri what a pretty kitty!





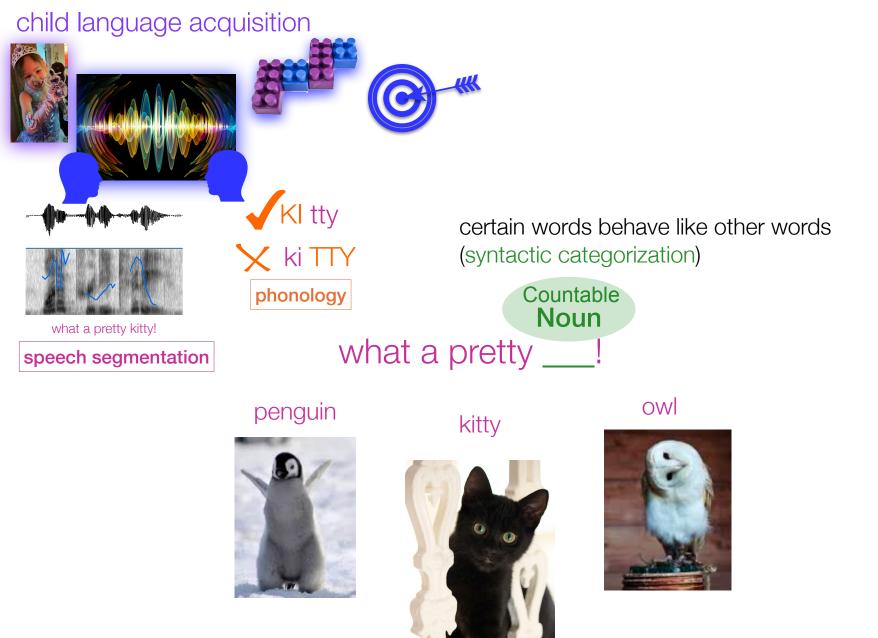


```
what a pretty kitty!
speech segmentation
```

how to pronounce words (phonology)

KI tty ki TTY





how to interpret words in context (syntax, semantics)

"Oh look — a kitty!" "He's such a pretty kitty!"

"Look - there's another one!"



speech segmentation







how to put words together to ask questions (syntax)

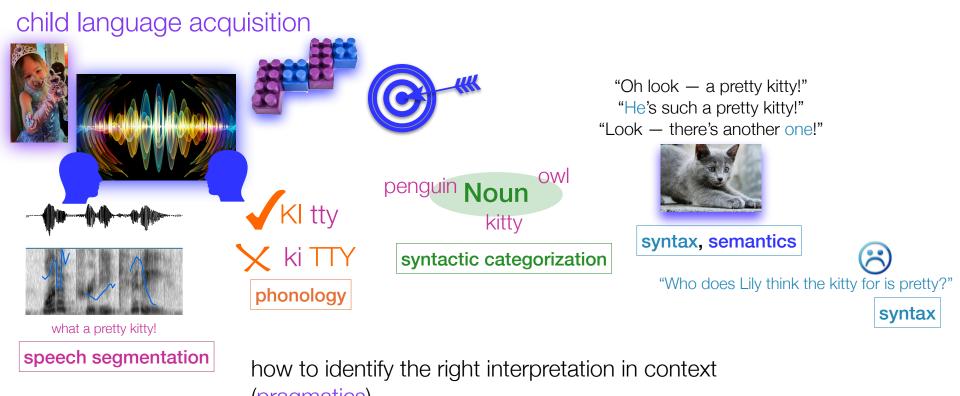
This kitty was bought as a present for someone.



Lily thinks this kitty is pretty.





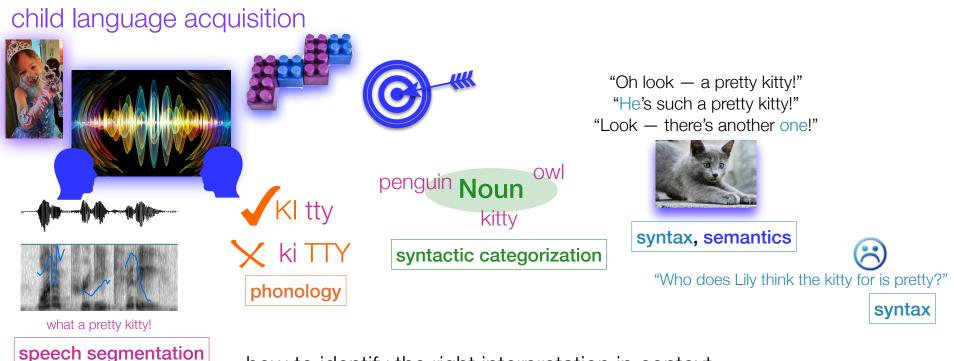


(pragmatics)

"I think I saw all the kitties on the stairs."

"No - every kitty didn't sit on the stairs"





how to identify the right interpretation in context (pragmatics)

"I think I saw all the kitties on the stairs."



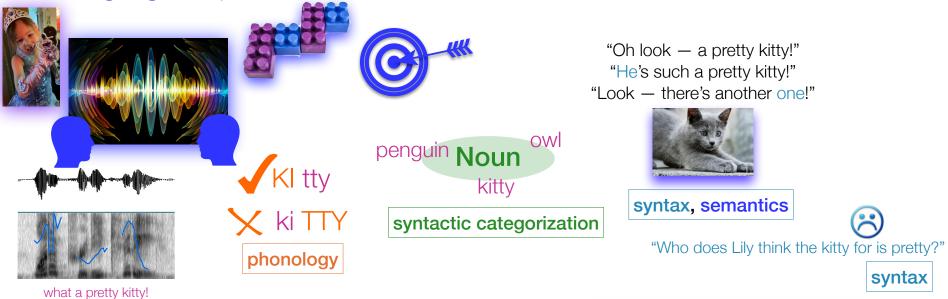


- "No every kitty didn't sit on the stairs"
- X No kitties sat on the stairs.

Not all kitties sat on the stairs.







Another important question: How does this magical acquisition process occur?



speech segmentation



pragmatics

"Every kitty didn't sit on the stairs"

Not all kitties sat on the stairs.



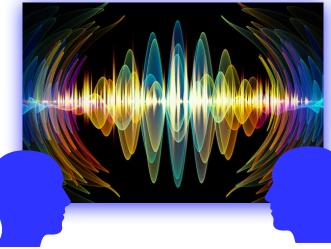


Children are amazing at learning language



















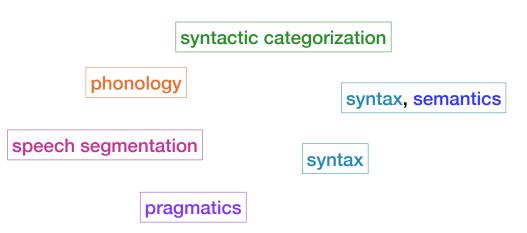








Much of the linguistic system is already known by age 4.







Also, children figure language out mostly without explicit instruction.





What they're doing: Extracting patterns and making generalizations from the surrounding data mostly just by hearing examples of what's allowed in the language.



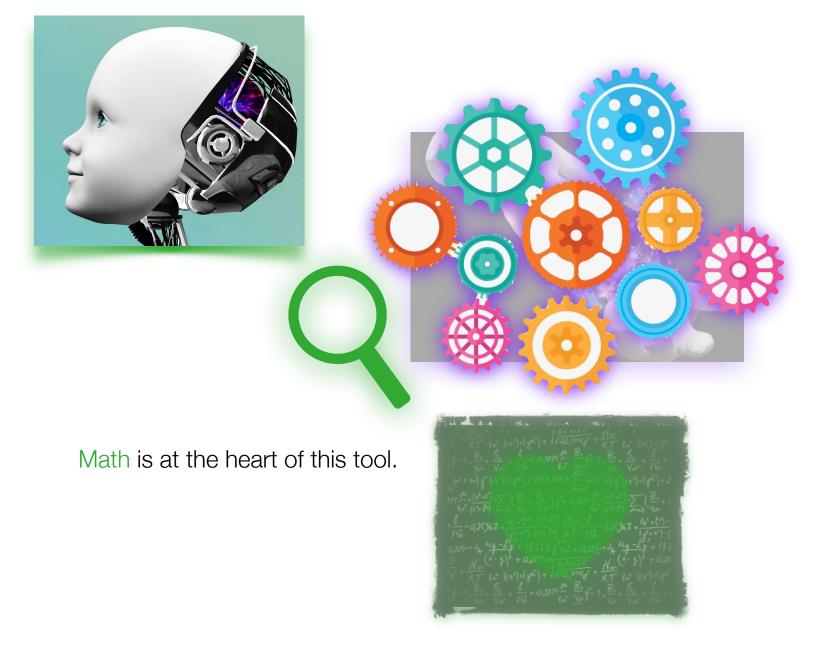
This is pretty magical. But how does it work?

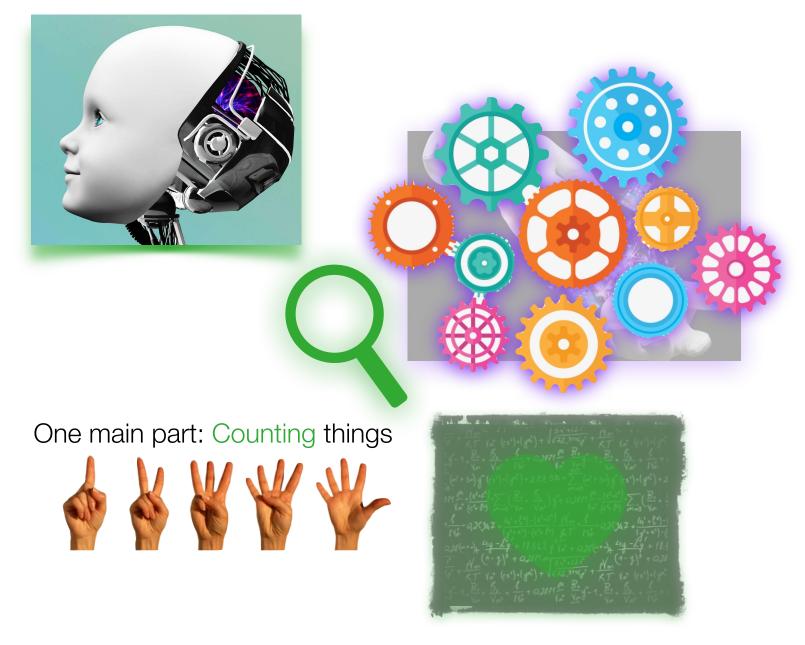
I primarily use quantitative methods like computational cognitive modeling to try to figure this out.



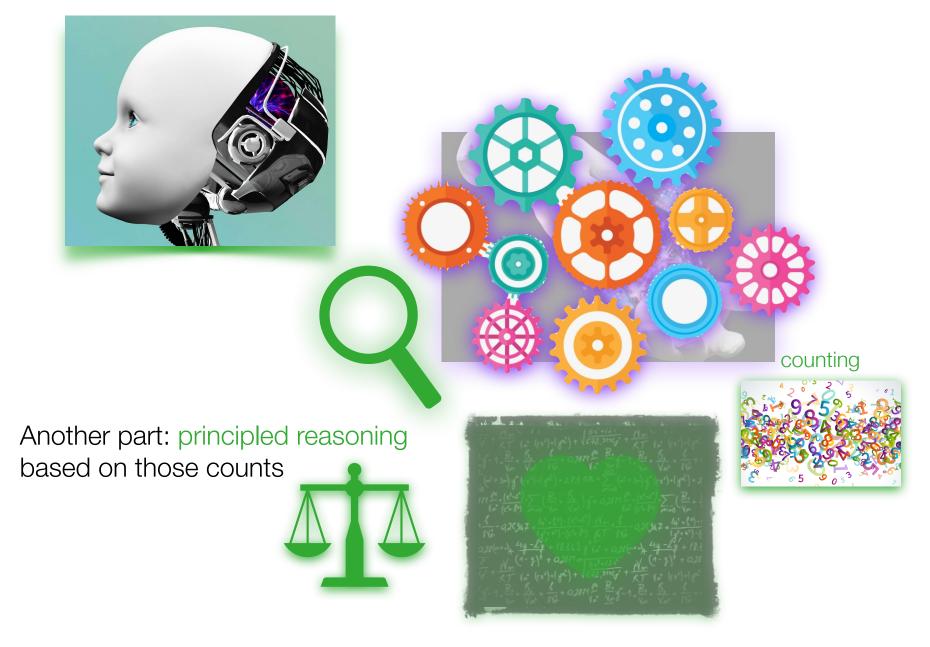


Computational cognitive modeling lets us explore theoretical ideas precisely, and evaluate how well any particular theory can explain empirical data on children's language acquisition.







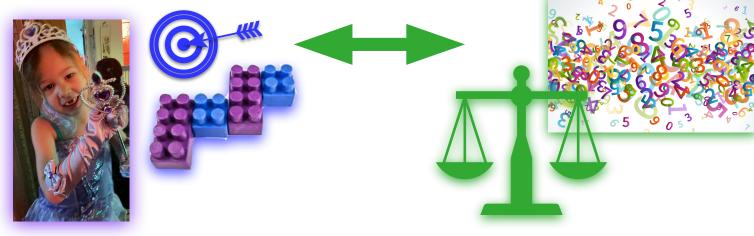




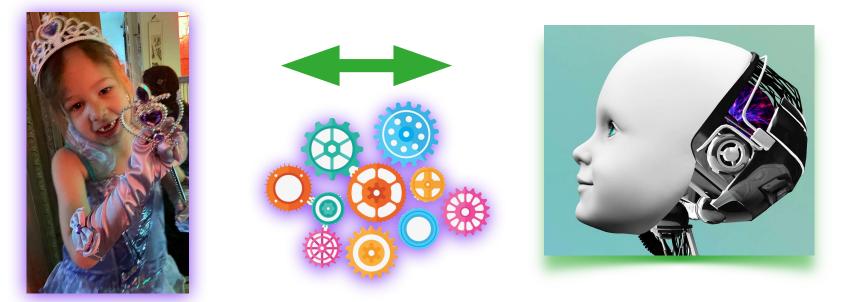
 $p(Generalization | Data) \propto p(Generalization) \cdot p(Data | Generalization)$



But what do we count and reason over? How do we connect that information to language acquisition?



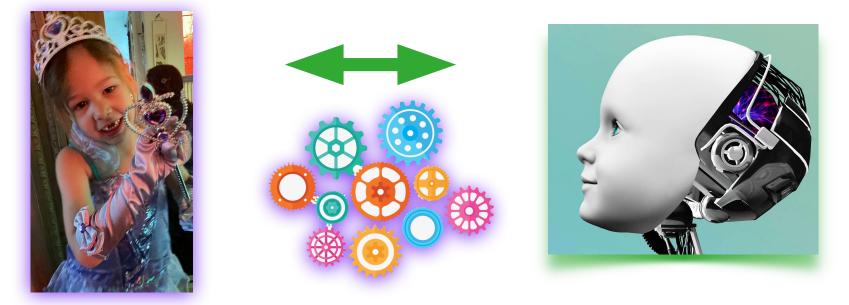
computational cognitive modeling



We typically using computational cognitive modeling to encode a child's acquisition process very precisely.



computational cognitive modeling



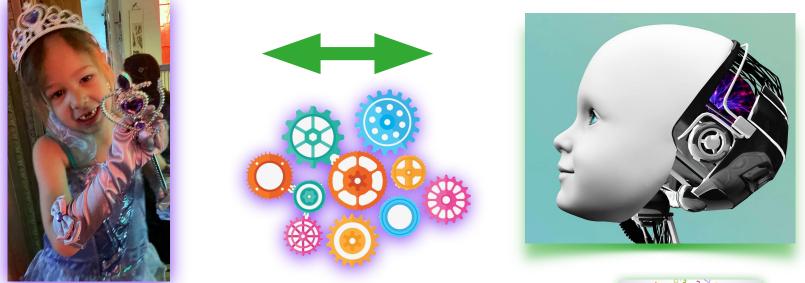
We think the child is learning by counting different parts of her input and reasoning over those counts in a sensible way.



So, the modeled learner will count those same things and learn about language by doing principled reasoning over those counts.



computational cognitive modeling



Let's see how this works for a type of syntactic knowledge known as "syntactic islands".







Syntactic islands involve *wh*-dependencies.

This kitty was bought as a present for someone.

What's going on here?

Lily thinks this kitty is pretty.



Who does Lily think the kitty for is pretty?

What does Lily think is pretty, and who does she think it's for?

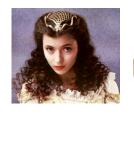






There's a dependency between the *wh*-word *who* and where it's understood (the gap)

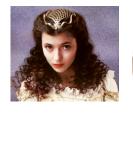
Who does Lily think the kitty for___who is pretty?







There's a dependency between the *wh*-word *who* and where it's understood (the gap)



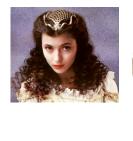


Who does Lily think the kitty for__who is pretty?

This dependency is strongly dispreferred in English.



There's a dependency between the *wh*-word *who* and where it's understood (the gap)





Who does Lily think the kitty for __who is pretty?

This dependency is strongly dispreferred in English.

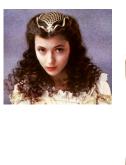
One explanation: The dependency crosses a "syntactic island" (Ross 1967)





Who does Lily think the kitty for ___who is pretty?

Subject island







Who does Lily think the kitty for ___who is pretty?

Subject island



Jack is somewhat tricksy.

He claimed he bought something.

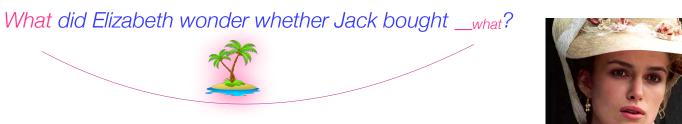


	Syntactic islands	
	Ross 1967	
Who does Lily think the kitty forwho is pret	tty? Subject island	
What did Jack make the claim that he boug	oht what? Complex NP island	

Jack is somewhat tricksy.

He claimed he bought something.

Elizabeth wondered if he actually did and what it was.

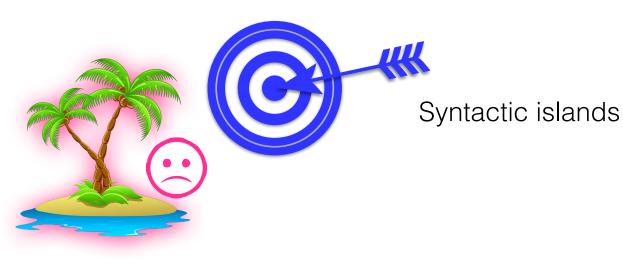


States of the st	yntactic islands	
	Ross 1967	
Who does Lily think the kitty forwho is pretty?	Subject island	
What did Jack make the claim that he bought _		
What did Elizabeth wonder whether Jack boug	htwhat? Whether island	Jack is somewhat tricksy.
		nad ha hayaht aamathing

He claimed he bought something. Elizabeth worried it was something dangerous.







Important: It's not about the length of the dependency.

(Chomsky 1965, Ross 1967)



Important: It's not about the length of the dependency. (Chomsky 1965, Ross 1967)

What did Elizabeth think _______?

Elizabeth





Important: It's not about the length of the dependency. (Chomsky 1965, Ross 1967)

What did Elizabeth think Jack said ____what?



Elizabeth



Jack





Syntactic islands

Who does Lily think the kitty for ___who is pretty? Subject island What did Jack make the claim that he bought ____what? Complex NP island What did Elizabeth wonder whether Jack bought ____what? Whether island What did Elizabeth worry if Jack bought ____what? Adjunct island

Important: It's not about the length of the dependency. (Chomsky 1965, Ross 1967)

What did Elizabeth think Jack said Lily saw _____what?

Elizabeth



Jack



Lily





> English adults judge these island-crossing dependencies to be far less acceptable than many others, including others that are very similar except that they don't cross syntactic islands (Sprouse et al. 2012).





What did Jack make the claim that he bought __what? Complex NP island What did Elizabeth wonder whether Jack bought __what? Whether island What did Elizabeth worry if Jack bought __what? Adjunct island



English-learning children strongly disprefer one of these islandcrossing dependencies compared to others (de Villiers et al. 2008).





> Additional *wh*-dependency knowledge: The frequency of a lexical item can also affect adult acceptability judgments of potential syntactic islands.

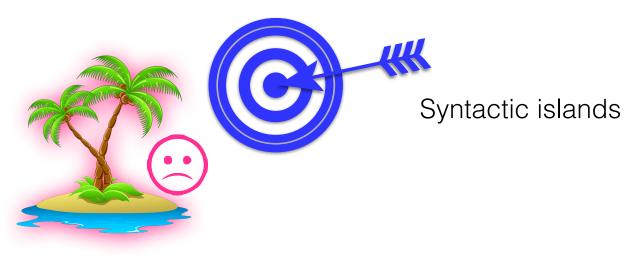




What did Elizabeth say that Jack saw___what?

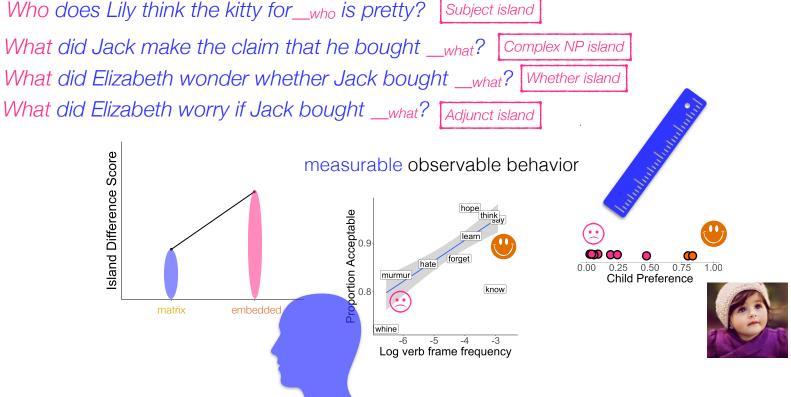
What did Elizabeth whine that Jack saw ____what?





These judgments and (dis)preferences are a measurable observable behavior that can signal the successful acquisition of syntactic island knowledge.







sland Difference Score

Syntactic islands

 \odot \odot

0.00

0.25

0.50 0.75

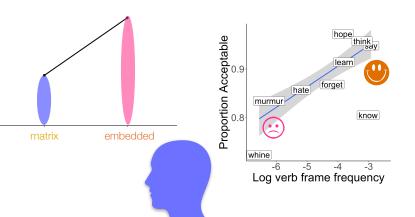
Child Preference

1.00



Who does Lily think the kitty for __who is pretty? Subject island What did Jack make the claim that he bought __what? Complex NP island What did Elizabeth wonder whether Jack bought __what? Whether island What did Elizabeth worry if Jack bought __what? Adjunct island

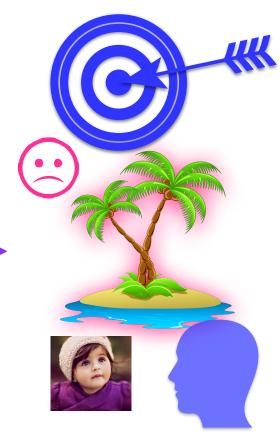
So, these judgments and (dis)preferences can serve as a target for successful acquisition — an outcome we can measure.



This is the target of acquisition. But how could a child learn this?









Let's use a computational cognitive model to help figure this out.













What's a learning theory the modeled learner could encode?









one learning theory

Pearl & Sprouse 2013 Dickson, Pearl, & Futrell 2022, 2024, in prep.

Learn the right building blocks

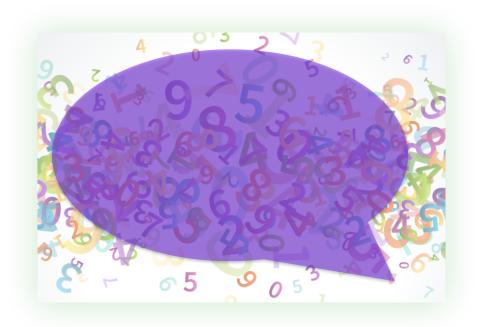




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View *wh*-dependencies in terms of their building blocks and track (count) those building blocks in the input.



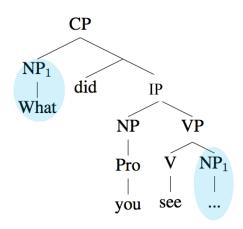


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building blocks of wh-dependencies

Dependencies represented as a sequence of container nodes



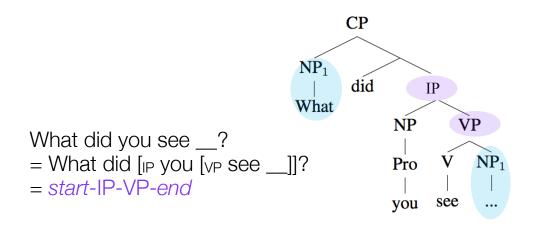


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building blocks of wh-dependencies

Dependencies represented as a sequence of container nodes



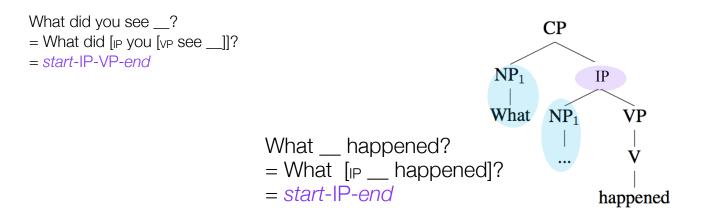


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building blocks of wh-dependencies

Dependencies represented as a sequence of container nodes



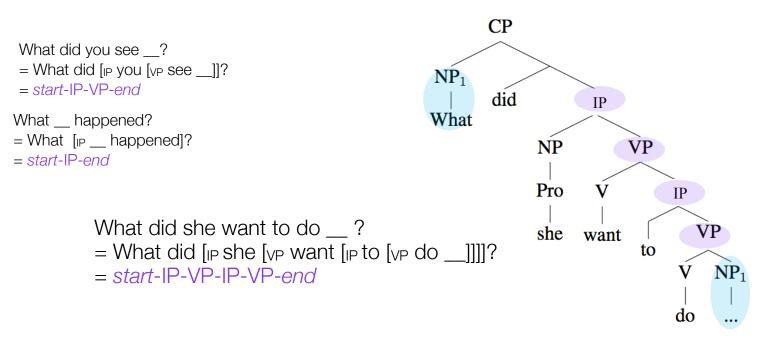


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building blocks of wh-dependencies

Dependencies represented as a sequence of container nodes





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building blocks of wh-dependencies

What __ happened? = What [IP __ happened]? = start-IP-end What did you see __? = What did [IP you [VP see __]]? = start-IP-VP-end

What did she want to do __ ? = What did [IP she [VP want [IP to [VP do __]]]]? = start-IP-VP-IP-VP-end

(Much) less acceptable dependencies have low probability segments

CP Who $[_{P} Lily [_{VP} think [_{CP-that} [_{P} [_{NP} the kitty [_{PP} for __]] was pretty ?]]]]$ did start-IP-VP-CP_{that}-IP-NP-PP-end



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building blocks of wh-dependencies

What ____happened? = What [IP ____happened]? = start-IP-end What did you see __? = What did [IP you [VP see __]]? = start-IP-VP-end

What did she want to do __ ? = What did [IP she [VP want [IP to [VP do __]]]]? = start-IP-VP-IP-VP-end

(Much) less acceptable dependencies have low probability segments

 [CP Who
 did
 [IP Lily
 [VP think [CP-that [IP [NP the kitty [PP for __]] was pretty ?]]]]

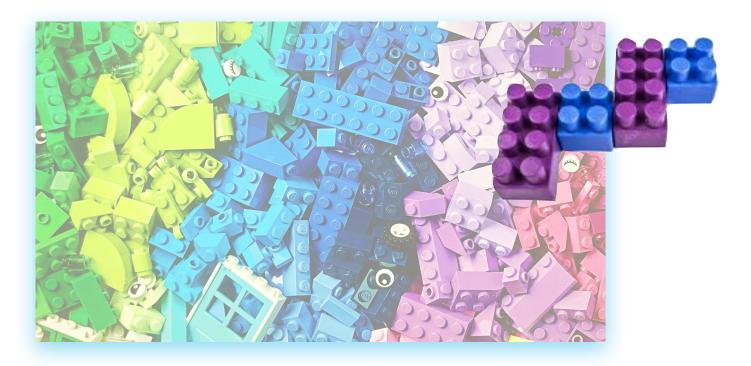
 Start-IP-VP-CPthat-IP-NP-PP-end

 So if children break these dependencies into smaller building blocks, they can identify if a dependency has bad segments (made up of one or more low probability building blocks).



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Theory: The child tries to learn what the "best" building blocks are

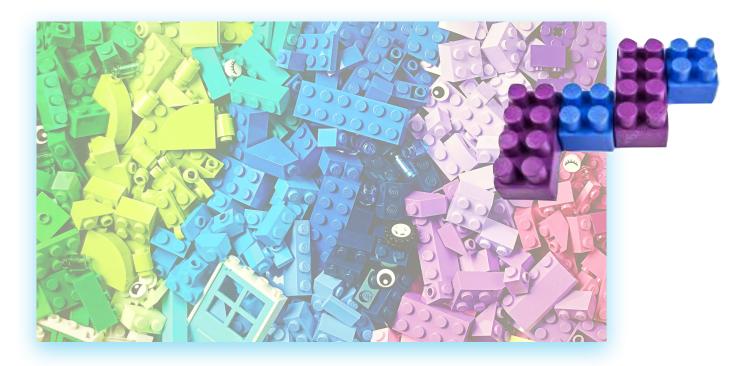




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Guiding intuition:

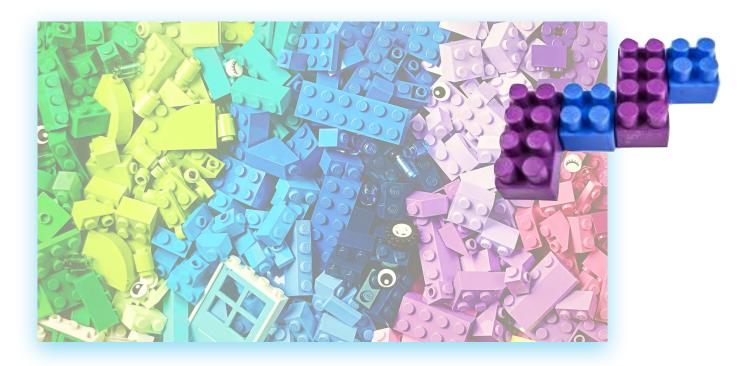
the "best" building blocks are the most "efficient" ones.





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Efficient building blocks allow the representation of current and future *wh*-dependencies to be more probable.



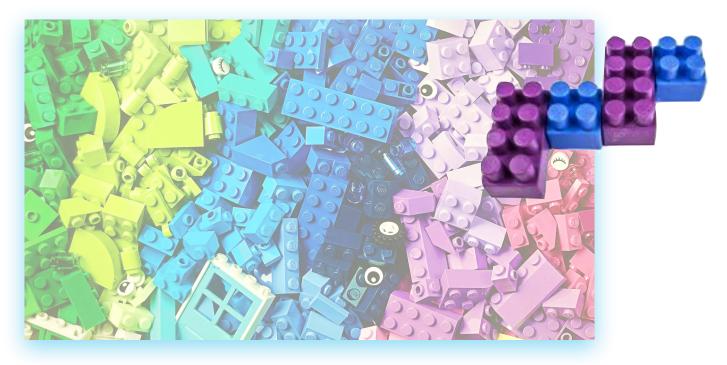


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Efficient building blocks allow the representation of current and future *wh*-dependencies to be more probable.



Why? One idea: Higher probability *wh*-dependencies are faster to process (comprehending or producing).





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learning efficient building blocks





How? Look for building blocks that are a balance between

(1) how big they are

(2) how fast they are to put together to make a *wh*-dependency



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learning efficient building blocks

a balance between (1) how big they are



(2) how fast they are to put together to make a *wh*-dependency

 CP $N\dot{P}_1$ did ΙP What ŃŶ ŴΡ Pro ĈР she say that ÌP ŃŶ ŇΡ NP_1 Pro he saw

What did she say that he saw __ ?



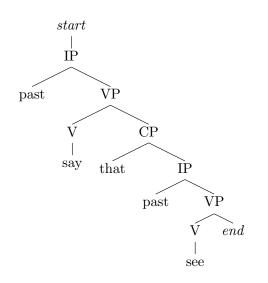
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learning efficient building blocks



a balance between
(1) how big they are
(2) how fast they are to put together to make a *wh*-dependency

start-IPpast-VPsay-CPthat-IPpast-VPsee-end





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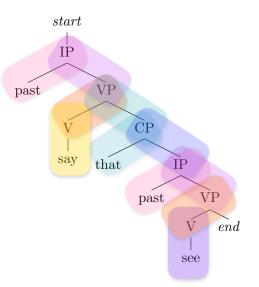
learning efficient building blocks



a balance between
(1) how big they are
(2) how fast they are to put together to make a *wh*-dependency

start-IPpast-VPsay-CPthat-IPpast-VPsee-end

Pieces can be small, so that many of them make up a *wh*-dependency





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learning efficient building blocks

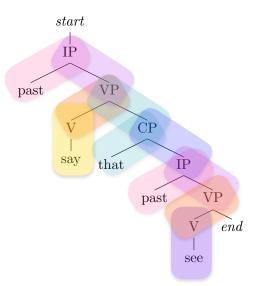


a balance between
(1) how big they are
(2) how fast they are to put together to make a *wh*-dependency

start-IPpast-VPsay-CPthat-IPpast-VPsee-end



It may be slower to put together many small pieces.





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learning efficient building blocks



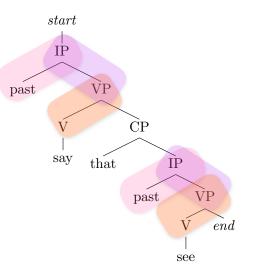
a balance between
(1) how big they are
(2) how fast they are to put together to make a *wh*-dependency

start-IPpast-VPsay-CPthat-IPpast-VPsee-end

many smaller

r slower because many

But these pieces may get reused, so that makes them faster to access.





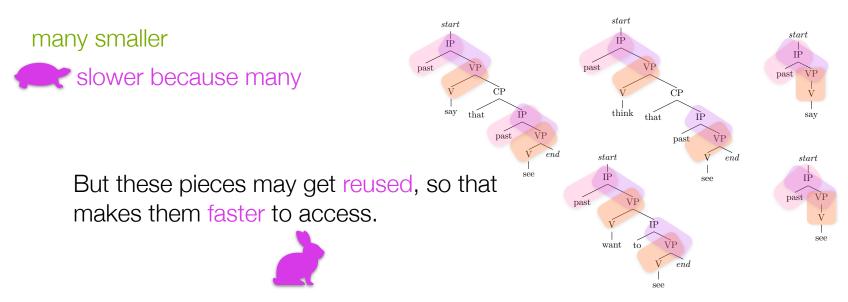
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learning efficient building blocks



a balance between
(1) how big they are
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start-IPpast-VPsay-CPthat-IPpast-VPsee-end





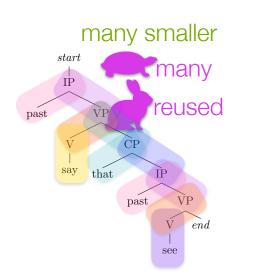
Dickson, Pearl, & Futrell 2022, 2024, in prep.

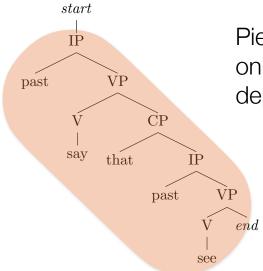
learning efficient building blocks



a balance between
(1) how big they are
(2) how fast they are to put together to make a *wh*-dependency

start-IPpast-VPsay-CPthat-IPpast-VPsee-end





Pieces can be big, so that only one makes up a *wh*dependency



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learning efficient building blocks a balance between (1) how big they are (2) how fast they are to put together to make a *wh*-dependency start-IPpast-VPsay-CPthat-IPpast-VPsee-end start many smaller ΙP It may be faster to put startmany IP together one big piece. VP past reused ŴΡ past ĊР CP say that ΪP say that ÌP past past VPendend see see



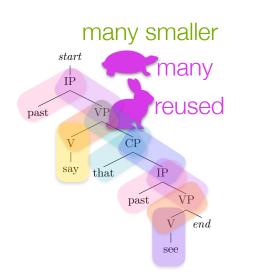
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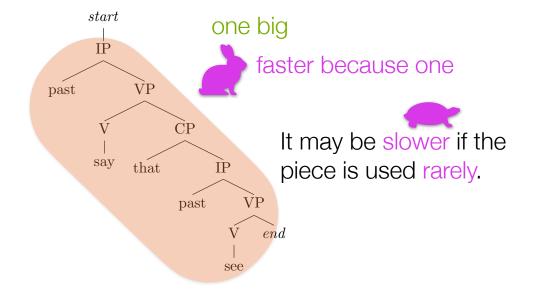
learning efficient building blocks



a balance between
(1) how big they are
(2) how fast they are to put together to make a *wh*-dependency

start-IPpast-VPsay-CPthat-IPpast-VPsee-end







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learning efficient building blocks

a balance between (1) how big they are (2) how fast they are to put together to make a *wh*-dependency



start

say that

start

IP

think

VР

that

past

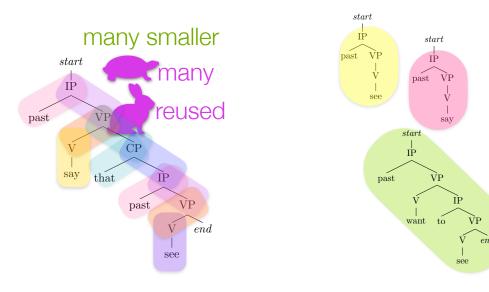
past

ĊР

past

past

start-IPpast-VPsay-CPthat-IPpast-VPsee-end



one big faster because one

> It may be slower if the piece is used rarely.



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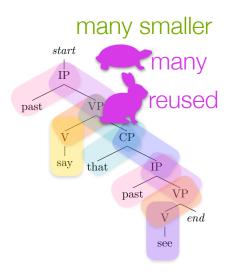
learning efficient building blocks



a balance between
(1) how big they are
(2) how fast they are to put together to

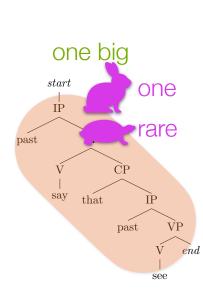
make a *wh*-dependency

start-IPpast-VPsay-CPthat-IPpast-VPsee-end



The most efficient option is probably a balance of bigger and smaller blocks that collectively are faster to access and put together.







IP

see

end

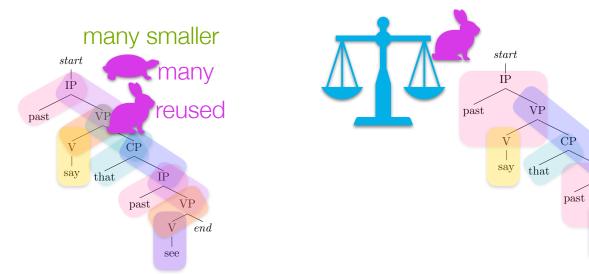
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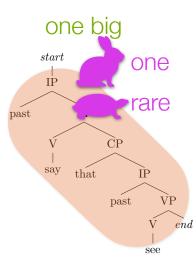
learning efficient building blocks



a balance between
(1) how big they are
(2) how fast they are to put together to make a *wh*-dependency

start-IPpast-VPsay-CPthat-IPpast-VPsee-end



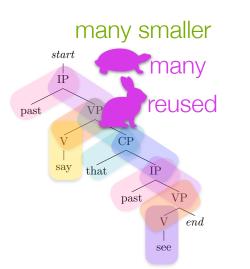


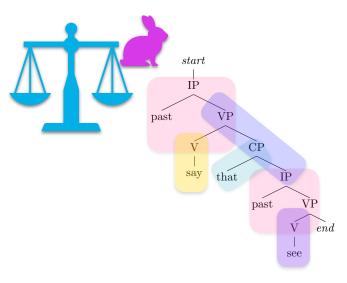


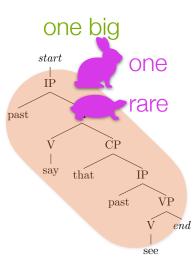
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learning efficient building blocks

How can children find the best balance?









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Use Bayesian inference to search through the hypothesis space of all possible building blocks (O'Donnell 2015) and find an efficient set for children's input.





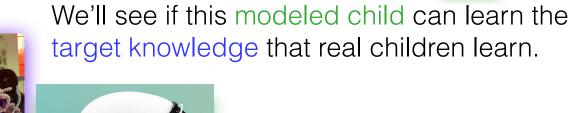
Dickson, Pearl, & Futrell 2022, 2024, in prep.







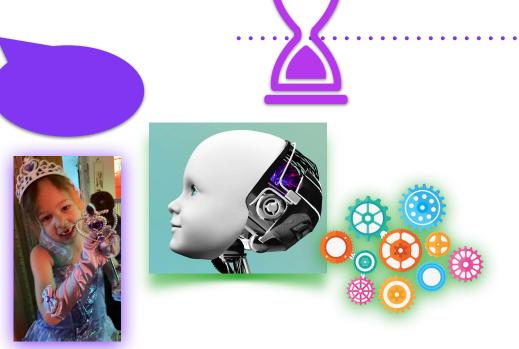








We'll have the modeled child learn from the same kind of input children encounter, for the same amount of time.







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Estimated from the CHILDES Treebank (Pearl & Sprouse 2013) ≈10,442,258 min (derived from De Villiers et al. 2008,

Perkins & Lidz 2021, & Davis et al. 2004)





We'll have the modeled child learn from the same kind of input children encounter, for the same amount of time.

Estimated from the CHILDES Treebank (Pearl & Sprouse 2013) ≈2.15 million wh-dependencies (derived from Hoff-Ginsberg 1998 and Rowe 2012)

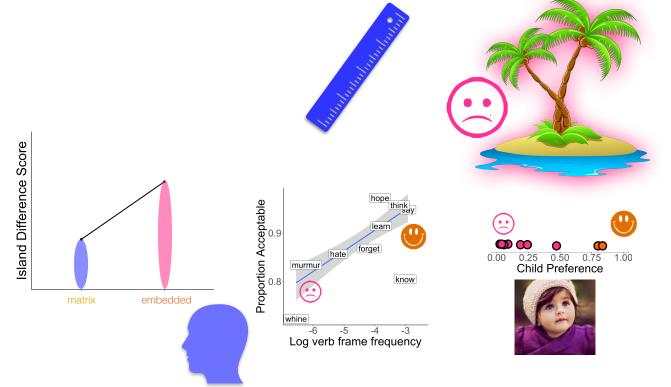








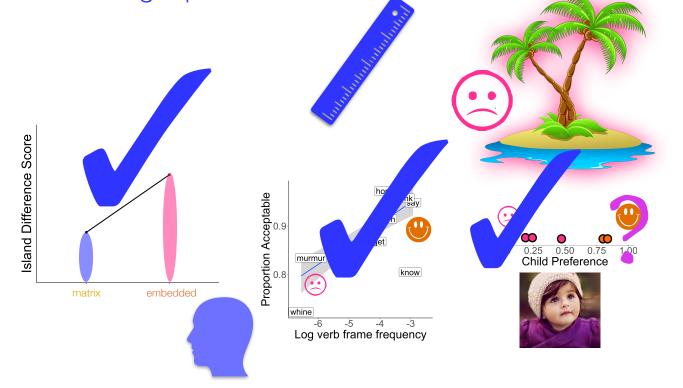
A reminder of the measurable target behavior patterns







Our modeled child can generate almost all of these target patterns.



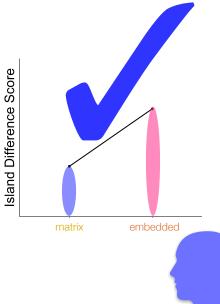


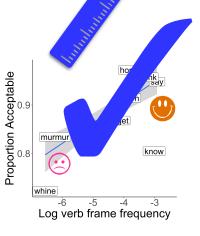


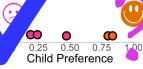
Dickson, Pearl, & Futrell 2022, 2024, in prep.

This means the modeled child, who encoded the "efficient building blocks" learning theory, was able to generate almost all of children's target behavior.

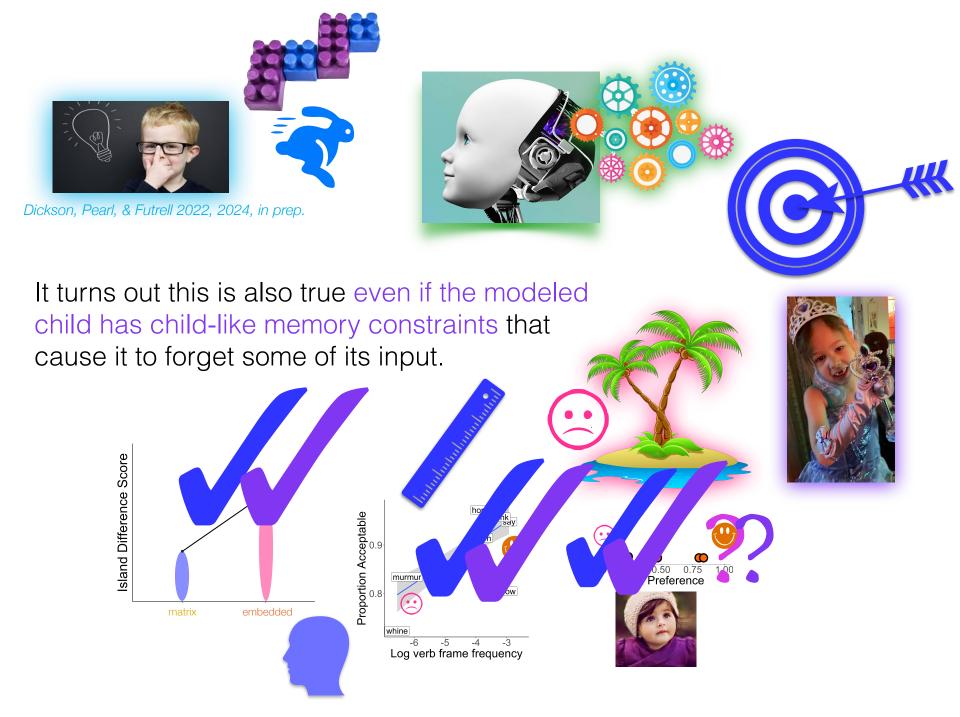


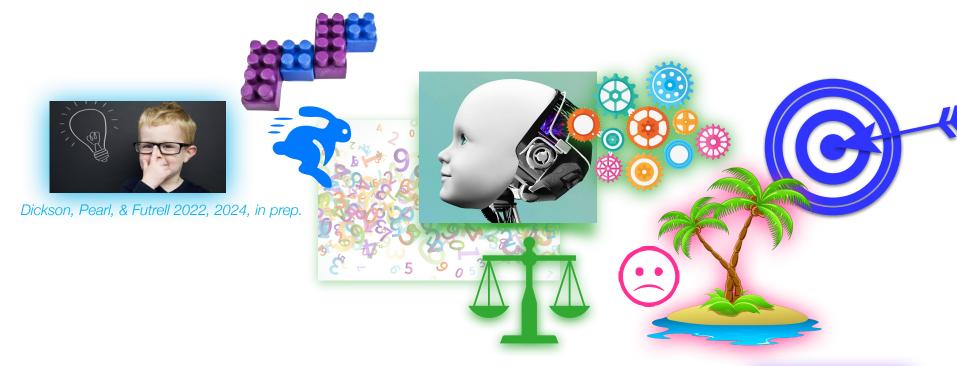






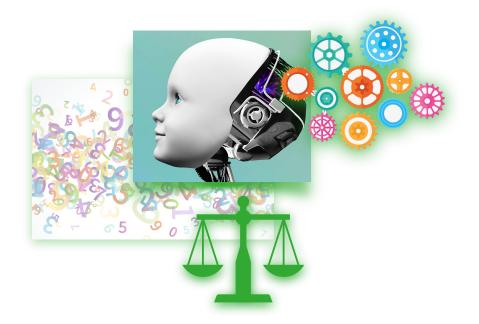






Takeaway: This learning theory (implemented by the modeled child using math) is pretty good at capturing children's target behavior. So, it may be a pretty good explanation for how children acquire syntactic island knowledge from their input.





Some other discoveries from my research group, using computational cognitive modeling





Children transform the input signal they encounter in order to learn.

















Sometimes acquisition success may result only when the data intake for acquisition is a selective subset of the available input.





(*basic word order*: Pearl 2005a,b, 2007, Pearl and Weinberg 2007; *metrical stress*: Pearl 2007, 2008, 2009, 2011, Pearl, Ho and Detrano 2014, 2016, Pearl 2017; *English anaphoric one*: Pearl 2007, Pearl and Lidz 2009; *syntactic islands*: Pearl and Sprouse 2013a,b, Pearl 2014, Pearl and Sprouse 2015; *English passive*: Nguyen and Pearl 2019, 2021)





However, sometimes acquisition success may also occur by taking a broader perspective on what counts as relevant data.





(Pearl 2023a; *English anaphoric one*: Pearl and Mis 2011, 2016; *syntactic islands*: Pearl and Sprouse 2013a,b, Pearl 2014, Pearl and Sprouse 2015, Pearl 2017, Bates and Pearl 2019, Pearl and Bates 2022; *English passive*: Nguyen and Pearl 2018, 2019, 2021).







To learn some types of linguistic knowledge, children may need to have language-specific knowledge built into their minds — however the exact form of this knowledge may be different than what we previously thought.

(*English anaphoric one*: Pearl and Lidz 2009, Pearl and Mis 2011, 2016; *syntactic islands*: Pearl and Sprouse 2013a,b, Pearl 2014, Pearl and Sprouse 2015, Dickson, Pearl and Futrell 2022; *linking theories*: Pearl and Sprouse 2019, 2021)







Children's linguistic knowledge may sometimes be far more well-developed than we realize earlier than we realize, with strong similarities between child and adult representations





(*closed-class syntactic categories*: Bates, Pearl and Braunwald 2018; *quantifier scope ambiguity resolution*: Savinelli, Scontras and Pearl 2017, 2018, Scontras and Pearl 2021; *adjective ordering preferences*: Bar-Sever, Lee, Scontras and Pearl 2018; *pronoun interpretation*: Forsythe and Pearl 2019, Pearl and Forsythe under review)

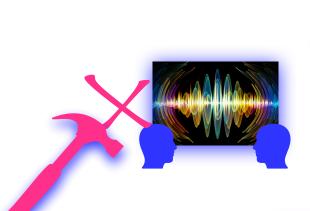




"Different" doesn't automatically mean "worse" when it comes to language development.









While there is certainly input variation across socio-economic status, the same language learning outcome could still occur, despite the variation. So, interventions targeted at "fixing" the input aren't likely to be effective.



syntactic islands: Bates and Pearl 2019, Pearl and Bates 2022



Even if the representations of very young children may not match adult representations, they can still be "good enough" for helping other acquisition processes get started.

early speech segmentation: Phillips and Pearl 2012, 2014a,b, 2015a,b,c, Pearl and Phillips 2018; *early syntactic categorization*: Bar-Sever and Pearl 2016





Learners with processing constraints (like children) may sometimes learn better than learners with fewer limitations ("less is more").

speech segmentation: Pearl, Goldwater and Steyvers 2010, 2011, Phillips and Pearl 2012, 2015c

Take home

Computational cognitive modeling is one way to use math to investigate the magical process of child language acquisition

















Take home

It allows us to implement learning theories concretely, evaluate them, and better understand how they (and potentially children) work.















1.



Take home

So let's keep using this wonderful tool to investigate child language acquisition!



















Thank you!

Niels Dickson





Richard

Jon Sprouse Alandi Bates



BUCLD 2018UCSD Linguistics 2020ForMA Group 2020UMD Linguistics 2020BUCLD 2021SCiL 2022UArizona Linguistics 2022UChicago LEAP 2022UPenn 2023Pomona Acquisition Workshop 2024UCI QuantLang Collective





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