

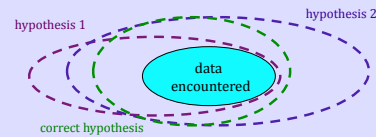
Psych 215L: Language Acquisition

Lecture 16 Poverty of the Stimulus: Anaphoric One

Making arguments from acquisition

"One explicit motivation for Universal Grammar (UG) comes from an *argument from acquisition*: UG allows children to acquire language knowledge as effectively and rapidly as they do...In particular, UG is meant to be one or more learning biases that are part of our biological endowment (*innate*) and are only used for learning language (*domain-specific*). These learning biases allow children to solve induction problems, where the available data appear to be compatible with multiple hypotheses about the generalizations for the language."

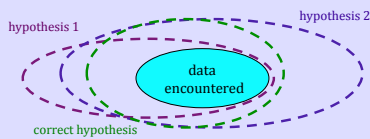
Induction problems → Universal Grammar (UG)



Making arguments from acquisition

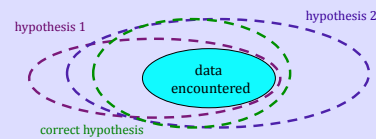
"Proposals for the *contents* of UG have traditionally come from characterizing a specific induction problem pertaining to a particular linguistic phenomenon, and describing the (UG) solution to that specific characterization."

- structure-dependent rules (Chomsky 1980)
- representation of *English anaphoric one* (Baker 1978)
- constraints on long-distance dependencies (Chomsky 1973)



The utility of computational modeling

"Computational modeling results based on realistic input allow us to make progress on the debate surrounding UG by providing a formal mechanism for exploring *whether learning strategies can solve apparent induction problems* (or at the very least, generate observed behavior). We are then able to *compare the types of biases required by each successful strategy*, consider whether any are UG, and compare precisely what kinds of UG biases each successful strategy motivates if UG biases are indeed involved."



Characterizing induction problems

initial state:
initial knowledge state + existing learning capabilities
(prior knowledge and learning biases)

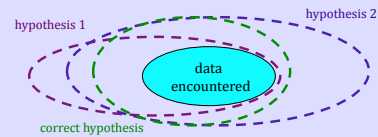
data intake (Fodor 1998):
available input that children use to learn
(defined by assumptions and biases in initial state)

learning period:
how long children have to learn (how many data points)
(usually assessed by experimental studies of children's behavior)

target state:
knowledge children are trying to attain
(usually a specific representation, theory-dependent)

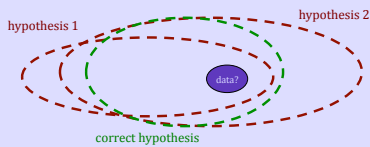
Characterizing induction problems

Definition of an induction problem:
Given a specific initial state, data intake, and learning period, the target state is not the only state that can be reached.



Induction problems, UG, and informative data

Traditional assumption:
Only directly related data are informative data. These data are often rare, and that's why induction problems occur.



The direct evidence assumption

If you want to learn linguistic knowledge L, you learn it by observing examples of L in your input (and possibly by also being sensitive to indirect negative evidence about what examples are missing from the input.)

Learning complex yes/no questions

Direct evidence L:
"Is the boy who is in the corner t_{is} happy?"

Possible indirect negative evidence:
**"Is the boy who t_{is} in the corner is happy?"

The direct evidence assumption

If you want to learn linguistic knowledge L, you learn it by observing **examples of L** in your input (and possibly by also being sensitive to **indirect negative evidence** about what examples are missing from the input.)

Learning the representation of English anaphoric one

Situation



Direct evidence L:

"Look - a red bottle! Oh look, another one."

Possible indirect negative evidence:

*"She sat by the side of the river and he sat by the one of the road."

The direct evidence assumption

If you want to learn linguistic knowledge L, you learn it by observing **examples of L** in your input (and possibly by also being sensitive to **indirect negative evidence** about what examples are missing from the input.)

Learning syntactic islands

Direct evidence L:

"Who who thinks the necklace is expensive?"

"What does Jack think is what expensive?"

"Who who thinks the necklace for Lily is expensive?"

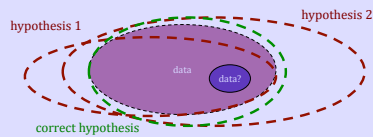
Possible indirect negative evidence:

*"Who does Jack think [[the necklace for who] is expensive]?"



A broader set of informative data

Indirect evidence: other kinds of data that may also be relevant, thereby broadening the set of informative data



Recent computational models have been exploring this:

- Complex yes/no questions (Reali & Christiansen 2005, Kam et al. 2008, Perfors, Tenenbaum, & Regier 2011)
- Anaphoric one (Regier & Gahl 2004, Pearl & Lidz 2009, Foraker et al. 2009)
- Syntactic islands (Pearl & Sprouse forthcoming a, b)

Mapping out UG & the acquisition process

Big questions:


When induction problems exist, what does it take to solve them?

- What **indirect evidence** is available? How might a child leverage this evidence?
- What learning biases can get the job done, given the available data? Are they necessarily **innate** and **domain-specific** (UG)?





Anaphoric One

Look - a red bottle!




Do you see another *one*?



Anaphoric One

Look - a red bottle!



Do you see another *one*?


red bottle

Process: First determine the antecedent of *one* (what string *one* is referring to). → "red bottle"



Anaphoric One

Look - a red bottle!



Do you see another *one*?


red bottle



Process: Because the antecedent ("red bottle") includes the modifier "red", the property RED is important for the referent of *one* to have.
→ referent of *one* = RED BOTTLE

Anaphoric One

Look - a red bottle!



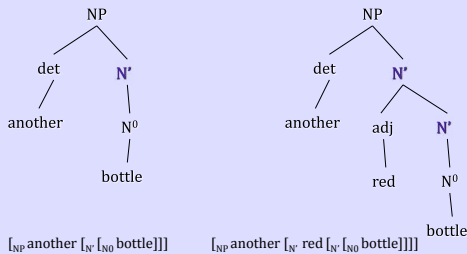
Do you see another *one*?

Two steps:
(1) Identify syntactic antecedent (based on syntactic category of *one*)
(2) Identify semantic referent (based on syntactic antecedent)

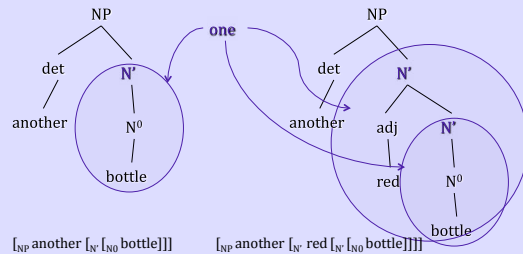
Anaphoric *One*: Syntactic Category

Standard linguistic theory (Chomsky 1970, Jackendoff 1977) claims that *one* in these kind of utterances is a syntactic category smaller than an entire noun phrase, but larger than just a noun (N⁰). This category is sometimes called N'. This category includes strings like "bottle" and "red bottle".



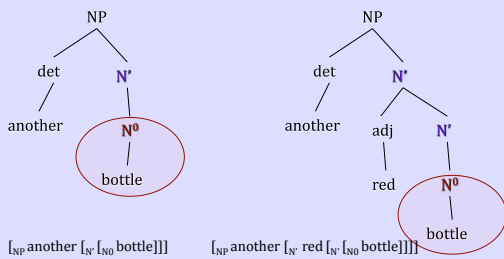
Anaphoric *One*: Syntactic Category

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Anaphoric *One*: Syntactic Category

Importantly, *one* is not N⁰. If it was, it could only have strings like "bottle" as its antecedent, and could never have strings like "red bottle" as its antecedent.



Anaphoric *One*: Interpretations based on Syntactic Category

If *one* was N⁰, we would have a different interpretation of

"Look - a red bottle! Do you see another *one*?"



Because *one's* antecedent could only be "bottle", we would have to interpret the second part as "Do you see another *bottle*?" and the purple bottle would be a fine referent for *one*.

Since *one's* antecedent is "red bottle", and "red bottle" cannot be N⁰, *one* must not be N⁰.

Anaphoric *One*: Adult Knowledge

"Look - a red bottle! Look, there's another *one*!"



Target state:

Syntactic knowledge: category N'

Semantic knowledge: mentioned property ("red") is included in the linguistic antecedent (antecedent = "red bottle")

→ "Look - a red bottle! Look, there's another red bottle!"

Anaphoric *One*: Children's Knowledge

Lidz, Waxman, & Freedman (2003) [LWF] found that 18-month-olds have a preference for the red bottle in the same situation.

"Look - a red bottle! Do you see another *one*?"

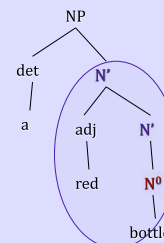


LWF interpretation & conclusion:

Preference for the RED BOTTLE means the preferred syntactic antecedent is "red bottle".

LWF conclude that 18-month-old knowledge = syntactic category of *one* = N' syntactic antecedent when modifier is present (i.e., property is mentioned) includes modifier (e.g., "red") = referent has modifier property

Learning period = completed by 18 months



Anaphoric *One*: The induction problem

initial state

Knowledge: Syntactic categories exist, in particular N⁰, N', and NP.

Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

Bias: Only direct evidence of *one* is useful.

Bias: Only unambiguous evidence of *one* is useful (Baker 1978).

data intake

All unambiguous *one* evidence in the input.

learning period

Completed by 18 months (LWF 2003)

target state

One is category N' and its antecedent includes the modifier.

Ex: [_N red [_{N'} [_{N⁰} bottle]]]

Anaphoric *One*: The available data

Acquisition: Children must learn the right syntactic category for *one*, and the right interpretation preference for *one* in situations with more than one option.

Anaphoric *One*: The available data

Acquisition: Children must learn the right syntactic category for *one*, and the right interpretation preference for *one* in situations with more than one option.

Problem: Unambiguous data are rare (<0.25%, based on LWF's analysis)

Unambiguous (UNAMB) data:
 "Look - a red bottle! Hmm - there doesn't seem to be another one here, though."



one's referent = BOTTLE? If so, *one's* antecedent = "bottle".
 But it's strange to claim there's not another *bottle* here.
 So, *one's* referent must be RED BOTTLE, and *one's* antecedent = $[_{N'} \text{red}[_{N_0} \text{bottle}]]$.

Anaphoric *One*: The available data

Acquisition: Children must learn the right syntactic category for *one*, and the right interpretation preference for *one* in situations with more than one option.

Problem: Most data children encounter are ambiguous.

Syntactically (SYN) ambiguous data:
 "Look - a bottle! Oh, look - another one."



one's referent = BOTTLE
one's antecedent = $[_{N'}[_{N_0} \text{bottle}]]$ or $[_{N_0} \text{bottle}]$?

Anaphoric *One*: The available data

Acquisition: Children must learn the right syntactic category for *one*, and the right interpretation preference for *one* in situations with more than one option.

Problem: Most data children encounter are ambiguous.

Semantically and syntactically (SEM-SYN) ambiguous:
 "Look - a red bottle! Oh, look - another one."



one's referent = RED BOTTLE or BOTTLE?
one's antecedent = $[_{N'} \text{red}[_{N_0} \text{bottle}]]$ or $[_{N'}[_{N_0} \text{bottle}]]$ or $[_{N_0} \text{bottle}]$?

Previous learning strategies

Update the initial state

Baker (1978) [**Baker**] (also Hornstein & Lightfoot 1981, Lightfoot 1982, Hamburger & Crain 1984, Crain 1991): **Only unambiguous data are informative.** Because they're so rare, they can't be responsible for the acquisition of *one*.

How then?
 Children have innate, domain-specific knowledge restricting the hypotheses about *one*: *one* cannot be syntactic category N^0 .

What about when there are multiple N' antecedents?
 $[_{N'} \text{red}[_{N_0} \text{bottle}]]$ or $[_{N'}[_{N_0} \text{bottle}]]$?
 (No specific proposal for this.)

Previous learning strategies

Update the initial state

Baker (1978) [Baker]


initial state

- Knowledge: Syntactic categories exist, in particular N⁰, N', and NP.
- Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.
- Bias: Only direct evidence of *one* is useful.
- Bias: Only unambiguous evidence of *one* is useful (Baker 1978).
- + (UG) Knowledge: *one* is not N⁰.

Previous learning strategies

Update the initial state

Regier & Gahl 2004 [R&G]: Sem-Syn ambiguous data can be leveraged, in addition to using unambiguous data.

"Look – a red bottle! Oh, look – another one!" 

How?

Use innate domain-general statistical learning abilities (Bayesian inference) to track how often *one*'s referent has the mentioned property (e.g. *red*). If the referent often has the property (RED BOTTLE), this is a suspicious coincidence unless the antecedent really does include the modifier ("red bottle") and *one*'s category is N'.

[_{N'} red [_{N'} _{N⁰} bottle]]

Previous learning strategies

Update the initial state

Regier & Gahl 2004 [R&G]


initial state

- Knowledge: Syntactic categories exist, in particular N⁰, N', and NP.
- Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.
- Bias: Only direct evidence of *one* is useful.
- ~~Bias: Only unambiguous evidence of *one* is useful (Baker 1978).~~
- + Bias: Use Bayesian inference.

Previous learning strategies

Update the initial state

Pearl & Lidz 2009 [P&L]: Syn ambiguous data must not be leveraged, even if Sem-Syn and unambiguous data are used.

"Look – a bottle! Oh, look – another one!" 

Why?

These data cause an "equal-opportunity" (EO) probabilistic learner to think *one*'s category is N⁰.

[_{N⁰} bottle]

How?

P&L propose a domain-specific learning bias to ignore just these ambiguous data, though they speculate how this bias could be derived from an innate domain-general preference for learning when there is local uncertainty.

Previous learning strategies

Update the initial state

Pearl & Lidz 2009 [P&L, R&G intended]

initial state


- Knowledge: Syntactic categories exist, in particular N^0 , N' , and NP.
- Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.
- Bias: Only direct evidence of *one* is useful.
- ~~Bias: Only unambiguous evidence of *one* is useful (Baker 1978).~~
- + Bias: Use Bayesian inference.
- + (UG?) Bias: Only Sem-Syn ambiguous and unambiguous data are useful.

Using indirect positive evidence

Pearl & Mis (2011, 2012 ms) [+OtherPro]: Other pronouns in the language can also be used anaphorically: *him, her, it, ...*

Look at the cute penguin. I want to hug *him/her/it*.
 $[_{NP} \text{ the } [_{N'} \text{ cute } [_{N^0} \text{ penguin}]]]] \longrightarrow [_{NP} \text{ him/her/it}]$

Look! A cute penguin. I want *one*.
 $[_{NP} \text{ a } [_{N'} \text{ cute } [_{N^0} \text{ penguin}]]]] \longrightarrow [_{NP} \text{ one}]$



Note: The issue of *one*'s category only occurs when *one* is used in a syntactic environment that indicates it is smaller than an NP (<NP).

Using indirect positive evidence


Pearl & Mis (2011, 2012 ms) [+OtherPro]: Track how often the referent of the anaphoric element (*one, him, her, it, etc.*) has the property mentioned in the potential antecedent, using innate domain-general statistical learning abilities (Bayesian inference).

Important: This applies, even when the syntactic category is known.

Look at the cute penguin. I want to hug *him/her/it*.

Look! A cute penguin. I want *one*.

Is the referent cute? Yes!
So the antecedent includes the modifier "cute".



Using indirect positive evidence

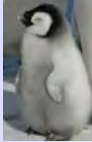
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Important: This applies, even when the syntactic category is known.

Look at the cute penguin. I want to hug *him/her/it*.

Look! A cute penguin. I want *one*.

Data points like those above will always include the modifier in the antecedent, since the category of the pronoun is NP and so the antecedent is the entire NP. These data are unambiguous: the referent must have the mentioned property & the antecedent must include the modifier corresponding to that property.



Using indirect positive evidence

Pearl & Mis (2011, 2012 ms) [+OtherPro]

initial state

Knowledge: Syntactic categories exist, in particular N⁰, N', and NP.
 Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

~~Bias: Only direct evidence of *one* is useful.~~

~~Bias: Only unambiguous evidence of *one* is useful (Baker 1976).~~

+ Bias: Use Bayesian inference.

+ (UG?) Bias: Learn from other pronoun data.

Data set comparisons: Learners using syntactic and semantic information

Unamb <NP

"Look - a red bottle! Hmmm - there doesn't seem to be another *one* here, though."



Learners: Baker, R&G, P&L's EO, +OtherPro

Sem-Syn Amb

"Look - a red bottle! Oh, look - another *one*!"



Learners: R&G, P&L's EO, +OtherPro

Syn Amb

"Look - a bottle! Oh, look - another *one*!"



Learners: P&L's EO, +OtherPro

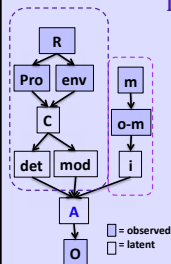
Unamb NP

"Look - a red bottle! I want *one/it*."



Learners: +OtherPro

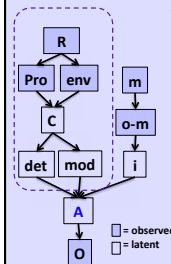
Information in the data




Understanding a referential expression

Includes both syntactic and semantic/referential information, since both are used to determine the linguistic antecedent.

Information in the data



"Look, a red bottle! Look, another one!" 


Syntactic information

R = referential expression used
ex: "another one"

Pro = pronoun used in referential expression
ex: "one"

Env = smaller than NP?
ex: yes

Information in the data

"Look, a red bottle! Look, another one!" 

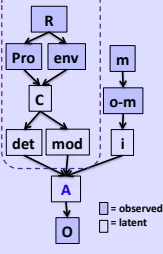
Syntactic information

C = syntactic category of pronoun used (= syntactic category of linguistic antecedent)
ex: N'


det = antecedent includes determiner?
ex: no

mod = antecedent includes modifier?
ex: yes

= observed
 = latent



Information in the data

"Look, a red bottle! Look, another one!" 

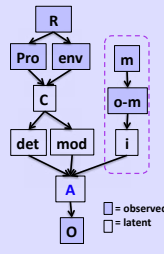
Semantic/referential information

m = property mentioned in potential antecedent
ex: yes


o-m = referent (object) in current context has mentioned property
ex: yes

i = mentioned property is included in antecedent?
ex: yes


= observed
 = latent



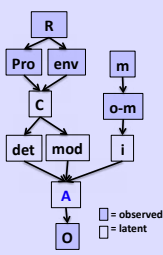
Information in the data

"Look, a red bottle! Look, another one!" 


A = antecedent
ex: "red bottle"
(depends on both syntactic information of **det** and **mod**, and semantic/referential information from I)

O = intended object (learner can usually observe this)
ex: RED BOTTLE 

= observed
 = latent



Information in the data: Unamb <NP


"Look, a red bottle! Hmm - there isn't another one here though!" 

R = "another one"
Pro = "one"
env = <NP

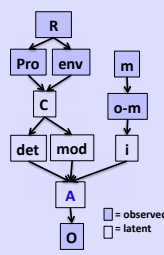
m = yes
o-m = yes

C = N'
det = no
mod = yes


i = yes

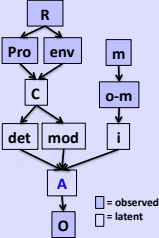
A = "red bottle"
O = RED BOTTLE 

= observed
 = latent



Information in the data: Sem-Syn ambiguous

"Look, a red bottle! Look - another one!" 




R = "another one"
 Pro = "one"
 env = <NP


m = yes
 o-m = yes

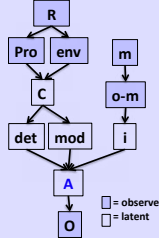
C = N' or N⁰?
 det = no
 mod = yes or no? i = yes or no?

A = "red bottle" or "bottle"?
 O = RED BOTTLE



Information in the data: Syn ambiguous

"Look, a bottle! Look - another one!" 




R = "another one"
 Pro = "one"
 env = <NP


m = no
 o-m = N/A

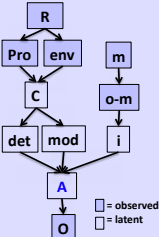
C = N' or N⁰?
 det = no
 mod = no i = N/A

A = "bottle"
 O = BOTTLE



Information in the data: Unamb NP

"Look, a red bottle! I want it." 




R = "it"
 Pro = "it"
 env = NP

m = yes
 o-m = yes

C = NP
 det = yes
 mod = yes i = yes

A = "a red bottle"
 O = RED BOTTLE




The online probabilistic framework

When an object has the property mentioned in the potential antecedent (o-m=yes), tracking the probability that the property is included in the antecedent (i=yes):

$$p_{incl} = p(i=yes \mid o-m=yes)$$


Two values: (i=yes or i=no)



When the syntactic environment indicates the category is smaller than NP, tracking the probability that the syntactic category is N' (C=N'):

$$p_{N'} = p(C=N' \mid env=<NP)$$

Two values: (C=N' or C=N⁰)



The online probabilistic framework

General form of update equations for p_x (adapted from Chew 1971):

$$p_x = \frac{\alpha + \text{data}_x}{\alpha + \beta + \text{totaldata}_x} \quad (\alpha = \beta = 1) \text{ A very weak prior}$$

data seen suggesting x is true
total informative data seen w.r.t x

After every informative data point encountered:
 $\text{data}_x = \text{data}_x + \phi_x$ Incremented by probability that data point suggests x is true

$\text{totaldata}_x = \text{totaldata}_x + 1$ One informative data point seen

The online probabilistic framework: Updating p_{incl}

	ϕ_{incl}	Explanation
Unamb <NP	1	Property definitely included
Unamb NP	1	Property definitely included
Syn Amb	N/A	Not informative for p_{incl}
Sem-Syn Amb	$\frac{rep_1}{rep_1 + rep_2 + rep_3}$	Probability property is included

$rep_1 = p_N * \frac{m}{m+n} * p_I$ Category = N', choose N' with modifier, property is included
 $rep_2 = p_N * \frac{n}{m+n} * (1 - p_{inc}) * \frac{1}{s}$ Category = N', choose N' without modifier, property is not included, choose object with property by chance
 $rep_3 = (1 - p_N) * (1 - p_{inc}) * \frac{1}{s}$ Category = N⁰, property is not included, choose object with property by chance

The online probabilistic framework: Updating $p_{N'}$

	$\phi_{N'}$	Explanation
Unamb <NP	1	Category definitely N'
Unamb NP	N/A	Not informative for $p_{N'}$
Syn Amb	$\frac{rep_4}{rep_4 + rep_5}$	Probability category is N'
Sem-Syn Amb	$\frac{rep_1 + rep_2}{rep_1 + rep_2 + rep_3}$	Probability category is N'

$rep_1 = p_N * \frac{m}{m+n} * p_I$ Category = N', choose N' with modifier, property is included
 $rep_2 = p_N * \frac{n}{m+n} * (1 - p_{inc}) * \frac{1}{s}$ Category = N', choose N' without modifier, property is not included, choose object with property by chance
 $rep_3 = (1 - p_N) * (1 - p_{inc}) * \frac{1}{s}$ Category = N⁰, property is not included, choose object with property by chance

The online probabilistic framework: Updating $p_{N'}$

	$\phi_{N'}$	Explanation
Unamb <NP	1	Category definitely N'
Unamb NP	N/A	Not informative for $p_{N'}$
Syn Amb	$\frac{rep_4}{rep_4 + rep_5}$	Probability category is N'
Sem-Syn Amb	$\frac{rep_1 + rep_2}{rep_1 + rep_2 + rep_3}$	Probability category is N'

$rep_4 = p_N * \frac{n}{m+n}$ Category = N', choose N' without modifier
 $rep_5 = 1 - p_N$ Category = N⁰

Example updates

Start with $p_N = p_{incl} = 0.50$, $m = 1$, $n = 2.9$, $s = 10$
[from P&L]

One Unamb <NP data point: $p_N = 0.67$, $p_{incl} = 0.67$

One Unamb NP data point: $p_N = 0.50$, $p_{incl} = 0.67$

One Sem-Syn Amb data point: $p_N = 0.59$, $p_{incl} = 0.53$

One Syn Amb data point: $p_N = 0.48$, $p_{incl} = 0.50$

Corpus Analysis & Learner Input

Brown/Eve corpus (CHILDES: MacWhinney 2000): starting at 18 months
 17,521 utterances of child-directed speech, 2874 referential pronoun utterances

Unamb <NP	0.00%
Sem-Syn Amb	0.66%
Syn Amb	7.52%
Unamb NP	8.42%
Uninformative	83.4%

Pearl & Lidz (2009): Children learn *one's* representation between 14 and 18 months.

Based on estimates of the number of utterances children hear from birth until 18 months (Akhtar et al., 2004), we can calculate the data distribution in their input (36,500 referential pronoun utterances total).

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 17,521 utterances of child-directed speech, 2874 referential pronoun utterances

		Baker	R&G	P&L's EO	P&M
Unamb <NP	0.00%	0	0	0	0
Sem-Syn Amb	0.66%	0	242	242	242
Syn Amb	7.52%	0	0	2743	2743
Unamb NP	8.42%	0	0	0	3073
Uninformative	83.4%	36500	36258	33515	30442

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Free parameters:
 $m=1$, $n=2.9$ (from corpus estimates deon by P&L)

s (concerns number of salient properties learner is considering):
 Child may only be aware of a few salient properties or may consider all known properties (# of adjectives known by 16 months \approx 49 (MacArthur CDI: Dale & Fenson 1996). Use range from 2 to 49.

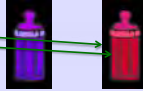
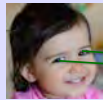
Measures of Success: LWF children's behavior

In addition to directly assessing p_{incl} and p_{N^0} , we can measure how often a learner would reproduce the behavior in the LWF experiment (p_{beh}).

Look - a red bottle!



Do you see another one?



Measures of Success: LWF children's behavior

In addition to directly assessing p_{incl} and p_{N^0} , we can measure how often a learner would reproduce the behavior in the LWF experiment (p_{beh}).

2 choices
 $s = 2$



$$p_{beh} = \frac{rep_1 + rep_2 + rep_3}{rep_1 + 2 * rep_2 + 2 * rep_3}$$

Any outcome where learner looks at red bottle
Additional two outcomes where learner looks at other bottle

$$rep_1 = p_{N^0} * \frac{m}{m+n} * p_{incl} \quad \text{Category} = N', \text{ antecedent} = \text{"red bottle"}$$

$$rep_2 = p_{N^0} * \frac{n}{m+n} * (1 - p_{incl}) * \frac{1}{s} \quad \text{Category} = N', \text{ antecedent} = \text{"bottle"}$$

$$rep_3 = (1 - p_{N^0}) * (1 - p_{incl}) * \frac{1}{s} \quad \text{Category} = N^0, \text{ antecedent} = \text{"bottle"}$$

Testing LWF's assumption about what behavior means

In addition to directly assessing the learner's behavior, we can assess LWF's assumption that target behavior indicates the children have the target representation for *one*.

Is it possible to get target behavior in the LWF experiment without having the target representation for *one* in general (as measured by p_{incl} and p_{N^0})?

Is it possible to get target behavior in the LWF experiment without having the target representation for *one* at the time the behavior is being produced?

$$p_{rep|beh} = \frac{rep_1}{rep_1 + rep_2 + rep_3}$$

the probability the look to the red bottle is because the learner has the target representation (N' , "red bottle") given that the learner looks at the red bottle

Learner results: Strategy comparison

Averages over 1000 simulations, standard deviations in parentheses.
 $s = 2, 5, 7, 10, 20, 49$

Baker	
p_{incl}	0.50 (<0.01)
p_{N^0}	0.50 (<0.01)
p_{beh}	0.56 (<0.01)
$p_{rep beh}$	0.23 (<0.01)

Since the input data include no Unambiguous <NP data, and those are the only data the Baker learner learns from, it learns nothing.

It is at chance for having the target syntactic and semantic representation.

It is only slightly above chance at producing the **observed toddler behavior**, and when it does, it **unlikely to have the target representation when doing so**.

Implication: This is an induction problem if only unambiguous <NP data are relevant.

Learner results: Strategy comparison

Averages over 1000 simulations, standard deviations in parentheses.
s = 2, 5, 7, 10, 20, 49

	Baker	+OtherPro
P _{incl}	0.50 (<0.01)	>0.99 (<0.01)
P _{N'}	0.50 (<0.01)	0.34-0.38 (0.03-0.05)
P _{beh}	0.56 (<0.01)	>0.99 (<0.01)
P _{repr beh}	0.23 (<0.01)	>0.99 (<0.01)

The learner robustly decides the antecedent should include the mentioned property.

However, the learner has a moderate dispreference for believing *one* is N' when it is smaller than NP.

This is therefore not the target representation.

Learner results: Strategy comparison

Averages over 1000 simulations, standard deviations in parentheses.
s = 2, 5, 7, 10, 20, 49

	Baker	+OtherPro
P _{incl}	0.50 (<0.01)	>0.99 (<0.01)
P _{N'}	0.50 (<0.01)	0.34-0.38 (0.03-0.05)
P _{beh}	0.56 (<0.01)	>0.99 (<0.01)
P _{repr beh}	0.23 (<0.01)	>0.99 (<0.01)

However...this learner still generates the observed toddler behavior (not what LWF would expect) with high probability, and has the target representation when doing so (is what LWF would expect).

Why? "Because the learner believes so strongly that a mentioned property must be included in the antecedent, the only representation that allows this (e.g., [_{N'} red]_{[N₀ bottle]])] overpowers the other potential representations' probabilities. Thus, the +OtherPro learner will conclude the antecedent includes the mentioned property, and so it and the referential pronoun referring to it (one) must be N' in this context - even if the learner believes one is not N' in general."}

Learner results: Strategy comparison

Averages over 1000 simulations, standard deviations in parentheses.
s = 7, 10, 20, 49

	Baker	R&G	+OtherPro
P _{incl}	0.50 (<0.01)	0.91-0.99 (<0.01)	>0.99 (<0.01)
P _{N'}	0.50 (<0.01)	0.98-0.99 (<0.01)	0.37-0.38 (0.04-0.05)
P _{beh}	0.56 (<0.01)	0.88-0.99 (<0.01)	>0.99 (<0.01)
P _{repr beh}	0.23 (<0.01)	0.87-0.99 (<0.01)	>0.99 (<0.01)

Other learning strategies: R&G (P&L's filtered learner)

Variability, depending on the value of s, which determines how suspicious a coincidence it is that the intended object just happens to have the mentioned property.

When s = 7 or above, this learner believes a mentioned property should be included in the antecedent and *one* is N' when it is smaller than NP, which is similar to previous findings by R&G & P&L. In addition, it is likely to generate the observed toddler behavior, and have the target representation when doing so.

Learner results: Strategy comparison

Averages over 1000 simulations, standard deviations in parentheses.
s = 5

	Baker	R&G	+OtherPro
P _{incl}	0.50 (<0.01)	0.68 (<0.01)	>0.99 (<0.01)
P _{N'}	0.50 (<0.01)	0.94 (<0.01)	0.36 (0.04)
P _{beh}	0.56 (<0.01)	0.70 (<0.01)	>0.99 (<0.01)
P _{repr beh}	0.23 (<0.01)	0.58 (<0.01)	>0.99 (<0.01)

Other learning strategies: R&G (P&L's filtered learner)

Variability, depending on the value of s, which determines how suspicious a coincidence it is that the intended object just happens to have the mentioned property.

However, when s=5, the learner is less sure the mentioned property should be included in the antecedent, which causes the learner to be less likely to generate the observed toddler behavior, and only slightly above chance at having the target representation when generating that behavior.

Learner results: Strategy comparison

Averages over 1000 simulations, standard deviations in parentheses.
s = 2

	Baker	R&G	+OtherPro
P_{incl}	0.50 (<0.01)	0.02 (<0.01)	>0.99 (<0.01)
P_N	0.50 (<0.01)	0.34 (<0.01)	0.34 (0.03)
P_{beh}	0.56 (<0.01)	0.50 (<0.01)	>0.99 (<0.01)
$P_{replbeh}$	0.23 (<0.01)	<0.01 (<0.01)	>0.99 (<0.01)

Other learning strategies: R&G (P&L's filtered learner)
Variability, depending on the value of s, which determines how suspicious a coincidence it is that the intended object just happens to have the mentioned property.

When s=2, the learner is **sure the mentioned property should not be included** in the antecedent, and prefer **one** to be N⁰ when it is smaller than NP. This causes the learner to be **at chance for generating the observed toddler behavior**, and **very unlikely to have the target representation** when generating that behavior.

Learner results: Strategy comparison

Averages over 1000 simulations, standard deviations in parentheses.
s = 2, 5

	Baker	R&G	+OtherPro
P_{incl}	0.50 (<0.01)	0.02, 0.68 (<0.01)	>0.99 (<0.01)
P_N	0.50 (<0.01)	0.34, 0.94 (<0.01)	0.34-0.36 (0.03-0.04)
P_{beh}	0.56 (<0.01)	0.50, 0.70 (<0.01)	>0.99 (<0.01)
$P_{replbeh}$	0.23 (<0.01)	<0.01, 0.58 (<0.01)	>0.99 (<0.01)

What's going on?

If the suspicious coincidence isn't strong enough, Sem-Syn ambiguous data don't help the learner increase P_{incl} – in fact, they cause P_{incl} to drop. Because both P_{incl} and P_N are used to calculate Φ_{incl} and Φ_N , a very low P_{incl} can eventually drag P_N down.

Ex: s=2
If the first 20 data points are Sem-Syn ambiguous data points, $P_{incl} = 0.12$ and $P_N = 0.48$.

Learner results: Strategy comparison

Averages over 1000 simulations, standard deviations in parentheses.
s = 2, 5, 7, 10

	Baker	R&G	P&L's EO	+OtherPro
P_{incl}	0.50 (<0.01)	0.02-0.96 (<0.01)	<0.01-0.38 (<0.01-0.18)	>0.99 (<0.01)
P_N	0.50 (<0.01)	0.34-0.99 (<0.01)	0.14-0.25 (<0.01-0.06)	0.34-0.37 (0.03-0.04)
P_{beh}	0.56 (<0.01)	0.50-0.98 (<0.01)	0.50-0.53 (<0.01-0.04)	>0.99 (<0.01)
$P_{replbeh}$	0.23 (<0.01)	<0.01-0.95 (<0.01)	<0.01-0.11 (<0.01-0.11)	>0.99 (<0.01)

Other learning strategies: P&L's EO learner
Variability, depending on the value of s, which determines how suspicious a coincidence it is that the intended object just happens to have the mentioned property.

When s is less than 10, the learner does **not believe the mentioned property should be included** in the antecedent, and prefers **one** to be N⁰ when it is smaller than NP. This causes the learner to be **at chance at generating the observed toddler behavior**, and **unlikely to have the target representation** when generating that behavior.

Learner results: Strategy comparison

Averages over 1000 simulations, standard deviations in parentheses.
s = 20, 49

	Baker	R&G	P&L's EO	+OtherPro
P_{incl}	0.50 (<0.01)	0.99 (<0.01)	0.93-0.99 (<0.01-0.03)	>0.99 (<0.01)
P_N	0.50 (<0.01)	0.99 (<0.01)	0.34-0.37 (0.05)	0.37-0.38 (0.04-0.05)
P_{beh}	0.56 (<0.01)	0.98-0.99 (<0.01)	0.79-0.94 (0.02-0.07)	>0.99 (<0.01)
$P_{replbeh}$	0.23 (<0.01)	0.98-0.99 (<0.01)	0.72-0.94 (0.02-0.11)	>0.99 (<0.01)

Other learning strategies: P&L's EO learner
Variability, depending on the value of s, which determines how suspicious a coincidence it is that the intended object just happens to have the mentioned property.

However, when s is 20 or 49, the learner **strongly believes the mentioned property should be included** in the antecedent, though it still prefers **one** to be N⁰ when it is smaller than NP. This causes the learner to be **likely to generate the observed toddler behavior**, and **likely to have the target representation** when generating that behavior.

This is more like the +OtherPro learner results.

Learner results: Strategy comparison

Averages over 1000 simulations, standard deviations in parentheses.

$s = 20, 49$

	Baker	R&G	P&L's EO	+OtherPro
p_{incl}	0.50 (<0.01)	0.99 (<0.01)	0.93-0.99 (<0.01-0.03)	>0.99 (<0.01)
p_N	0.50 (<0.01)	0.99 (<0.01)	0.34-0.37 (0.05)	0.37-0.38 (0.04-0.05)
p_{beh}	0.56 (<0.01)	0.98-0.99 (<0.01)	0.79-0.94 (0.02-0.07)	>0.99 (<0.01)
$p_{replbeh}$	0.23 (<0.01)	0.98-0.99 (<0.01)	0.72-0.94 (0.02-0.11)	>0.99 (<0.01)

What's going on?

The flip side of what we saw with the R&G learner: If the suspicious coincidence is very strong, Sem-Syn ambiguous data help the learner increase p_{incl} (and p_N) – in fact, they become almost as powerful as Unambiguous <NP data. Because both p_{incl} and p_N are used to calculate ϕ_{incl} and ϕ_N , a very high p_{incl} can bolster p_N and overpower the effect of the troublesome Syn ambiguous data.

Learner results: Strategy comparison

Averages over 1000 simulations, standard deviations in parentheses.

$s = 2, 5, 7, 10, 20, 49$

	Baker	R&G	P&L's EO	+OtherPro
p_{incl}	0.50 (<0.01)	0.02-0.99 (<0.01)	<0.01-0.99 (<0.01-0.18)	>0.99 (<0.01)
p_N	0.50 (<0.01)	0.34-0.99 (<0.01)	0.14-0.37 (<0.01-0.06)	0.34-0.38 (0.03-0.05)
p_{beh}	0.56 (<0.01)	0.50-0.99 (<0.01)	0.50-0.94 (<0.01-0.07)	>0.99 (<0.01)
$p_{replbeh}$	0.23 (<0.01)	<0.01-0.95 (<0.01)	<0.01-0.94 (<0.01-0.11)	>0.99 (<0.01)

Why isn't the +OtherPro learner as susceptible to changing s values?

Unambiguous NP data only ever increase p_{incl} , no matter what the value of s . So, because there are so many of them, they can overwhelm the effect of Sem-Syn ambiguous data on p_{incl} (whether s is low or high). This helps keep p_N from plummeting, though it still drops due to the troublesome Syn ambiguous data in the learner's intake.

Learner results: Strategy comparison

Averages over 1000 simulations, standard deviations in parentheses.

$s = 2, 5, 7, 10, 20, 49$

	Baker	R&G	P&L's EO	+OtherPro
p_{incl}	0.50 (<0.01)	0.02-0.99 (<0.01)	<0.01-0.99 (<0.01-0.18)	>0.99 (<0.01)
p_N	0.50 (<0.01)	0.34-0.99 (<0.01)	0.14-0.37 (<0.01-0.06)	0.34-0.38 (0.03-0.05)
p_{beh}	0.56 (<0.01)	0.50-0.99 (<0.01)	0.50-0.94 (<0.01-0.07)	>0.99 (<0.01)
$p_{replbeh}$	0.23 (<0.01)	<0.01-0.95 (<0.01)	<0.01-0.94 (<0.01-0.11)	>0.99 (<0.01)

Take away points:

An indirect positive evidence learning strategy has a beneficial impact on learning anaphoric *one* – it makes the learner's behavior robust, no matter how suspicious a coincidence the Sem-Syn ambiguous data are (or aren't).

A learner using an indirect positive evidence strategy can generate target behavior without reaching the target state – instead, this learner has a context-sensitive representation (depending on whether a property was mentioned).

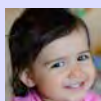
Recap: Learning strategies & induction problems

"...using a learning strategy that draws on indirect positive evidence, a child would be able to produce the behavior at 18 months that was thought to indicate the target knowledge state, presumably solving the induction problem."

"However, surprisingly, this behavior can be produced without reaching the target state – instead, a child with an immature context-dependent representation of one could produce the observed behavior. This suggests that the link between observed behavior, interpretation, and representation may not be as clear cut as once thought. Even though children demonstrate they have the adult interpretation some of the time (by displaying adult-like behavior), this does not necessarily mean they have the adult representation all of the time."

Recap: Learning strategies & induction problems

"...the learning period may not be restricted to 18 months. Instead, it could be that children achieve the target knowledge state later on. If so, this means they may have access to additional data, knowledge, and learning capabilities to solve the induction problem that we did not allow the learners modeled here...More generally, it would suggest a two-stage acquisition trajectory for anaphoric one, with the first stage completed by 18 months and the second stage completed sometime afterwards."



Recap: Motivating UG

What kind of biases does the +OtherPro learner use?

initial state: Two new biases

Knowledge: Syntactic categories exist, in particular N^0 , N' , and NP.

Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

+ Bias: Use Bayesian inference.

+ Bias: Learn from other pronoun data.

Bias to use Bayesian inference: innate, domain-general statistical learning ability (not UG)

Recap: Motivating UG

What kind of biases does the +OtherPro learner use?

initial state: Two new biases

Knowledge: Syntactic categories exist, in particular N^0 , N' , and NP.

Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

+ (non-UG) Bias: Use Bayesian inference.

+ Bias: Learn from other pronoun data.

Bias to learn from other pronoun data: concerns language data, so clearly domain-specific

innate or derived?

If innate, then this is a UG bias.

Could be derived from prior linguistic experience with pronouns (and noticing overlapping syntactic environments for "one" and other referential pronouns.)

Recap: Motivating UG

What kind of biases does the +OtherPro learner use?

initial state: Two new biases

Knowledge: Syntactic categories exist, in particular N^0 , N' , and NP.

Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

+ (non-UG) Bias: Use Bayesian inference.

+ Bias: Learn from other pronoun data.

Bias to learn from other pronoun data: "...if [it] is innate, this is then a specific proposal about the contents of UG that differs from the original Baker proposal: Instead of explicitly limiting the hypothesis space, the desired behavior can be produced by broadening the data intake. If [it] is instead derived, this is a non-UG learning strategy that will produce the desired behavior, in addition to the the potentially non-UG one proposed by the R&G/P&L filtering strategy which restricts the data intake."

Other induction problem characterizations

A different target state

Baker 1978 & Foraker et al. 2009

target state

One is category N' and its antecedent includes the modifier.

Just learning about the syntactic representation of *one* when it is smaller than NP.

Baker's original proposal:

initial state includes UG knowledge that *one* is not N⁰.

Other induction problem characterizations

A different target state

Baker 1978 & Foraker et al. 2009

target state

One is category N' and its antecedent includes the modifier.

Just learning about the syntactic representation of *one* when it is smaller than NP.

Foraker et al.'s proposal:

Use Bayesian inference on the available syntactic data only, given domain-specific knowledge of complements and modifiers.

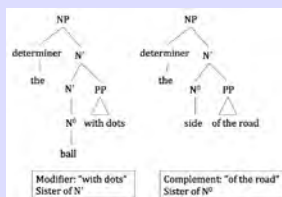
Modifiers & Complements

Syntactic modifier: not "conceptually evoked by its head noun", indicates noun string is N'

Ex: "the ball with dots" (I like the one with dots.)

Syntactic complement: "conceptually evoked by its head noun", indicates noun string is N⁰

Ex: "the side of the road" (*I waited by the one of the road.)



The Foraker et al. learning strategy

Foraker et al. 2009

initial state

Knowledge: Syntactic categories exist, in particular N⁰, N', and NP.

Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

- + Bias: Only syntactic data are useful.
- + Bias: Use Bayesian inference.
- + Bias: Learn from all linguistic elements that take complements or modifiers.
- + Knowledge: Complements conceptually evoke their head noun while modifiers do not.
- + Knowledge: Syntactic category N⁰ is sister to a complement, not a modifier.

This strategy was successful at learning *one* is category N' (not N⁰) from child-directed speech data.

Foraker et al. bias types

Foraker et al. 2009

initial state

Knowledge: Syntactic categories exist, in particular N⁰, N', and NP.Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

+ Bias: Only syntactic data are useful.

This bias could be **derived** from the target knowledge only pertaining to the syntactic representation.

Foraker et al. bias types

Foraker et al. 2009

initial state

Knowledge: Syntactic categories exist, in particular N⁰, N', and NP.Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

+ (non-UG) Bias: Only syntactic data are useful.

+ Bias: Use Bayesian inference.

This bias is likely **innate** and **domain-general**.

Foraker et al. bias types

Foraker et al. 2009

initial state

Knowledge: Syntactic categories exist, in particular N⁰, N', and NP.Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

+ (non-UG) Bias: Only syntactic data are useful.

+ (non-UG) Bias: Use Bayesian inference.

+ Bias: Learn from all linguistic elements that take complements or modifiers.

This indirect positive evidence bias is clearly **domain-specific**. It could be specified **innately**, though it could possibly be **derived** by noticing salient properties of nominal phrases.

Foraker et al. bias types

Foraker et al. 2009

initial state

Knowledge: Syntactic categories exist, in particular N⁰, N', and NP.Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

+ (non-UG) Bias: Only syntactic data are useful.

+ (non-UG) Bias: Use Bayesian inference.

+ (UG?) Bias: Learn from all linguistic elements that take complements or modifiers.

+ Knowledge: Complements conceptually evoke their head noun while modifiers do not.

Knowing complements evoke their head nouns while modifiers do not is **domain-specific** knowledge that is **not** obviously derivable.

Foraker et al. bias types

Foraker et al. 2009

initial state

Knowledge: Syntactic categories exist, in particular N^0 , N' , and NP.

Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

- + (non-UG) Bias: Only syntactic data are useful.
- + (non-UG) Bias: Use Bayesian inference.
- + (UG?) Bias: Learn from all linguistic elements that take complements or modifiers.
- + (UG) Knowledge: Complements conceptually evoke their head noun while modifiers do not.
- + Knowledge: Syntactic category N^0 is sister to a complement, not a modifier.

Knowing N^0 is sister to complement is also domain-specific knowledge that is not obviously derivable.

Foraker et al. bias types

Foraker et al. 2009

initial state

Knowledge: Syntactic categories exist, in particular N^0 , N' , and NP.

Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

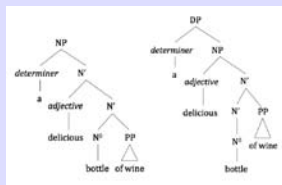
- + (non-UG) Bias: Only syntactic data are useful.
- + (non-UG) Bias: Use Bayesian inference.
- + (UG?) Bias: Learn from all linguistic elements that take complements or modifiers.
- + (UG) Knowledge: Complements conceptually evoke their head noun while modifiers do not.
- + (UG) Knowledge: Syntactic category N^0 is sister to a complement, not a modifier.

Upshot: This form of the induction problem leads to a different proposal for the contents of UG, even when Bayesian inference is used.

Other induction problem characterizations

A different initial & target state: Alternate theoretical representations

N^0 , N' , and NP vs. N^0 , N' , NP, and DP



Other induction problem characterizations

A different initial & target state: Syntactic categories N^0 , N' , NP, DP

initial state

Knowledge: Syntactic categories exist, in particular N^0 , N' , NP, and DP.

Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

Bias: Only direct evidence of *one* is useful.

Bias: Only unambiguous evidence of *one* is useful.

target state

Knowledge: In utterances like "Look, a red bottle! Look, another one!", *one* is category NP and so its antecedent includes the modifier ("red").

Other induction problem characterizations

A different initial & target state: Syntactic categories N^0 , N' , NP, DP

What an indirect positive evidence strategy like +OtherPro would do

initial state

Knowledge: Syntactic categories exist, in particular N^0 , N' , NP, and DP.

Knowledge: Anaphoric elements like *one* take linguistic antecedents of the same category.

Bias: Only direct evidence of *one* is useful. —

Bias: Only unambiguous evidence of *one* is useful.

- + (non-UG) Bias: Use Bayesian inference
- + (UG?) Bias: Learn from other pronoun data.

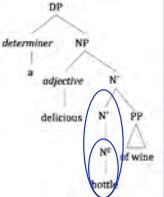
Other induction problem characterizations

A different initial & target state: Syntactic categories N^0 , N' , NP, DP

What an indirect positive evidence strategy like +OtherPro would do

(1) Syn ambiguous data still ambiguous between two categories (N^0 and N'), and Bayesian inference causes learner to prefer the hypotheses that includes fewer strings, which is still the N^0 category. (N' includes noun+complement strings)

Syn ambiguous data still cause $p_{N'}$ to drop, though perhaps not as fast.



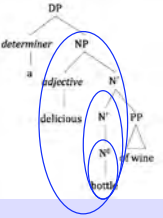
Other induction problem characterizations

A different initial & target state: Syntactic categories N^0 , N' , NP, DP

What an indirect positive evidence strategy like +OtherPro would do

(2) Sem-Syn ambiguous data still ambiguous between three antecedents. When s is high enough (>5), the suspicious coincidence still causes the learner to increase p_{incl} .

Sem-Syn ambiguous data still cause p_{incl} to increase when the suspicious coincidence is strong enough.



Other induction problem characterizations

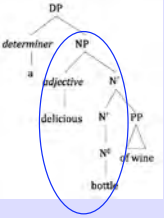
A different initial & target state: Syntactic categories N^0 , N' , NP, DP

What an indirect positive evidence strategy like +OtherPro would do

(3) Unambiguous <DP data still indicate antecedent that includes modifier – it's just that the category label is NP (rather than N').

p_{incl} and p_{NP} both increase.

Unambiguous <DP data still cause p_{incl} and the category that includes the modifier (NP) to increase.



Other induction problem characterizations

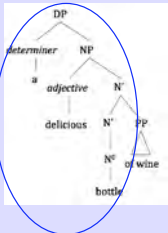
A different initial & target state: Syntactic categories N^0 , N' , NP, DP

What an indirect positive evidence strategy like +OtherPro would do

(4) Unambiguous DP data still indicate antecedent that includes modifier – it's just that the category label is DP (rather than NP).

p_{incl} Still increases.

Unambiguous DP data still cause p_{incl} to increase.



Other induction problem characterizations

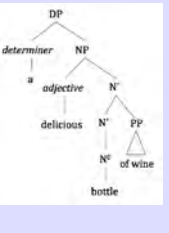
A different initial & target state: Syntactic categories N^0 , N' , NP, DP

What an indirect positive evidence strategy like +OtherPro would do

Given that the updates from the different data types are effectively the same, the overall outcome should be similar: p_{incl} should be high while p_{NP} should be low. (Note: p_w should also be very low, since no data cause it to increase.)

Non-target context-dependent representation.
 $p_{incl} = \text{high}$, $p_{NP} = \text{low}$

LWF experiment: target behavior (and target representation when displaying that behavior) because of p_{incl} .



Back to the big picture

Motivating UG through the **existence** of induction problems & the **solutions** to those induction problems

- Existence
 - Requires a specific characterization that defines initial state, data intake, learning period, and target state

Here: Specifying different forms of the induction problem for learning anaphoric *one*, drawing on theoretical and experimental data ...so we can compare different solutions

Back to the big picture

Motivating UG through the **existence** of induction problems & the **solutions** to those induction problems

- Existence
 - Requires a specific characterization that defines initial state, data intake, learning period, and target state
- Solutions
 - Exploring an indirect positive evidence learning strategy...
 - Can't reach the target state *but can generate observed behavior*, so maybe we need to redefine the induction problem (learning period is longer than 18 months).

Back to the big picture

About acquisition

- Solving induction problems in language may **proceed in stages**
 - Anaphoric *one* knowledge, pre- and post-18 months
- **The link between observed behavior and underlying knowledge is not always straight-forward**
 - Target behavior can be produced even without the target knowledge for anaphoric *one* when learning from both syntactic and semantic information. Specifically, context-dependent representations can result, even though the target representation is (purportedly) context-independent.

Take-home points

- Indirect evidence does **not necessarily mean indirect negative** evidence - it can come from considering a broader pool of informative data
- Indirect evidence does **not necessarily negate** the need for learning biases (of whatever kind)
- Considering indirect evidence and its impact on acquisition can help **define concrete proposals** about what is necessarily innate and domain-specific, and thus **what is in Universal Grammar**
- Knowing the impact of the necessary learning biases on acquisition may also inform us about the **acquisition trajectory**