Bootstrapping the Syntactic Bootstrapper: Probabilistic Labeling of Prosodic Phrases

Ariel Gutman, Isabelle Dautriche, Benoît Crabbé & Anne Christophe

To cite this article: Ariel Gutman, Isabelle Dautriche, Benoît Crabbé & Anne Christophe (2015) Bootstrapping the Syntactic Bootstrapper: Probabilistic Labeling of Prosodic Phrases, Language Acquisition, 22:3, 285-309, DOI: 10.1080/10489223.2014.971956

To link to this article: http://dx.doi.org/10.1080/10489223.2014.971956

Accepted author version posted online: 06 Oct 2014.
Published online: 15 Dec 2014.

Submit your article to this journal

Article views: 357

View related articles

View Crossmark data
Bootstrapping the Syntactic Bootstrapper: Probabilistic Labeling of Prosodic Phrases

Ariel Gutman
University of Konstanz

Isabelle Dautriche
Ecole Normale Supérieure, PSL Research University, CNRS, EHESS

Benoît Crabbé
Université Paris Diderot, Sorbonne Paris Cité, INRIA, IUF

Anne Christophe
Ecole Normale Supérieure, PSL Research University, CNRS, EHESS

The syntactic bootstrapping hypothesis proposes that syntactic structure provides children with cues for learning the meaning of novel words. In this article, we address the question of how children might start acquiring some aspects of syntax before they possess a sizeable lexicon. The study presents two models of early syntax acquisition that rest on three major assumptions grounded in the infant literature: First, infants have access to phrasal prosody; second, they pay attention to words situated at the edges of prosodic boundaries; third, they know the meaning of a handful of words. The models take as input a corpus of French child-directed speech tagged with prosodic boundaries and assign syntactic labels to prosodic phrases. The excellent performance of these models shows the feasibility of the syntactic bootstrapping hypothesis, since elements of syntactic structure can be constructed by relying on prosody, function words, and a minimal semantic knowledge.

1. INTRODUCTION

Children acquiring a language have to learn its phonology, its lexicon, and its syntax. For a long time researchers, focusing on children’s productions, thought that children start by learning the phonology of their language, then work on their lexicon, and only once they have a sufficient store of words do they start acquiring the syntax of their language (in correspondence to their productions—up to one year: babbling; 1 to 2 years: isolated words; at 2 years: first sentences). However, a wealth of experimental results has shown that children start acquiring the syntax of

Correspondence should be sent to Ariel Gutman, University of Konstanz, Zukunftskolleg, Box 216, 78457 Konstanz, Germany. E-mail: ariel.gutman@uni-konstanz.de

Color versions of one or more of the figures in the article can be found online at www.tandfonline.com/hlac.
their native language much earlier. For instance, at around 1 year of age they recognize certain function words (determiners) and appear to use them to categorize novel words (Shi & Melançon 2010). Indeed, it has been previously suggested that children may use the syntactic structure of sentences to facilitate their acquisition of word meanings (the syntactic bootstrapping hypothesis; Gleitman 1990). In this article, we address the question of how children might start acquiring some aspects of syntax before they possess a sizeable lexicon.

How might children infer the syntactic structure of sentences? Since prosody correlates with syntactic structure, and young children are sensitive to prosody, phrasal prosody has been suggested to help bootstrap the acquisition of syntax (Morgan 1986; Morgan & Demuth 1996). However, even though phrasal prosody provides some information regarding syntactic constituent boundaries, it does not provide information regarding the nature of these constituents (e.g., noun phrase, verb phrase). In this article, we address the question of whether such information can be retrieved from the input. Computational modeling is an essential step in answering this question, as it can test the usefulness of hypothesized sources of information for the learning process. Specifically, we propose a model that attempts to categorize prosodic phrases by relying on distributional information and a minimal semantic knowledge.

Several models have shown that distributional information is useful for categorization (Chemla et al. 2009; Mintz 2003; Mintz, Newport & Bever 2002; Redington, Crater & Finch 1998; Schütze 1995; St. Clair, Monaghan & Christiansen 2010). For instance, in the frequent frame model proposed by Mintz (2003), the model groups together all words X appearing in a context, or frame, of the type [A X B], where A and B are two words frequently occurring together. This model builds highly accurate syntactic categories based on only a few highly frequent contexts (e.g., [the X is] selecting nouns, or [you X the] selecting verbs). Importantly, young infants have been shown to use distributional information for categorizing words in a number of experiments using artificial languages (e.g., Gómez & Gerken 1999; Marchetto & Bonatti 2013) and natural languages (e.g., Heugten & Johnson 2010; Höhle et al. 2006). A common feature of all these approaches is that the most useful contexts for categorization turn out to contain function words, such as determiners, auxiliaries, pronouns, etc.

The models we present here rest on three major assumptions: (1) infants have access to phrasal prosody; (2) infants pay attention to “edge-words,” words situated at the edges of prosodic units; and (3) infants know the meaning of a handful of words, the semantic seed.

Regarding the first assumption, infants display sensitivity to prosody from birth on (e.g., Mehler et al. 1988). For example, 4-month-old children are sensitive to major prosodic breaks, displaying a preference for passages containing artificial pauses inserted at clause boundaries over passages containing artificial pauses within clauses (Jusczyk, Hohne & Mandel 1995). Sensitivity to smaller prosodic units is attested at 9 months of age (Gerken, Jusczyk & Mandel 1994). Slightly older infants use prosodic boundaries to constrain lexical access. That is, 13-month-old infants trained to recognize the word paper correctly reject sentences where both syllables of paper are present, but span across a prosodic boundary as in [the man with the highest pay][performs the most] (Gout, Christophe & Morgan 2004; see also Johnson 2008). Finally, older children have been shown to use phrasal prosody to constrain their online syntactic processing of sentences (Carvalho, Dautriche & Christophe 2013; Millotte et al. 2008). This early sensitivity to prosodic information has been mirrored by computational models succeeding in extracting information regarding syntactic boundaries from the speech signal (Pate & Goldwater 2011). In order to integrate this prosodic information directly, our models operate on a corpus of child-directed speech automatically tagged with prosodic boundaries. To our knowledge, no model to date has...
incorporated prosodic information in a model of category induction (but see Frank, Goldwater & Keller [2013] for the incorporation of sentence type).

The second assumption states that words situated at the edges of prosodic phrases play a special role. We are specifically interested in these words for two distinct reasons. First, words at edges tend to have a special status: Depending on the language, syntactic phrases typically either start with function words (or morphemes) and end with content words, or start with content words and end with function words. Focusing on words at the edges of prosodic phrases is therefore an easy way to enhance the weight of functional elements, which is desirable because function words are the elements that drive the classification in distributional models of syntactic categorization (Chemla et al. 2009; Mintz 2003; Redington, Crater & Finch 1998). Second, the infant literature shows that infants are especially sensitive to edge-words. For instance, words situated at the end of utterances are easier to segment than words situated in sentence-medial position (Seidl & Johnson 2006; Shukla, Nespor & Mehler 2007; Johnson, Seidl & Tyler 2014). Our model therefore relies on the edge-words of prosodic phrases to compute the most likely category of each prosodic phrase.

The third assumption states that children learning the grammatical categories of their language, presumably before their second birthday (e.g., Bernal et al. 2010; Brusini, Dehaene-Lambertz & Christophe 2009; Oshima-Takane et al. 2011), are equipped with a small lexicon to help them with this task. This assumption is highly plausible, as recent evidence has shown that infants as young as 6 to 9 months know the meaning of some nouns in their language (Bergelson & Swingley 2012; Parise & Cibra 2012; Tincoff & Jusczyk 2012). It seems, moreover, that they start learning the meanings of verbs at the age of 10 months (Bergelson & Swingley 2013). Children could group words together according to their semantic category as soon as they start to know the meaning of basic words. For example, they could start grouping together toy, car, and teddy bear because they all refer to concrete objects, and drink, eat, and play because they all refer to actions. Because nouns are likely to refer to objects and verbs to actions, these basic semantic categories may constitute a seed for the prototypical “noun” and “verb” grammatical categories.

In order to estimate the benefit of a small lexicon in our models of prosodic phrases categorization, we use this additional semantic knowledge, the semantic seed, in our second model.

The basic idea of the model is thus that prosodic boundaries signal syntactic boundaries (following Morgan 1986; Morgan & Demuth 1996), while function words (appearing at the edges of prosodic phrases) serve to label the prosodic phrases. For instance, in the following example, a sentence such as He’s eating an apple may be split into two prosodic phrases: [He’s eating] [an apple]. The first words of each of these prosodic phrases happen to be function words: he and an. These words may allow the models to attribute the first prosodic phrase to a class containing other verbal nuclei (VN, a phrase containing a verb and adjacent words such as auxiliaries and clitic pronouns), and the second one to a class containing other noun phrases (NP).

Input sentence He’s eating an apple.

Prosodic structure [He’s eating] [an apple]

Syntactic skeleton [He’s eating]_{VN} [an apple]_{NP}

In fact, the present model follows the syntactic skeleton proposal, according to which children may combine their knowledge of function words and prosodic boundaries to build an approximate
shallow syntactic structure (Christophe et al. 2008). We present two modeling experiments testing whether access to phrasal prosody, edge-words, and a semantic seed is sufficient to label prosodic phrases. The first model relies only on the first two assumptions: It has access to prosodic boundaries and gives a special status to edge-words. The second model further adds the semantic seed assumption.

In addition to these three major assumptions, both models also incorporate an additional, less crucial, constraint. In natural languages, function words tend to appear either at the beginning (on the left) or at the end (on the right) of syntactic phrases, and several experiments suggest that infants can deduce this by the age of 8 months (Bernard & Gervain 2012; Gervain & Werker 2013; Gervain et al. 2008; Hochmann, Endress & Mehler 2010). In French, function words tend to appear phrase-initially and content words phrase-finally. Accordingly, both our models incorporate a left-right asymmetry (although they could be rendered symmetric; see discussion).

The two models are presented in detail in the following.

2. EXPERIMENT 1

In this experiment, the model uses a clustering algorithm that explicitly relies on the intuition that in a head-initial language like French, the first word of a prosodic phrase is often a function word that is informative of the category of the prosodic phrase. This intuition is illustrated in Table 1. Consequently, in this experiment, classes are built by grouping together prosodic phrases that start with the same word (using frequent phrase-initial words). For instance, the prosodic phrase le petit oiseau désolé ‘the sad little bird’ would be assigned to a class labelled le ‘the (masc.)’.

2.1. Material

2.1.1. Input Corpus

We used the Lyon corpus collected by Demuth & Tremblay (2008) (available at http://childes.psy.cmu.edu/data/Romance/French/Lyon.zip), containing conversations with four

<table>
<thead>
<tr>
<th>Table 1</th>
<th>Examples from the Prosodically Augmented Corpus</th>
</tr>
</thead>
<tbody>
<tr>
<td>[Le petit oiseau désolé][NP est prêt à pleurer][VN]</td>
<td>‘The desolate little bird is nearly crying.’</td>
</tr>
<tr>
<td>[Elle prend][VN le petit cheval][NP]</td>
<td>‘She takes/the small horse.’</td>
</tr>
<tr>
<td>[Tu veux][VN que je reste là?]</td>
<td>‘You want/that I stay here?’</td>
</tr>
</tbody>
</table>

Note. The text is divided into prosodic phrases, which are labeled for evaluation according to their underlined lexical heads: VN = Verbal Nucleus; NP = Noun Phrase. For comparison, the function words that may help our classification model are given in boldface. These markings are reproduced on the corresponding word in the English translation.
children aged between 1 and 4 years, forming part of the CHILDES database (MacWhinney 2000). From the corpus, we extracted the orthographically transcribed raw text (ignoring all metadata), without the speech of the child itself, as we are interested only in child-directed speech. This resulted in approximately 180,000 utterances, consisting of approximately 700,000 words.

2.1.2. Prosodic Tagging of the Corpus

The model takes as input a corpus of orthographically transcribed speech (i.e., divided into word-like units),\(^1\) to which prosodic information (i.e., the segmentation of the speech onto prosodic phrases) was added. For the sake of simplicity, prosodic boundaries were automatically derived from the corpus relying on current linguistic theory, as explained in the following.

The raw corpus was syntactically analyzed by a state-of-the-art French parser (Crabbé & Candito 2008). The text was then automatically segmented into prosodic phrases, using the notion of the phonological phrase defined in the theory of prosody proposed by Nespor & Vogel (2007). This theory has the merit of being relatively explicit and is thus suitable for algorithmic implementation. In addition, it is accepted by a large part of the linguistic community.\(^2\) Moreover, the phonological phrases are generally comparable to the syntactic phrases we are interested in, namely the NP and VN (see Selkirk 1984). According to this theory, “[t]he domain of \(\phi\) [\(\phi\) = Phonological phrase] consists of a C [\(\phi\) = Clitic group] which contains a lexical head (X) and all Cs on its nonrecursive side [i.e., left side] up to the C that contains another head outside of the maximal projection of X” (Nespor & Vogel 2007:168).

The automated process also took into account the following optional reconstruction rule, whenever the prosodic phrase was followed by a short complement (up to three syllables): “A nonbranching \(\phi\) which is the first complement of X on its recursive side [i.e., right side] is joined into the \(\phi\) that contains X” (Nespor & Vogel 2007:173). The lexical head X (i.e., a noun, verb, adjective, adverb, or interjection) that appears in the definition allows us to assign a syntactic category to each prosodic phrase (namely, the phrasal category of X, as provided by the parser), which we consider as the correct category of the phrase for evaluation purposes. This lexical head often appears at the end of the prosodic phrase, though this is not always the case due to the previously mentioned reconstruction rule. Table 1 presents some examples taken from the prosodically tagged corpus.

As a final clean-up step, we discarded all utterances that consist of a single word, which amount to approximately 22% of our corpus. While single-word utterances may play a role in word learning (Lew-Williams, Pelucchi & Saffran 2011), they are not interesting for our purposes: Since they appear without context, they can hardly be classified syntactically without

---

\(^1\)We assume that our child model has knowledge of word boundaries. This assumption is reasonable in the case of function words because of their frequency (Hochmann et al. 2010). However, the age at which children have adult-like segmentation of the full speech signal is unknown (Nazzi et al. 2006; Ngon et al. 2013). Note that in our model this assumption is not crucial since we aim to categorize prosodic phrases rather than words.

\(^2\)See, however, the contrasting view of Lahiri & Plank (2010), who oppose the view that prosodic phrasing is strictly dependent on syntactic constituency. They claim that in Germanic languages functional elements often cliticize to the syntactic constituent preceding them, even though they syntactically belong to the following constituent, such as in the clause [drink a][pint of][milk a][day] where square brackets mark prosodic units (p. 376). If this is the case in child-directed speech, our predictive model would have to be adapted such that it takes into account frequent words both before and after the initial boundary of each prosodic phrase.
knowing their content. Moreover, they mostly consist of categories that are not of interest to us: A third of these utterances are interjections (‘oui’ ‘yes’, ‘oh’, etc.), and another third are proper names, according to the parser. Only 11% are VNs (mostly imperatives, e.g., ‘Regarde!’ ‘Look!’).

Our procedure resulted in a corpus with 246,013 prosodic phrases. In most of the experiments we divided the corpus into 10 nonconsecutive mini-corpora, each containing about 24,601 prosodic phrases, to estimate the variability in performance.

Although the results of the prosodic phrase segmentation procedure are good, they are not perfect, in part because the syntactic parser we used was not specifically designed to deal with spoken language. Nonetheless, a comparison of our algorithmic segmentation with segmentation conducted by human annotators on a sample of randomly selected sentences showed that our method gives satisfactory results for our needs: The human annotators annotated the prosodic boundaries of 30 written sentences following an example provided to them. The average agreement rate between the annotators and the algorithm was 84%, only slightly lower than the agreement rates between the annotators, 89%.

We also evaluated the quality of the syntactic labeling of the prosodic phrases by the parser: Two annotators categorized the head word of each prosodic phrase as noun, verb, or another category (since these are the categories that interest us most). Their interannotator agreement rate was 91%, and the average agreement rate with the label assigned by the parser was 79%, which we considered sufficient for our purposes.

2.2. Method

2.2.1. A Probabilistic Model

We use a Naive Bayes model to categorize prosodic phrases. In our case, we use this model to specifically express the class $C$ of each prosodic phrase in our corpus conditional to a series of $m$ independent predictor variables $V_i$.

$$p(C = c|V_0 = v_0 \ldots V_m = v_m) = \frac{p(C = c) \prod_{i=0}^{m} P(V_i = v_i|C = c)}{p(V_0 \ldots V_m)}$$ \hspace{1cm} (1)

For the specific case of predicting a class $\hat{c}$ given some known predictor variables, the decision rule amounts to maximizing the following formula:

$$\hat{c} = \arg\max_{c \in C} \prod_{i=0}^{m} P(V_i = v_i|C = c)$$ \hspace{1cm} (2)

This equation says that the predicted class $\hat{c}$ is the one that maximizes the product of its prior probability $p(C = c)$ and the conditional probability of the different predictor variables given the class value.

In this experiment, the set of classes $c \in C$ is defined as follows: the $k$ most frequent words at the beginning of the prosodic phrases containing at least two words are used to define $k$ classes, each of them initially corresponding to prosodic phrases starting with that frequent word. The parameter $k$ is allowed to vary from 5 to 70 in this experiment. This design captures the intuition
that in a head-initial language, the first words of prosodic phrases will usually be function words. Indeed, when $k$ is small, the most frequent phrase-initial words are function words. For instance, among the 50 most frequent phrase-initial words, there are only three content words, namely *faut* ‘(one) must,’ *regarde* ‘look,’ and *fais* ‘do.’

For each data point, the predicting observations $V_i = v_i$ are word forms chosen to represent the linguistic context and content of each prosodic phrase. These variables reflect our assumption that the child is especially sensitive to both function words and content words appearing near the boundaries of prosodic phrases. In a language like French, which was the language used for conducting this experiment, first words are mostly function words, while final words are mostly content words. To capture this, our learning model uses the two prosodic phrase edge-words as variables, dubbed $L_0$ for the first, “leftmost” word and $R_0$ for the final, “rightmost” word. Following preliminary experimentation with the model, we also included the second word of the phrase dubbed $L'_0$.\(^3\) Intuitively, this is important since the “true” function word of a phrase can appear in the second position as well, following a conjunction, as in: *mais le bébé* ‘but the baby,’ *que je sache* ‘that I know,’ etc. In order to model the immediately preceding context of the phrase, we also selected the first word of the preceding phrase, $L_{-1}$, as a variable. Hence, the set of predictor variables is $V = \{L_{-1}, L_0, L'_0, R_0\}$ (see Table 2 for an example).\(^4\)

Clearly, the independence hypothesis of the model is too strong. The predictor variables $V_i$, conditionally dependent on $C$, are not independent. However, common experience with the Naive Bayes model has shown that this strong independence assumption entails a computationally tractable framework without impeding its predictions. This is also the case for the current study.

### 2.2.2. Parameter Estimation

The purpose of the parameter estimation mechanism described in the following is to estimate the parameters of the probabilistic model—i.e., the prior probabilities $p(C = c)$ and the conditional probabilities $p(V_i = v_i \mid C = c)$ present in equation 2—in a case where some variables remain unobserved in the data (the class variable $C$ in our model). Here, we use the Naive Bayes Expectation Maximisation algorithm (NB-EM) as described by Pedersen (1998)\(^3\)

\(^3\)In the special case where a prosodic phrase contains only one word, we have $L_0 = R_0$ and $L'_0$ is void.

\(^4\)As mentioned previously, our choice of predictor variables has a built-in “leftward” bias, due to the fact that our model is designed to work with French child-directed speech. In the conclusions we discuss the plausibility of this bias and ways we can extend our model to be more “symmetric.”
algorithm, each data point is initially randomly assigned to a category (initialization step). Subsequently, the model parameters are calculated according to this assignment (maximization step). Using the newly calculated model parameters, the data points are reassigned to the various categories (expectation step). These two steps are iterated until the resulting likelihood of the data set ceases to increase. Note that the number $k$ of possible categories is chosen initially (as one of the hypotheses of the model) and does not change subsequently.

Once the parameters are estimated, the model can be used to predict the categories of each prosodic phrase in the corpus using the decision rule given in (2), so that each prosodic phrase is assigned to one of the $k$ classes.

### 2.2.3. Initial Clustering According to Frequent L-Words

Instead of using a random initialization phase as is typical with the NB-EM algorithm, each prosodic phrase is assigned initially to a category corresponding to its first word (the L-word), if and only if this word is part of the $k$ most frequent L-words appearing in prosodic phrases longer than one word (as one-word phrases cannot normally contain a function word). If this is not the case, the prosodic phrase is initially left unassigned (see Table 3 for examples). The subsequent maximization phase is based only on those data points that had initially been categorized. Then, the NB-EM algorithm proceeds normally.

### 2.2.4. Evaluation Measures

In order to evaluate the performance of our model, and compare it to a model whose parameters are estimated with a full random-initialization, we calculated for each resulting class (i.e., group of phrases whose predicted category is the same), its purity measure, which measures how well

<table>
<thead>
<tr>
<th>Phrase</th>
<th>Assigned category</th>
</tr>
</thead>
<tbody>
<tr>
<td>vas-y</td>
<td>‘go! (sg.)’</td>
</tr>
<tr>
<td>$tu$ vas apprendre</td>
<td>‘you (sg.) will learn’</td>
</tr>
<tr>
<td>$je$ vais prendre</td>
<td>‘I will take’</td>
</tr>
<tr>
<td>le bain</td>
<td>‘the bath’</td>
</tr>
<tr>
<td>au bébé</td>
<td>‘to the baby’</td>
</tr>
<tr>
<td>et le crocodile</td>
<td>‘and the crocodile’</td>
</tr>
</tbody>
</table>

Table 3: Examples of Prosodic Phrases with Their Initial Functional Category, When Initializing with the 10 Most Frequent Function Words ($tu$, $c'$, $et$, $il$, $on$, ça, je, qu', de, le).

$^5$The NB-EM algorithm is a standard parameter estimation algorithm that can potentially suffer from local minima. Nevertheless, our results were extremely stable, as evidenced for instance by the almost invisible error bars in Figure 1, even though each of the different subcorpora was rather small. This suggests that the behavior of the model itself is highly stable and would not change with a different procedure for estimating the model’s parameters.

$^6$The idea of creating initial classes that contain only one type of “head-word” is similar to the idea proposed by Parisien, Fazly & Stevenson (2008). However, in their algorithm, the head-word could be any word in the stream of words, while in our algorithm the “head-word” must be an L-word of a prosodic phrase.
this class captures a real syntactic category (as given by our rule-based parser). Following Strehl, Ghosh & Mooney (2000), we measure this by comparing the size of the class to the size of the largest syntactic category represented in it. Formally, this gives the following definition:

$$\text{purity} (\text{Cl}) = \max_i \frac{|\text{Cat}_i \cap \text{Cl}|}{|\text{Cl}|} = \frac{\text{Size of largest category}}{\text{Class size}}$$

(3)

A class that has an absolute majority of one phrasal category (purity $> \frac{1}{2}$) can be considered a reasonably good class. A good class will exhibit a purity above $\frac{2}{3}$.

The purity measures of all $k$ classes can be averaged in order to estimate the overall success of the algorithm.

As a further baseline of comparison, we use “chance purity,” which is the average purity that would result if we would distribute the prosodic phrases by chance in the $k$ classes. This should be equal to the proportion of the largest phrasal category, which happens to be the VN category with a proportion of approximately 37%.

2.2.5. Precision and Recall of Best Classes

As explained previously, we are particularly interested in the labelling of prosodic phrases that correspond to the VN and NP categories. In the current experiment, we have no classes that correspond uniquely to these labels, but for comparison purposes with other approaches (as well as with Experiment 2) we can a posteriori select the class with the highest (“best”) proportion of VNs, and the class with the highest proportion of NPs, and label them as such. For those classes we can calculate the standard recall and precision measures, which are defined as follows:

$$\text{precision} = \frac{\text{Number of hits}}{\text{Class size}}$$

(4)

$$\text{recall} = \frac{\text{Number of hits}}{\text{Category size}}$$

(5)

The term hit in this context should be understood as a VN prosodic phrase in the best VN class, or alternatively an NP prosodic phrase in the best NP class.

Since we select the classes with the highest proportion of these prosodic phrases, our precision measure should be high. By contrast, since we look only at one class for each category (out of our $k$ classes), the recall measure will be very low, because each category (NP and VN) is spread out over many classes.

As a baseline, we can compare these measures to a chance distribution of the prosodic phrases into $k$ clusters, which yields precision levels equal to the relative NP or VN proportions in the corpus, and recall levels that equal $1/k$.

---

7We have also used a more fine-grained measure, namely the “pair-wise precision” measure, which measures the probability of selecting by chance a pair of phrases with the same category in a given class, or formally: $\text{PWP (Cl)} = \sum_i \left( \frac{|\text{Cat}_i \cap \text{Cl}|}{|\text{Cl}|} \right)^2$. This measure is called “precision” (Hatzivassiloglou & McKeown 1993) or “accuracy” (Chemla et al. 2009). The two measures, purity and PWP, are closely correlated. In our data, a purity measure of $\frac{2}{3}$ PWP measure of $\frac{1}{2}$, which indicates that the probability of two randomly selected phrases belonging to the same category is $\frac{1}{2}$. 
2.3. Results

The average purity measure over the 10 subcorpora as a function of the number of classes is given in Figure 1.

In general, we expect the average purity to grow with the number of classes (Strehl, Ghosh & Mooney 2000). This expectation is indeed borne out for the random-initialization model. By contrast, this is not the case for the function-word initialization model. Purity reaches a fixed level (about 0.65) with 10–30 classes and does not increase with the addition of more classes. While the random-initialization model shows a continuous increase in purity as a function of the number of classes, it remains substantially lower than the purity of the function-word initialization model for any number of classes. Both models show a clear advantage over the chance baseline.

Importantly, the performance of our model decreases substantially when there are fewer than 10 classes. Using only 5 classes is insufficient—this is intuitively understandable given that none of the five most frequent L-words is a determiner (*tu, c’, et, il, on/ça*, with the last L-word varying

![Figure 1](image-url)
between the different subcorpora). Indeed, the most common determiners (de, le, un depending on the subcorpus) are ranked in positions 9–11 among the L-words.

Exploring the precision values of the best VN and NP classes (as defined in section 2.2.5) leads to similar conclusions. These values, together with the corresponding recall values, are presented in Figure 2. For both the VN category and the NP category, we see that the function-word initialization model substantially outperforms the random-initialization model in constructing precise VN or NP classes. As expected, recall is generally low and decreases with the number of classes. Both the random-initialization model and function-word initialization model outperform chance-level baseline in all measures. For recall only, the random-initialization model does slightly better than the function-word initialization model.

We can conclude that the L-word initialization is highly beneficial even when considering a relatively low number of function words. Strikingly, purity and precision levels are consistently high across the whole spectrum. This holds despite the fact that the 10 most frequent function words only initially classify approximately 33% of the corpus, while the 70 most frequent L-words initially classify 70% of the corpus. This increase hardly has any effect on the average purity of the model (as illustrated in Figure 1) or on the best-classes precision levels.
2.3.1. 10 Classes

We further analyzed the behavior of the model with 10 classes, the smallest number of classes that yielded good results for both VNs and NPs.

The results of the 10-class model on the entire corpus (rather than on a subcorpus, as previously) are presented in Figure 3. Table 4 gives the purity measure of the output classes, sorted by descending purity. The name of each class indicates the initial L-word from which it was created, while the growth column provides the ratio between the final and the initial class sizes (in other words, it provides an indication of how many phrases were added to the class in the EM learning process).

The results show that five classes have an excellent purity measure, above 0.75, and that an additional two classes have good purity of 0.63–0.65. All these classes are good predictors of the NP or VN phrasal categories (see Figure 3). While the remaining three classes do not serve as predictors for these classes, they may still reveal some structure. For instance, the ‘ça’ ‘that’ class captures 94% of all interjection phrases. The random initialization model, on the other hand, provides on average only 2.2 ± 0.25 classes of purity larger than 0.60 (range: 1–3 in our test).

An interesting observation about the good classes is the negative correlation between the growth rate and the purity measures. Considering the five best classes together, we see that the higher the purity measure, the lower the growth level. The verbal classes ‘tu’, ‘on’, and ‘je’ in particular tend to have a very high purity rate (85% and above) and a relatively low growth rate. In other words, these classes are initially very good (i.e., the L-word initialization provides homogeneous

![Figure 3](image-url) FIGURE 3 Results of the model with 10 classes. Every vertical bar represents a class, and the colored regions describe the proportions of the different phrasal categories in each class. Note in particular the topmost regions, which correspond respectively to VNs and NPs (the other categories are VPpart = Participal Verbal Phrases, P.N = Proper Nouns, AdvP = Adverbial Phrases, AdjP = Adjective Phrases, Inter. = Interjections, Func. = Functional words appearing alone). The labels in lower case correspond to the class name, while the labels in capitals are manually marked and signal classes with high purity values as well as their majority category (VN or NP): Thus, the classes labeled by the determiners ‘le’ and ‘de’ predict NPs while those labeled by pronouns (‘tu’, ‘on’, ‘je’, ‘il’) as well as the relativizer ‘qu’ predict VNs.
classes), but the algorithm succeeds only mildly in generalizing them to more data points (in contrast to the nominal classes). This corroborates the hypothesis that relying on function words is highly informative for the classification process.

2.4. Discussion

The present model tested the hypothesis that the edge-words of a prosodic phrase provide useful information regarding the category of that phrase. The model was initialized with a limited number of classes that contained all prosodic phrases starting with a certain left-most word. The number of classes was varied parametrically from 5 to 70: the $k$ most frequent left-most words were selected to build $k$ classes. When the model contained 10 classes, all these words were function words, and the model exhibited a good average purity, of approximately 0.65, much higher than that of a model starting with random classes. Hence, relying on frequent words appearing at the left edges of prosodic phrases provided the model with useful information to categorize these phrases.

However, despite the quality of the classes produced by this method, it establishes classes based on single function words rather than generalized grammatical classes, such as VN or NP. As a result, VNs and NPs are distributed over several classes. A similar problem was identified in several distributional word-categorization approaches (Mintz 2003; Chemla et al. 2009), and no straightforward way to merge classes post-hoc could be identified (but see Parisien, Fazly & Stevenson 2008). To overcome this problem, we chose to initialize the model with semantically based classes.

8 The remarkably low growth rate of the *tu* class, only 9%, can likely be attributed to the use of an orthographically transcribed corpus, as second person singular French present tense verb forms are written differently from other present tense singular verbal forms, thus making it difficult for the learning algorithm to generalize over orthographically different (but phonetically identical) verbal forms, such as *(tu) manges ‘(you) eat’ and *(je) mange ‘(I) eat.’

## Table 4

<table>
<thead>
<tr>
<th>Class</th>
<th>Purity</th>
<th>Growth</th>
</tr>
</thead>
<tbody>
<tr>
<td>on</td>
<td>0.89</td>
<td>1.76</td>
</tr>
<tr>
<td>tu</td>
<td>0.88</td>
<td>1.09</td>
</tr>
<tr>
<td>je</td>
<td>0.86</td>
<td>2.07</td>
</tr>
<tr>
<td>le</td>
<td>0.76</td>
<td>4.86</td>
</tr>
<tr>
<td>de</td>
<td>0.76</td>
<td>6.50</td>
</tr>
<tr>
<td>il</td>
<td>0.65</td>
<td>2.31</td>
</tr>
<tr>
<td>qu’</td>
<td>0.63</td>
<td>2.77</td>
</tr>
<tr>
<td>c’</td>
<td>0.49</td>
<td>1.09</td>
</tr>
<tr>
<td>ça</td>
<td>0.43</td>
<td>8.72</td>
</tr>
<tr>
<td>et</td>
<td>0.38</td>
<td>4.58</td>
</tr>
</tbody>
</table>

Avg. Purity 0.67
Rand. Avg. Purity 0.50 ± 0.01

Note. For comparison the average purity measure is also given for the random initialization model, run 10 times.
3. EXPERIMENT 2

In the second experiment, we incorporate the possibility that early on, the child manages to learn the meaning of a few frequent nouns and verbs. These words often refer to concrete objects and agentive actions and can thus constitute a seed for the prototypical “noun” and “verb” grammatical categories. For example, if the child knows the words *voiture* ‘car’ and *jouet* ‘toy,’ she would be able to associate the two prosodic phrases *la voiture* ‘the car’ and *le jouet* ‘the toy’ to the same phrasal category related to physical objects, which we call NP. The idea that children group together words referring to physical objects on the one hand and words referring to actions on the other hand on the basis of semantics is in line with experimental data showing that children have a separate representation for agents and artifacts (for a review, see Carey 2009) and for causal actions (Saxe & Carey 2006). Indeed, such words are plausible candidates to be among the first words learned by a child.\(^9\)

To model this initial semantic knowledge, we provide our clustering algorithm with a **semantic seed**, i.e., a short list of known words, which are explicitly associated with the VN and NP categories.

3.1. Material

We used the same input corpus, tagged with prosodic phrase information, as in Experiment 1. Additionally, a limited prior word knowledge, the semantic seed, is fed into our clustering algorithm. The size of the semantic seed is varied parametrically in order to observe how the size of the vocabulary can influence categorization. Following Brusini et al. (2011), we defined five semantic seeds ranging from a very small set of 6 nouns and 2 verbs (6N, 2V) to a larger set of 96 nouns and 32 verbs (96N, 32V). The \(n\) words chosen for the semantic seed correspond to the \(n\) most frequent nouns and verbs in the corpus.\(^{10}\) For example, the smallest semantic seed (6N, 2V) contains the 6 most frequent nouns in the corpus, *doudou* ‘stuffed toy,’ *bébé* ‘baby,’ *livre* ‘book,’ *chose* ‘thing,’ *micro* ‘microphone,’ *histoire* ‘story,’ and the 2 most frequent verbs, *aller* ‘go’ and *faire* ‘do.’

3.2. Method

As in Experiment 1, we used the Expectation-Maximization algorithm, with a modified initialization stage.

During initialization, the final word (or R-word) of each phrase was examined; if it was one of the known words from the semantic seed, the phrase was assigned to the V (Verbal) or N (Nominal) classes (according to the category of the known word). The remaining phrases were assigned to the U (Unknown) class (see Table 5 for examples). The first maximization

\(^9\)The idea that semantic classes can serve as a basis for syntactic classes is not new. Pinker (1984, 1989) proposed the **semantic bootstrapping hypothesis** in which children are hypothesized to group words into universal meaning categories, such as agent, patient, transitive verb, and so on. In his account, they would furthermore use innate linking rules to map such semantic categories onto the corresponding syntactic categories.

\(^{10}\)In order to construct the semantic seed, the full corpus was taken into consideration, including the one-word utterances that were excluded from the actual modeling.
phase was then conducted on the N and V phrases together with a similarly sized random sample of U phrases (so that the prior probability of the U class would be similar to those of the N and V classes). The remainder of the EM algorithm proceeded as before. Note that under this initialization condition there is no flexibility regarding the number of classes: There are exactly three (N, V, or U). The percentage of phrases that were assigned to the N or V classes in the initialization phrase for each semantic seed level ranged between 4.5% (6N, 2V) to 23% (96N, 32V).

As in Experiment 1, the learning algorithm relies on the variables $L_{-1}$, $L_0$, $L'_0$, and $R_0$ (see Table 2).

### 3.2.1. Evaluation Measures

Ideally, the resulting N and V classes should correspond to the NP and VN syntactic categories respectively. Thus, we can easily calculate their precision and recall levels, as defined in equations 4 and 5 (see section 2.2.5).

As we have five levels of semantic seed used in the method, we can compare these measures across various levels of initial knowledge. Moreover, the results are compared to two baselines: First, we compare them to a uniform random clustering into three classes. Such classes will, by definition, have a recall level of $1/3$, and a precision level equivalent to the relative proportion of NPs and VNs in the corpus. These are the “chance” results. Second, we compare the results to a “zero-knowledge” model, which is modeled by running the random initialization EM with three classes, which are a posteriori labeled as N or V classes in order to obtain maximal precision measures (specifically, among the classes with a majority of VNs, we take the one with the highest VN purity as the V cluster, and subsequently we take the class with the highest NP purity as the N cluster).

As in Experiment 1, we divided our corpus into 10 subcorpora to estimate the variability of our results across different runs.

### 3.2.2. Discriminatory Power

To investigate which variables are the most important ones in the learning process, we used a measure called “discriminatory power.” For a given data point with its predicted category, we
can calculate the additional contribution a variable adds to the likelihood in comparison to its average contribution when predicting other categories. When we average this measure over all data points, we get the discriminatory power. Formally, it can be computed as follows ($i$ runs over the $n$ data points, while $j$ runs over the $k$ classes):

$$
\text{disc}(F) = \frac{1}{n} \sum_{i=1}^{n} \frac{1}{k} \sum_{j=1}^{k} \log p(F = f_i, \phi = \text{Cl}_{\text{best}}) - \log p(F = f_i, \phi = \text{Cl}_j) \tag{6}
$$

A higher measure indicates a higher contribution of a variable. While we expect all variable measures to be positive, the absolute discriminatory value of a variable is not interpretable. We are rather interested in the relative magnitudes of these values.

3.3. Results

Figure 4 presents the precision measures as a function of the different sizes of the semantic seed, compared to the random baselines. Precision is very high, between 75% and 85%, and varies very little with the size of the semantic seed.

Figure 5 presents the recall measure for each semantic seed level. Again, recall is much higher compared to the baseline recalls and relatively stable across the variation in semantic seed size.

![FIGURE 4](image-url) Precision as function of the semantic seed level, given as the number of known nouns (N) and verbs (V). The lower lines represent the chance baselines (related to the proportion of NPs and VNs in the corpus). The standard error is less than 0.01 for all conditions except for 0N,0V.
The high precision levels are further illustrated in Figure 6, which presents the content of the classes obtained using the smallest seed. Considering that the smallest seed permits an initial classification of only about 4.5% of the prosodic phrases of the corpus, the final classes capture the verbal and nominal phrases extremely well, while other phrasal categories fall mainly in the U class. Using a larger semantic seed results in a similar picture.

Although the semantic seed model is based on an initial clustering according to content words (R-words), the classification process ultimately relies on the function words (L-words). Indeed, as Figure 7 shows, the most prominent variables for the classification are \( L_0 \) and \( L'_0 \). Note that while the \( R_0 \) variable becomes somewhat more prominent with the larger seeds (reflecting the larger initial semantic knowledge), it is still less important than the phrasal L-words. Not surprisingly, the \( L_{-1} \) variable, which represents the previous phrase’s L-word, contributes least to the classification, in part because this variable is empty (thus not truly informative) whenever the first prosodic phrase of an utterance is considered. We can conclude that even though the model starts its classification on the basis of examining content words given in a semantic seed, it “learns” that a good classification should instead be based on the examination of function words. In other words, ultimately relying on function words leads to a more accurate classification of prosodic phrases.

Further support for this claim arises from examining how the model fares with one-word prosodic phrases, which for the large part consist only of a content word (such as an interjection or an imperative verb). For these phrases the results are far from satisfactory: Using the largest semantic seed, for example, the precision levels for these phrases are only of 46% (N) and

![FIGURE 5](image-url)

**FIGURE 5** Recall as a function of the semantic seed size (given as number of known nouns and verbs). The lower line represents the chance baseline. The standard error is at most 0.012 for all conditions except for 0N,0V.
50% (V), with recall levels as low as 6% (N) and 37% (V). By contrast, for phrases with at least two words, which normally contain a function word, the precision levels are 79% (N) and 86% (V) with a recall level of 62% and 69% respectively. Clearly, phrases containing more than one word are easier to classify correctly, and these phrases often contain a function word.
Looking closer at the performance on phrases of at least two words, we observe that the length of prosodic phrases differentially affects the quality of the N and V classes. The N class fares best with phrases of exactly two words—typically consisting of a determiner + noun—and captures longer nominal phrases less well. For example, the precision level of nominal phrases of at least five words is only 46% with 34% recall. This aligns with the predominant pattern of nominal phrases containing only two words. These short phrases appear to be beneficial for NP classification. By contrast, the V class is quite indifferent to phrasal length. For instance, verbal phrases of at least five words achieve an excellent precision level of 78% with recall of 72%. The word-length distribution for V phrases is also more spread out (with comparable results for any multiword phrases regardless of exact length). In other words, verbal phrases tend to have a larger scope than nominal phrases, and the model copes well with all these lengths.

3.4. Discussion

Initializing a model with semantically based classes allows it to categorize initially unclassified prosodic phrases with an excellent precision. In addition, the performance of the model remains remarkably stable with increases in the size of the semantic seed. This rather counterintuitive result suggests that having a large vocabulary is not necessary to initialize the categorization process: Even a very small semantic seed (six nouns and two verbs) is sufficient. By assuming that the language learner can ground these semantically based classes in her extralinguistic experience—e.g., nouns typically refer to objects, and verbs to actions—we provide a plausible means of initializing syntactic categorization. In addition, the high contribution of the leftmost words of the prosodic phrases to the categorization confirms the hypothesis that function words play a central role in the classification process.

4. CONCLUSIONS

In this article, we presented two models that tested the role of phrasal prosody and edge-words in the identification and classification of prosodic phrases. Both models successfully assigned syntactic labels to prosodic phrases, relying on phrasal prosody to delimit phrases, and their edge-words to classify them. The two models differed only in the way classes are initially defined. The first model started out with a limited number of classes, each class being initially defined as containing all prosodic phrases starting with the same initial word. The model exhibited a good average purity level, much higher than a model starting with random classes. Thus, this model shows that relying on a small number of frequent function words is sufficient to create meaningful syntactic classes. A closer look at the behavior of individual classes revealed that the model built a number of good VN and NP classes, as well as some classes that contained a mixture of categories. Thus, while this model confirms the intuition that paying attention to the leftmost words of prosodic phrases is a good start for classifying them, it has the property that several different classes are constructed for each syntactic category.

To overcome this issue, the second model incorporated an additional piece of information, a semantic seed, that allowed the model to start with exactly three categories, one containing noun phrases, one containing verb phrases (or parts of verb phrases, corresponding to VNs), and the third one containing phrases of different categories. The size of the semantic seed was varied.
parametrically, from an extremely reduced semantic seed, consisting of only 6 known nouns and 2 known verbs, to a larger but still realistic one (96 nouns and 32 verbs). The results show that such an approach is highly successful: With as little initial knowledge as 4.5% of the phrases of the corpus, the algorithm manages to construct highly precise VN and NP classes, containing over 50% of the prosodic phrases in these categories. This excellent performance reveals two important features of our model. First, relying on the knowledge of a few frequent content words is sufficient for the emergence of abstract syntactic categories. Since these abstract categories (i.e., the VN and the NP) are grounded in semantic experience (some of these words represent actions and some represent objects), no innate knowledge of the syntactic categories is a priori needed. Second, although the initial classes are based on content words from the semantic seed, the learning process relies ultimately on function words: The discriminatory power analysis showed that the most efficient variables are the left-most words—$L_0$ and $L'_0$—which often correspond to function words. This can happen, since newly classified data points contribute to the learning of more structure. In other words, the knowledge of a few content words may allow the language learner to discover the role of function words.

This important role of function words is consistent with the infant literature. A number of experiments have shown that infants are sensitive to the function words of their language within their first year of life (Hallé, Durand & Boysson-Bardies 2008; Shafer et al. 1998; Shi et al. 2006). In addition, 15- to 18-month-old children exploit function words to constrain lexical access to known words—for instance, they expect a noun after a determiner (Cauvet et al. 2014; Heugten & Johnson 2011; Kedar, Casasola & Lust 2006; Zangl & Fernald 2007). Crucially, when hearing unknown words, children of this age are able to infer the acceptable contexts for these unknown words. For instance, after hearing the *blick*, they would consider that a *blick* is possible but not *I blick* (for French: Shi & Melançon 2010; for German: Höhle et al. 2004). The present models provide a way in which infants can not only gather such information but also use it in order to label prosodic phrases.

Our models rest on three assumptions. First, the language learner must have access to the boundaries of intermediate prosodic phrases. As we saw in the introduction, this hypothesis seems plausible, given a wealth of experimental data showing that by the end of the first year of life, infants are not only sensitive to prosodic boundaries, but are also able to exploit them to constrain lexical access (Gout, Christophe & Morgan 2004). Second, the models rest on the assumption that words placed at the edges play an important role: the left- and rightmost words of a phrase are given special status. This assumption received experimental support from several studies: Words at edges are more salient, hence easier to segment from continuous speech (Cutler 1993; Endress & Mehler 2009; Johnson, Seidl & Tyler 2014; Seidl & Johnson 2006; Shi, Morgan & Allopenna 1998). Third, we assume that children manage to learn and group together a few frequent and concrete nouns and verbs. This, too, is a plausible assumption, given recent findings that show that infants know at least some nouns at 6 months (Bergelson & Swingley 2012; Tincoff & Jusczyk 2012) and possibly even some verbs at 10 months (the “abstract words” of Bergelson & Swingley 2013).

This final assumption does, however, warrant a note of caution. While we simplistically assume that children create two broad semantic categories of physical entities (corresponding to nouns) and actions (corresponding to verbs), several studies have suggested that infants represent distinct types of physical entities differently, for instance agents versus artifacts (see e.g., Carey 2009), or human versus nonhumans (Bonatti et al. 2002). It is thus quite possible that children
may initially have more than two categories and could hence distinguish between phrases referring to agents and phrases referring to artifacts (in addition to those referring to actions). For example, the nouns in our smallest semantic seed could represent (at least) two distinct categories of entities: agents (i.e., bébé ‘baby’) and artifacts (livre ‘book,’ chose ‘thing,’ micro ‘microphone’). While more research is needed to better understand the early conceptual representations, our model suggests that the acquisition of syntax could be responsible for the merging of these separated classes by observing that agents and artifacts can (to a certain extent) occur in the same distributional environment.¹¹

As for the second assumption, note that our models are currently built with a right-left asymmetry. In the first model, the most frequent leftmost words are used to initially classify phrases, while in the second model the known rightmost words are used for this initial categorization. This assumption is plausible, since several lines of experimental research suggest that infants know that frequent functional items typically occur either at the left or right edges of phrases, depending on the language (Bernard & Gervain 2012; Gervain & Werker 2013; Gervain et al. 2008; Hochmann 2013; Hochmann, Endress & Mehler 2010). However, this assumption is not crucial for the models: The first model could very well start with a symmetrical search of frequent items at both edges, while the second model could search the known content words at both edges. The model does not need to know in advance where content and function words typically occur. We would, however, need to make our variable set symmetrical, by adding, for example, an $R_0$ variable to equate it with $L_0$.

If the language learner has access to an approximate shallow syntactic structure consisting of labeled prosodic phrases, this can help her in two important ways. First, it may allow her to gain some insight into the syntactic structure of the language. This in turn may serve as an intermediate step toward a full understanding of its syntax. Second, this syntactic skeleton may enable the child to infer the meaning of unknown content words. The syntactic bootstrapping hypothesis proposes that syntactic structure provides additional constraints to the word learning inference problem (Gleitman 1990).

Thus, language learners trying to figure out the meaning of a novel word, such as blick, perform better when they have access to the syntactic structure of the sentence. For instance, upon hearing a sentence such as he blicks that the dog is angry, listeners can infer that blick refers to a thought or communication verb (verbs that can take a whole proposition as complement; Gillette et al. 1998). Likewise, toddlers use sentence structure to predict that a verb used in a transitive sentence has a causative meaning (Naigles 1990; Yuan & Fisher 2009). The language learner could also directly exploit the label of a prosodic phrase to constrain the meaning of some of its content words; for instance, a prosodic phrase labeled as a noun phrase should normally contain a noun (referring to an object), while a verbal nucleus should contain a verb (referring to an action). This may help the child learn the meaning of new words more easily.

Finally, our model illustrates the role of synergies in language acquisition. Knowledge of some lexical items (such as the semantic seed) permits the inference of syntactic categories, through the use of prosodic phrases and function words. Subsequently, knowledge of some syntactic categories enables the learner to enrich her vocabulary, which will further expand the child’s

¹¹We thank an anonymous reviewer for this interesting suggestion.
syntactic knowledge. As such, our computational model provides a formalization of the insights gained from the psycholinguistic literature to explain the mechanisms underlying early syntactic acquisition.

ACKNOWLEDGMENTS

This work originated in the first author’s master thesis of the Master Parisien de Recherche en Informatique. We thank all colleagues who attended our talks on the subject, as well as Marieke van Heugten, Mark Johnson, Sonia Gharbi, Inka Keller (Leidig), Amy Perfors, Frans Plank, Valerie Shafer, and two anonymous reviewers for their suggestions and help.

FUNDING

The first author is grateful for the École Normale Superieure for providing him the scholarship enabling him to pursue this research. The research was furthermore supported by the French Ministry of Research, the French Agence Nationale de la Recherche (grant numbers ANR-2010-BLAN-1901, ANR-13-APPR-0012, ANR-10-IDEX-0001-02 PSL*, ANR-10-LABX-0087 IEC, and ANR-10-LABX-0083 EFL), the Fondation de France, the DGA (doctoral grant to ID), as well as the Région Île-de-France.

REFERENCES


Ngon, Céline, Andrew Martin, Emmanuel Dupoux, Dominique Cabrol, Michel Dutat & Sharon Peperkamp. 2013. (Non)words, (non)words, (non)words: Evidence for a protolexicon during the first year of life. Developmental Science 16(1). 24–34.


