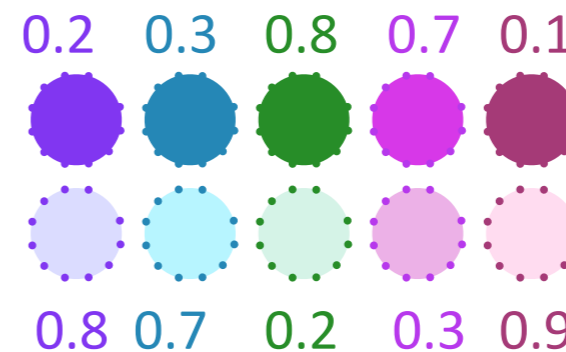
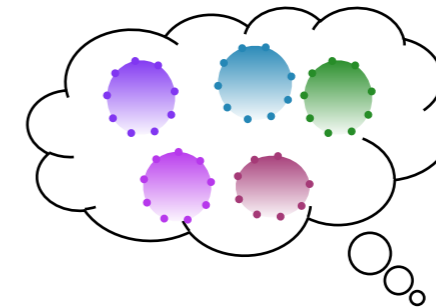
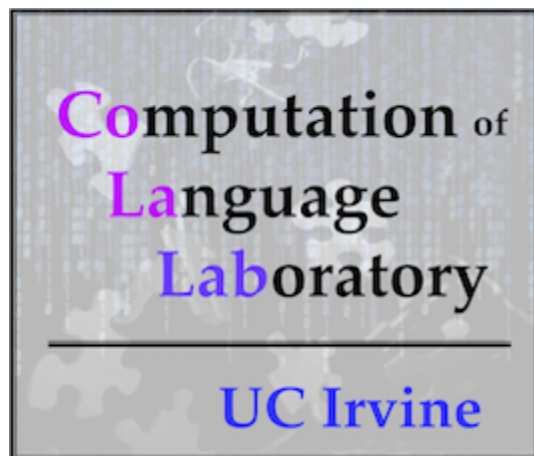


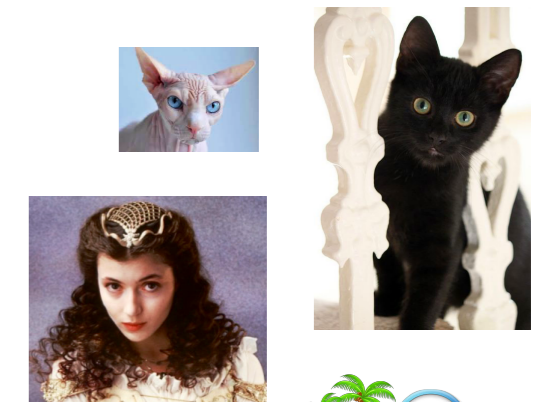
# Computational models of syntactic acquisition

Lisa Pearl

University of California, Irvine



*another one*



*Who does... is pretty?*

August 4, 2017:

Norwegian Summer Institute on Language & Mind

University of Oslo

# Today's Plan:

## Computational models of syntactic acquisition

### I. Some non-parametric examples

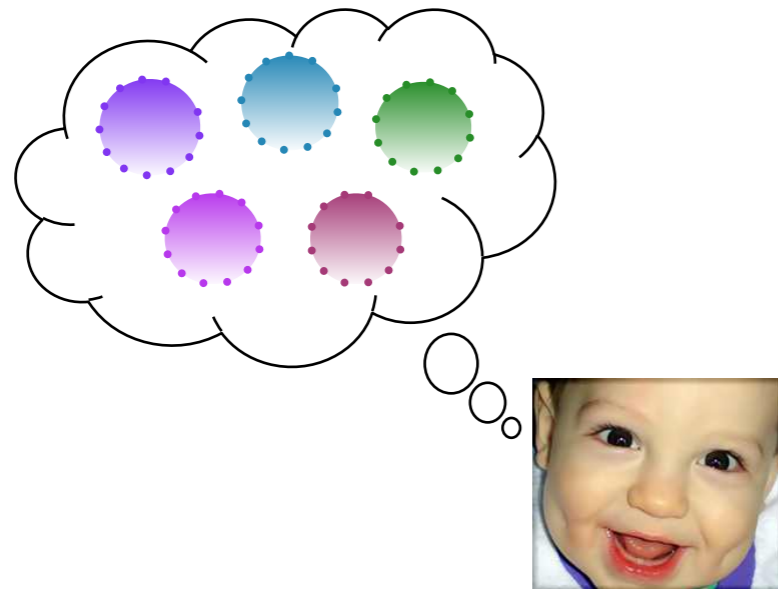
Who does  ...  is pretty?

**syntax** 

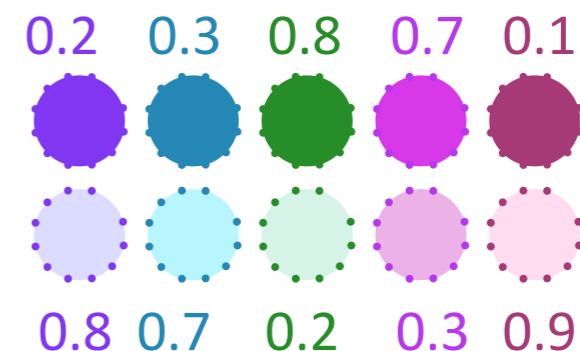
*another one*   

**syntax, semantics**

### II. About linguistic parameters



### III. Learning with parameters



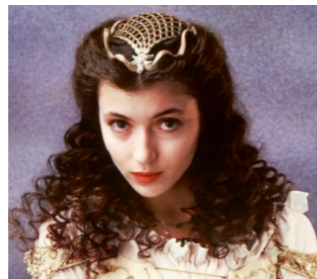
# Today's Plan:

## Computational models of syntactic acquisition

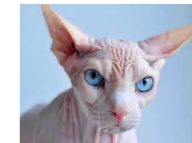
### I. Some non-parametric examples

Who does  ...  is pretty?

syntax



another one



syntax, semantics

# Some non-parametric examples syntax

*This kitty was bought as a present for someone.*

*Lily thinks this kitty is pretty.*



**What's going on here?**

*Who does Lily think the kitty for is pretty?*



*What does Lily think is pretty, and who does she think it's for?*



# Some non-parametric examples syntax

Who does 

Lily think the kitty for is pretty?



What's going on here?

There's a **dependency** between the *wh*-word *who* and where it's understood (**the gap**)

*Who does Lily think the kitty for \_\_\_ is pretty?*



This dependency is **not allowed** in English.

One explanation: The dependency crosses a “syntactic island” (Ross 1967)



# Some non-parametric examples syntax

Who does 

*Lily think the kitty for is pretty?*



What's going on here?  syntactic island (Ross 1967)

*Who does Lily think the kitty for \_\_\_ is pretty?*



*Jack is somewhat tricky.*

*He claimed he bought something.*

*What did Jack make the claim that he bought \_\_\_?*



# Some non-parametric examples syntax

Who does 

*Lily think the kitty for is pretty?*



What's going on here?  syntactic island (Ross 1967)

*Who does Lily think the kitty for \_\_\_ is pretty?*

*What did Jack make the claim that he bought \_\_\_ ?*



*Jack is somewhat tricky.*

*He claimed he bought something.*

*Elizabeth wondered if he actually did and what it was.*

*What did Elizabeth wonder whether Jack bought \_\_\_ ?*



# Some non-parametric examples syntax

Who does 

Lily think the kitty for is pretty?



What's going on here?  syntactic island (Ross 1967)

Who does Lily think the kitty for \_\_\_ is pretty?

What did Jack make the claim that he bought \_\_\_ ?

What did Elizabeth wonder whether Jack bought \_\_\_ ?



*Jack is somewhat tricky.*

*He claimed he bought something.*

*Elizabeth worried it was something dangerous.*

What did Elizabeth worry if Jack bought \_\_\_ ?





# Some non-parametric examples syntax

Who does 

Lily think the kitty for is pretty?



What's going on here?  syntactic island (Ross 1967)

Who does Lily think the kitty for \_\_\_ is pretty?

What did Jack make the claim that he bought \_\_\_ ?

What did Elizabeth wonder whether Jack bought \_\_\_ ?

What did Elizabeth worry if Jack bought \_\_\_ ?



Jack bought something.

Elizabeth met him afterwards.


What did you meet the pirate who bought \_\_\_ ?



Lily asks Elizabeth about it.



# Some non-parametric examples syntax

Who does   
Lily think the kitty for is pretty?



What's going on here?  syntactic island

*Who does Lily think the kitty for \_\_\_ is pretty?*

*What did Jack make the claim that he bought \_\_\_ ?*

*What did Elizabeth wonder whether Jack bought \_\_\_ ?*

*What did Elizabeth worry if Jack bought \_\_\_ ?*

*What did you meet the pirate who bought \_\_\_ ?*



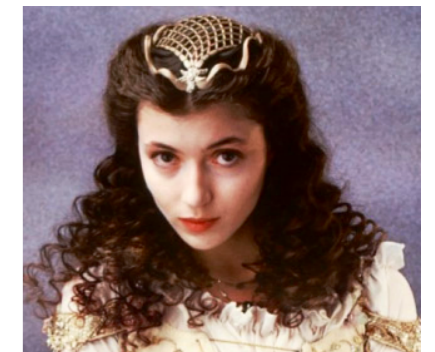
*Jack bought something.*

*Elizabeth was surprised by it.*




*Lily asks Elizabeth about it.*

*What did that Jack bought \_\_\_ surprise you ?*



# Some non-parametric examples syntax

Who does   
Lily think the kitty for is pretty?



What's going on here?  syntactic island

Who does Lily think the kitty for \_\_\_ is pretty?

What did Jack make the claim that he bought \_\_\_ ?

What did Elizabeth wonder whether Jack bought \_\_\_ ?

What did Elizabeth worry if Jack bought \_\_\_ ?

What did you meet the pirate who bought \_\_\_ ?

What did that Jack bought \_\_\_ surprise you ?



Jack bought two things - a kitty  
and something else.

What did you buy a kitty and \_\_\_ ?



Elizabeth wants to know about  
the other thing.

# Some non-parametric examples syntax

Who does 

Lily think the kitty for is pretty?



What's going on here?  syntactic island

Who does Lily think the kitty for \_\_\_ is pretty?

What did Jack make the claim that he bought \_\_\_ ?

What did Elizabeth wonder whether Jack bought \_\_\_ ?

What did Elizabeth worry if Jack bought \_\_\_ ?

What did you meet the pirate who bought \_\_\_ ?

What did that Jack bought \_\_\_ surprise you ?

What did you buy a kitty and \_\_\_ ?

Which did you buy \_\_\_ kitty?



Jack bought a specific kind of kitty.



Elizabeth wants to know about the kind.

# Some non-parametric examples syntax

Who does 

Lily think the kitty for is pretty?



What's going on here?  syntactic island

*Who does Lily think the kitty for \_\_\_ is pretty?*

*What did Jack make the claim that he bought \_\_\_ ?*

*What did Elizabeth wonder whether Jack bought \_\_\_ ?*

*What did Elizabeth worry if Jack bought \_\_\_ ?*

*What did you meet the pirate who bought \_\_\_ ?*

*What did that Jack bought \_\_\_ surprise you ?*

*What did you buy a kitty and \_\_\_ ?*

*Which did you buy \_\_\_ kitty ?*

**Important: It's not about the length of the dependency.**

(Chomsky 1965, Ross 1967)

# Some non-parametric examples syntax

Who does 

Lily think the kitty for is pretty?



What's going on here?  syntactic island

Who does Lily think the kitty for \_\_\_ is pretty?

What did Jack make the claim that he bought

What did Elizabeth wonder whether Jack bought

What did Elizabeth worry if Jack bought \_\_\_

What did you meet the pirate who bought

What did that Jack bought \_\_\_ surprise you

What did you buy a kitty and \_\_\_ ?

Which did you buy \_\_\_ kitty ?

Elizabeth



What did Elizabeth think \_\_\_ ?



**It's not about the length  
of the dependency.**

# Some non-parametric examples syntax

Who does 

Lily think the kitty for is pretty?



What's going on here?  syntactic island

Who does Lily think the kitty for \_\_\_ is pretty?

What did Jack make the claim that he bought \_\_\_ ?

What did Elizabeth wonder whether Jack bought \_\_\_

What did Elizabeth worry if Jack bought \_\_\_ ?

What did you meet the pirate who bought \_\_\_?

What did that Jack bought \_\_\_ surprise you? ?

What did you buy a kitty and \_\_\_ ?

Which did you buy \_\_\_ kitty ?

Jack



Elizabeth



What did Elizabeth think Jack said \_\_\_ ?



**It's not about the length  
of the dependency.**

# Some non-parametric examples syntax

Who does 

Lily think the kitty for is pretty?



What's going on here?  syntactic island

Who does Lily think the kitty for \_\_\_ is pretty?

What did Jack make the claim that he bought \_\_\_ ?

What did Elizabeth wonder whether Jack bought \_\_\_

What did Elizabeth worry if Jack bought \_\_\_ ?

What did you meet the pirate who bought \_\_\_?

What did that Jack bought \_\_\_ surprise you?

What did you buy a kitty and \_\_\_ ?

Which did you buy \_\_\_ kitty ?

Jack



Elizabeth



Lily

What did Elizabeth think Jack said Lily saw \_\_\_ ?



**It's not about the length of the dependency.**



# Some non-parametric examples syntax

Who does 

Lily think the kitty for is pretty?

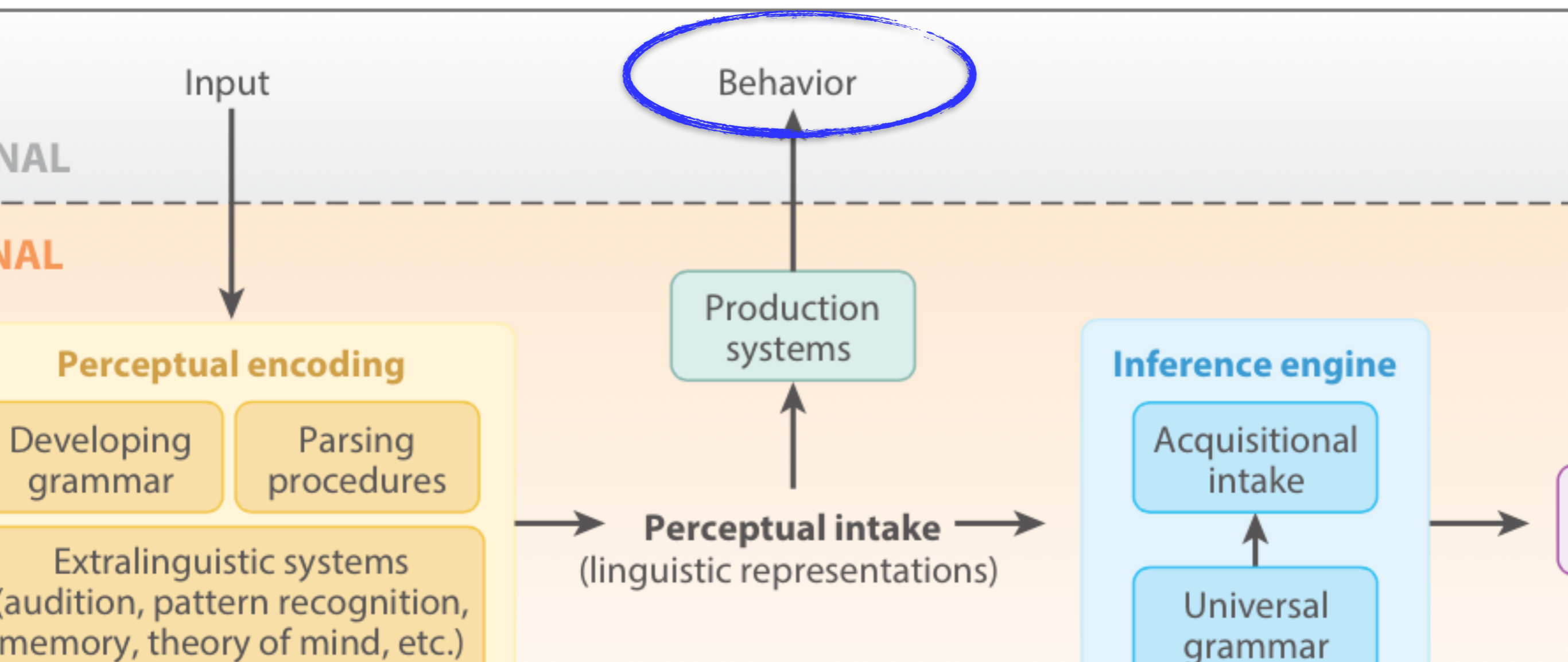


syntactic island

Who does Lily think the kitty for \_\_\_ is pretty?



Adults **judge** these dependencies to be far worse than many others, including others that are very similar except that they don't cross syntactic islands (Sprouse et al. 2012).



# Adult judgments: Target behavior



syntax

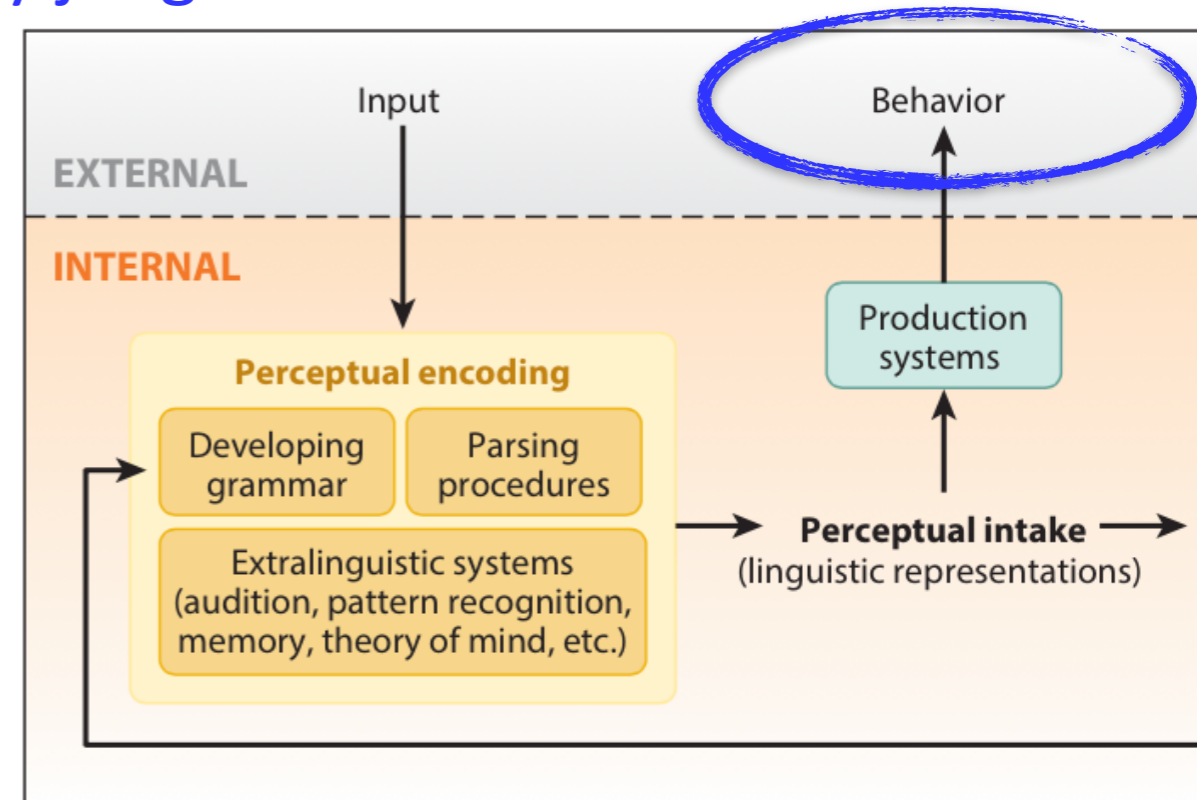


syntactic island

Adult knowledge as measured by **acceptability judgment** behavior

Sprouse et al. (2012) collected magnitude estimation judgments for four different islands, using a factorial definition that controlled for two salient properties of island-crossing dependencies:

- **length** of dependency (**matrix vs. embedded**)
- presence of an **island** structure (**non-island vs. island**)



Lidz & Gagliardi 2015

# Adult judgments: Target behavior



syntax



syntactic island

Adult knowledge as measured by **acceptability judgment** behavior

*Sprouse et al. (2012)*

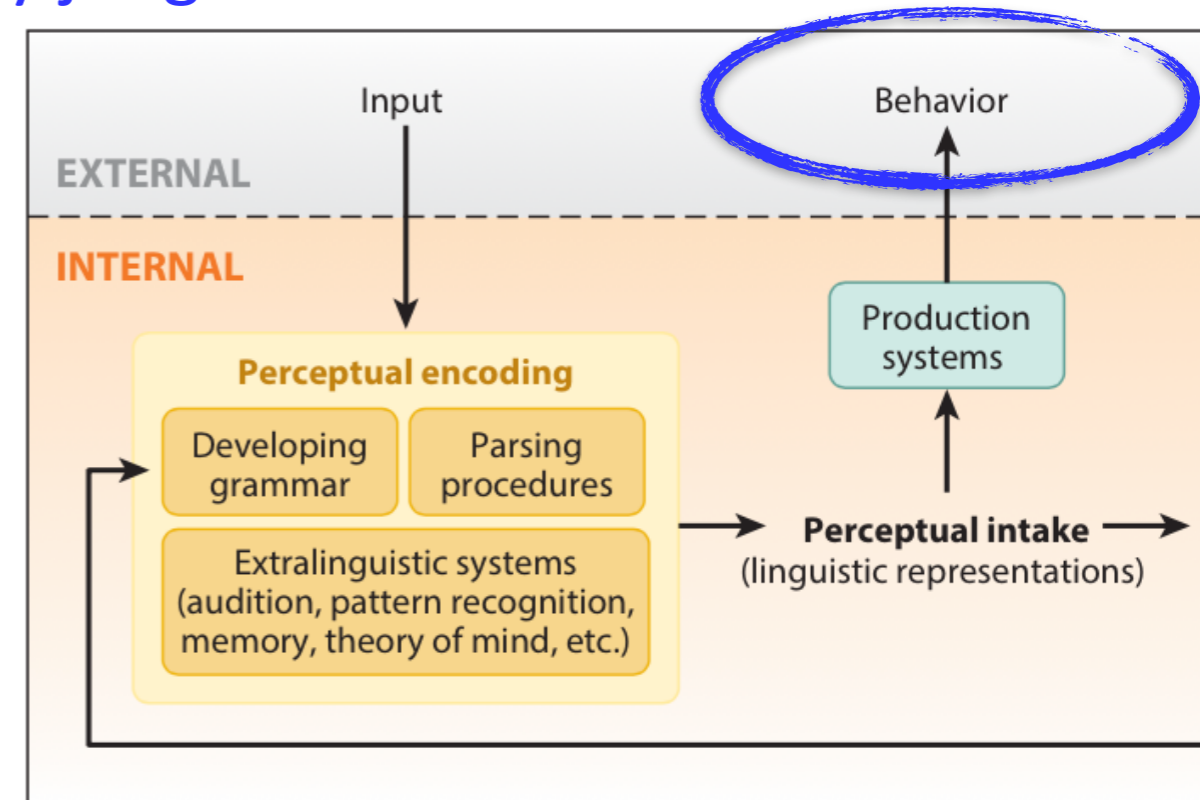
**length** of dependency

(**matrix** vs. **embedded**)

presence of an **island** structure

(**non-island** vs. **island**)

Complex NP island stimuli



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Who \_\_\_ claimed that Lily forgot the necklace?

What did the teacher claim that Lily forgot \_\_\_?

Who \_\_\_ made the claim that Lily forgot the necklace?

\*What did the teacher make the claim that Lily forgot \_\_\_?

matrix | non-island

embedded | non-island

matrix | island

embedded | island

# Adult judgments: Target behavior



syntax



syntactic island

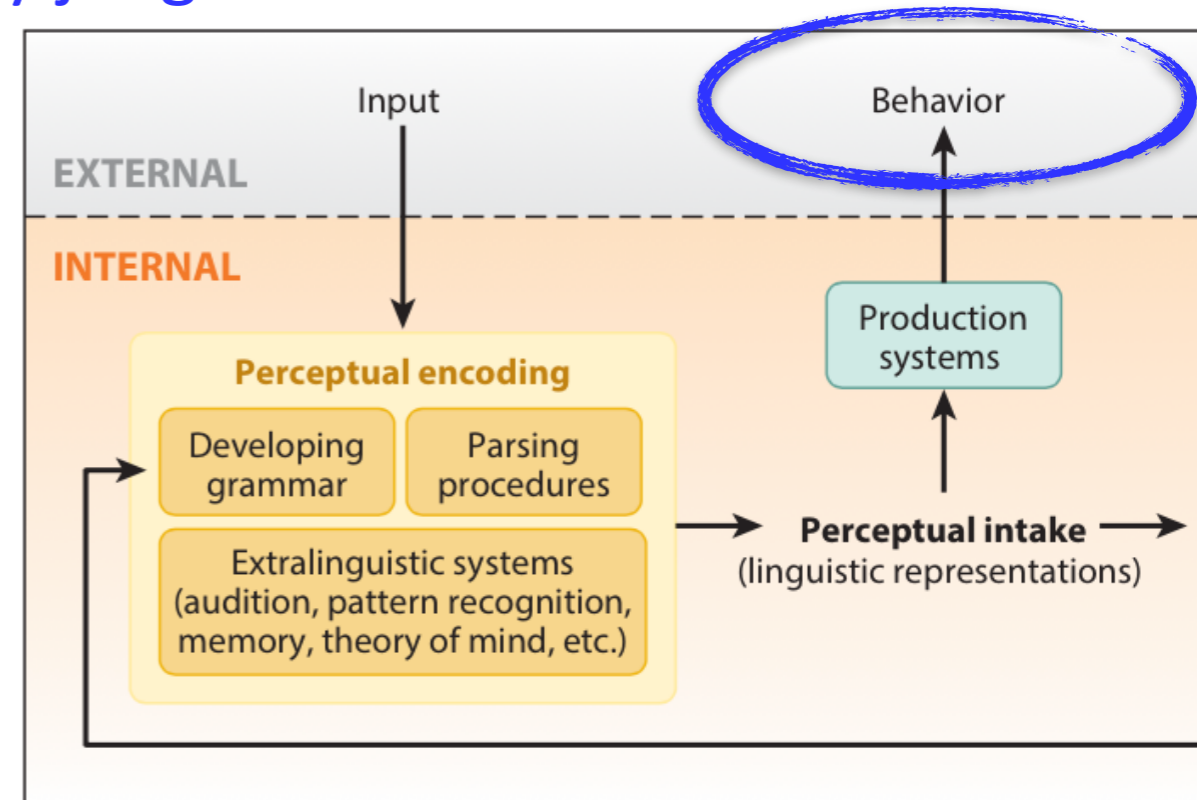
Adult knowledge as measured by **acceptability judgment** behavior

*Sprouse et al. (2012)*

**length** of dependency  
(**matrix** vs. **embedded**)

presence of an **island** structure  
(**non-island** vs. **island**)

Subject island stimuli



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Who \_\_\_ thinks the necklace is expensive?

What does Jack think \_\_\_ is expensive?

Who \_\_\_ thinks the necklace for Lily is expensive?

\*Who does Jack think the necklace for \_\_\_ is expensive?

matrix | non-island

embedded | non-island

matrix | island

embedded | island

# Adult judgments: Target behavior



syntax



syntactic island

Adult knowledge as measured by **acceptability judgment** behavior

*Sprouse et al. (2012)*

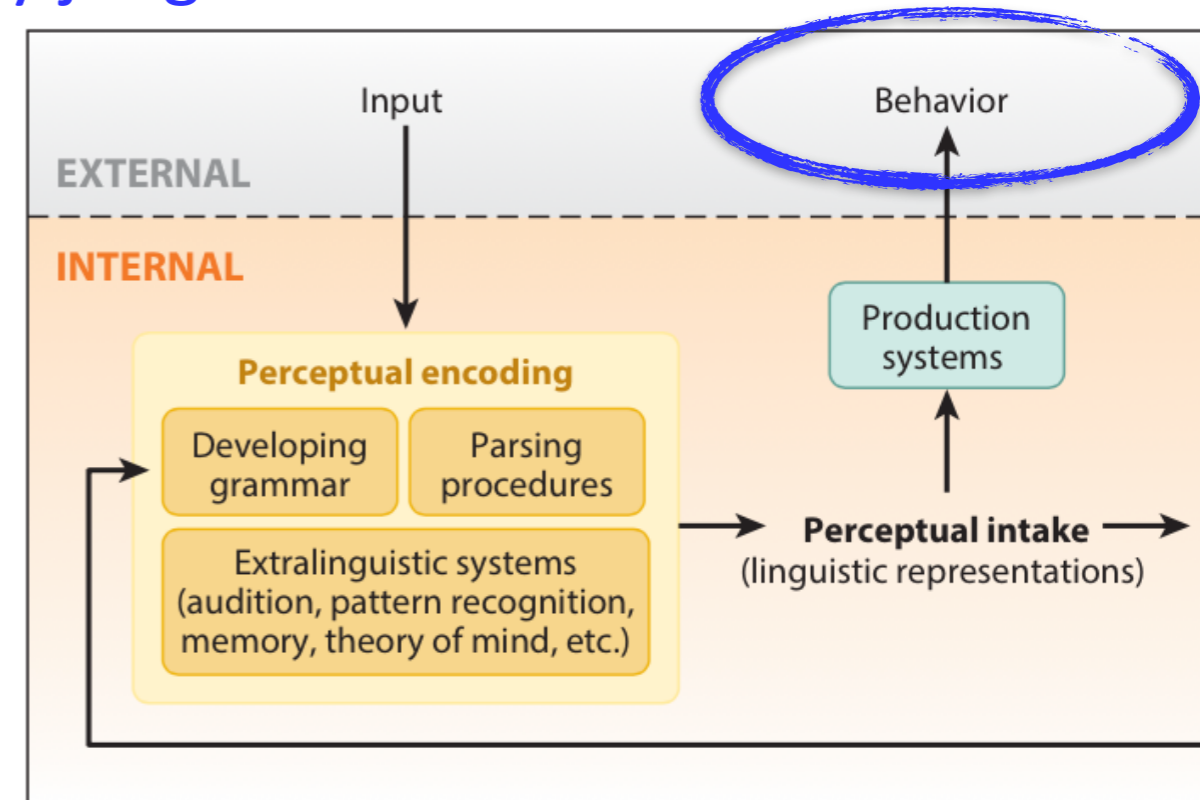
**length** of dependency

(**matrix** vs. **embedded**)

presence of an **island** structure

(**non-island** vs. **island**)

Whether island stimuli



Lidz & Gagliardi 2015

Who \_\_\_ thinks that Jack stole the necklace?

What does the teacher think that Jack stole \_\_\_ ?

Who \_\_\_ wonders whether Jack stole the necklace?

\*What does the teacher wonder whether Jack stole \_\_\_ ?

matrix | non-island

embedded | non-island

matrix | island

embedded | island

# Adult judgments: Target behavior



syntax



syntactic island

Adult knowledge as measured by **acceptability judgment** behavior

*Sprouse et al. (2012)*

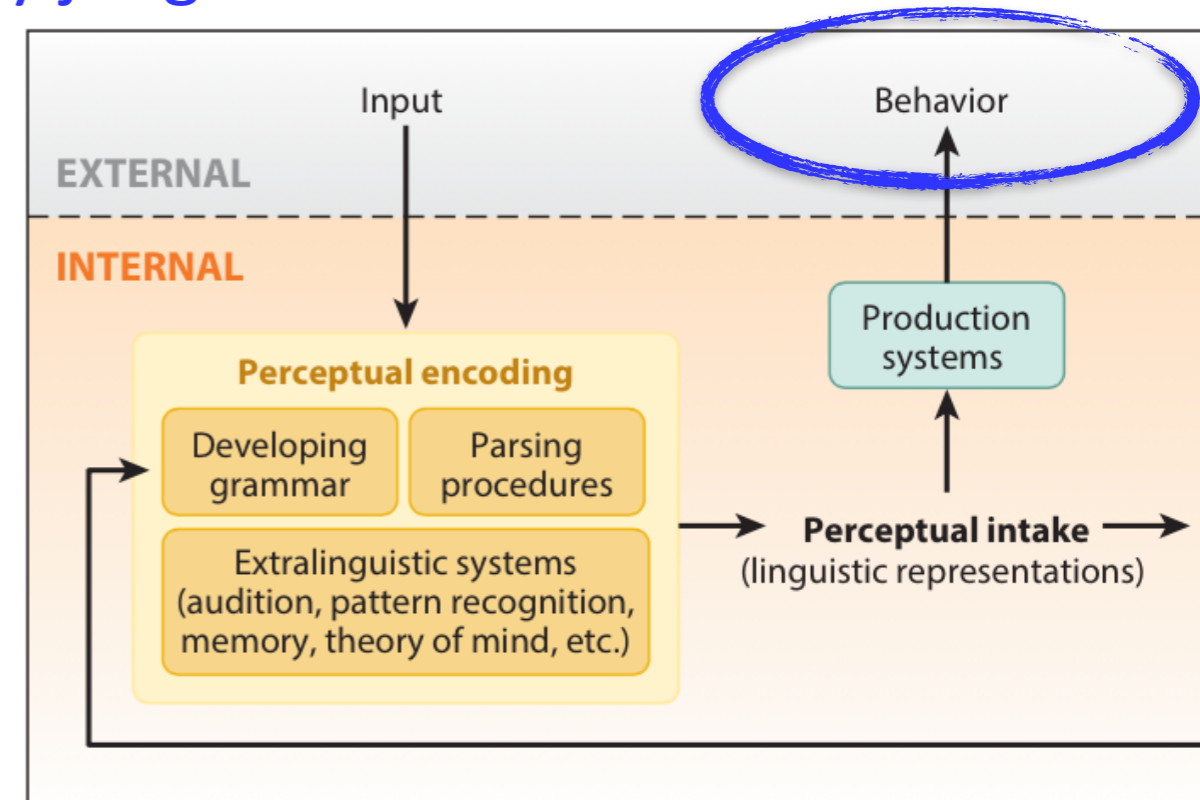
**length** of dependency

(**matrix** vs. **embedded**)

presence of an **island** structure

(**non-island** vs. **island**)

Adjunct island stimuli



Lidz & Gagliardi 2015

Who \_\_\_ thinks that Lily forgot the necklace?

What does the teacher think that Lily forgot \_\_\_ ?

Who \_\_\_ worries if Lily forgot the necklace?

\*What does the teacher worry if Lily forgot \_\_\_ ?

matrix | non-island

embedded | non-island

matrix | island

embedded | island

# Adult judgments: Target behavior



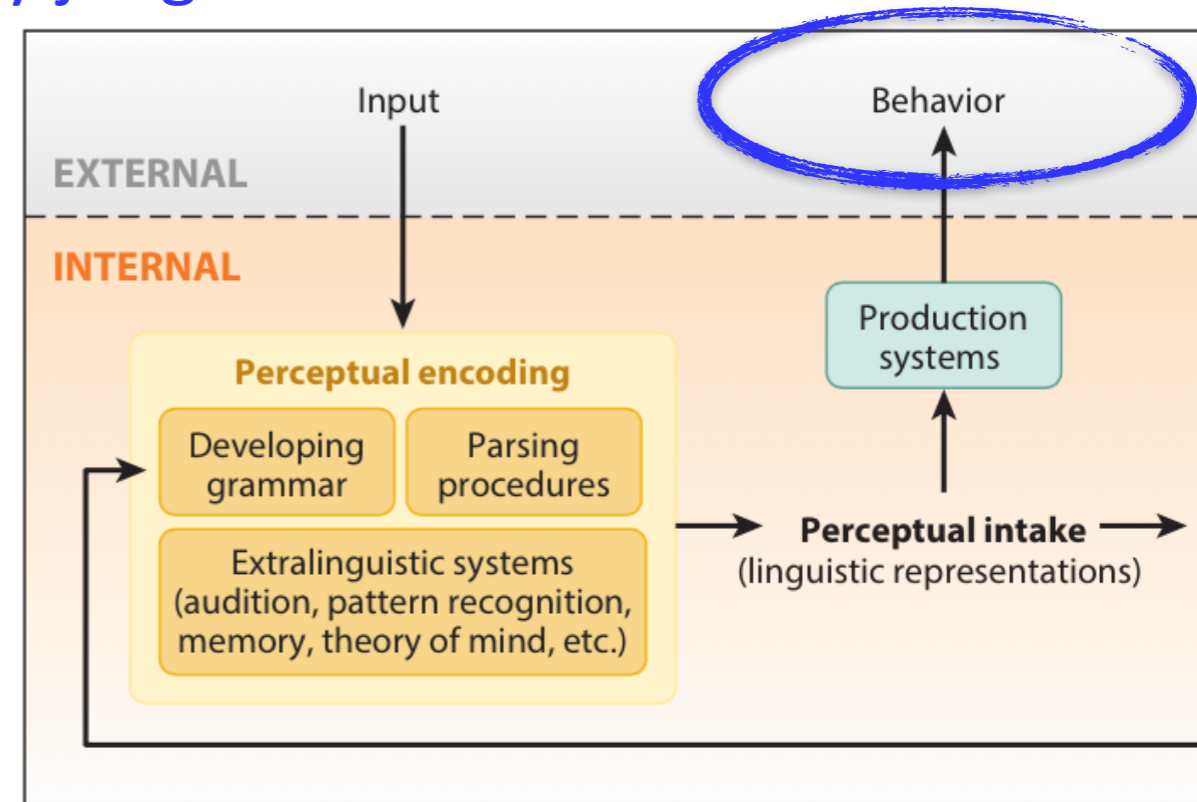
syntax



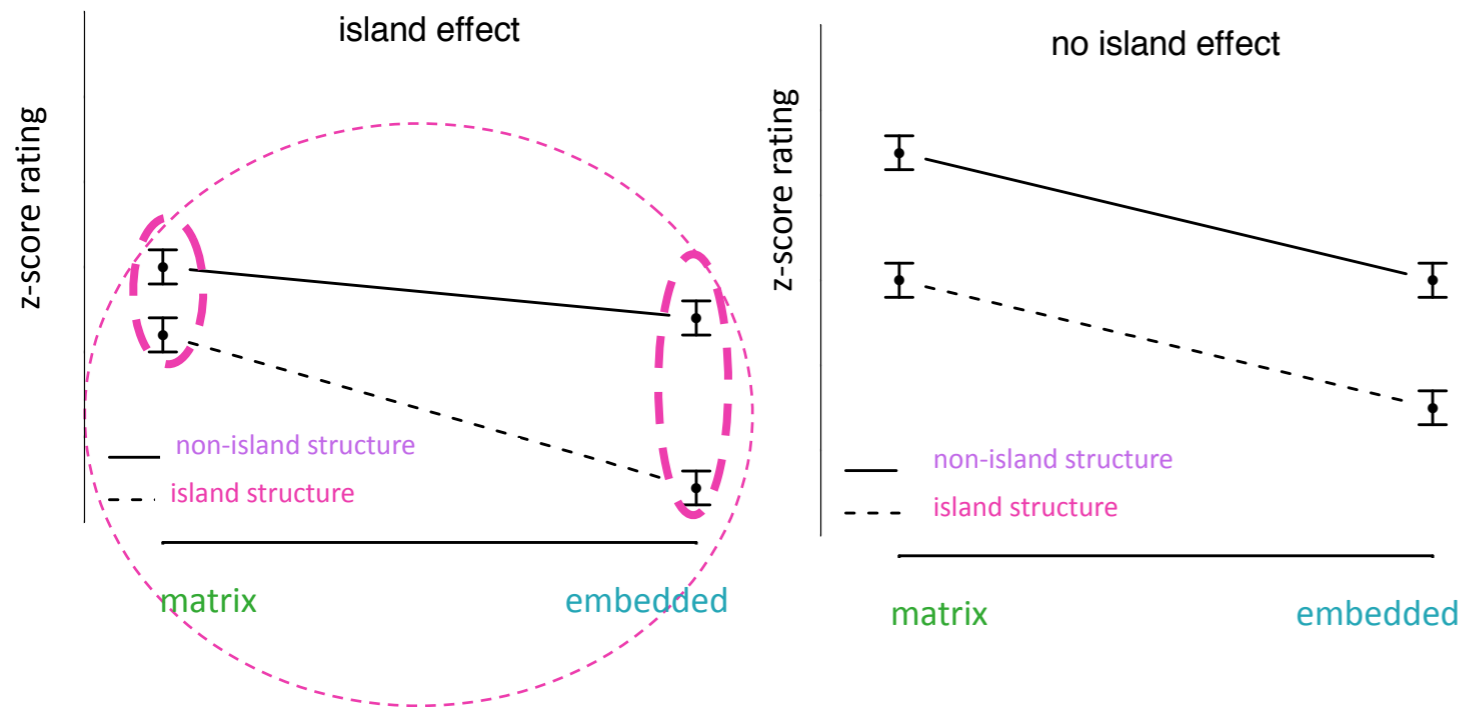
syntactic island

Adult knowledge as measured by **acceptability judgment** behavior

Syntactic island = **superadditive** interaction of the two factors (additional unacceptability that arises when the two factors — **length** & presence of an **island** structure — are combined, above and beyond the independent contribution of each factor).



Lidz & Gagliardi 2015



# Adult judgments: Target behavior



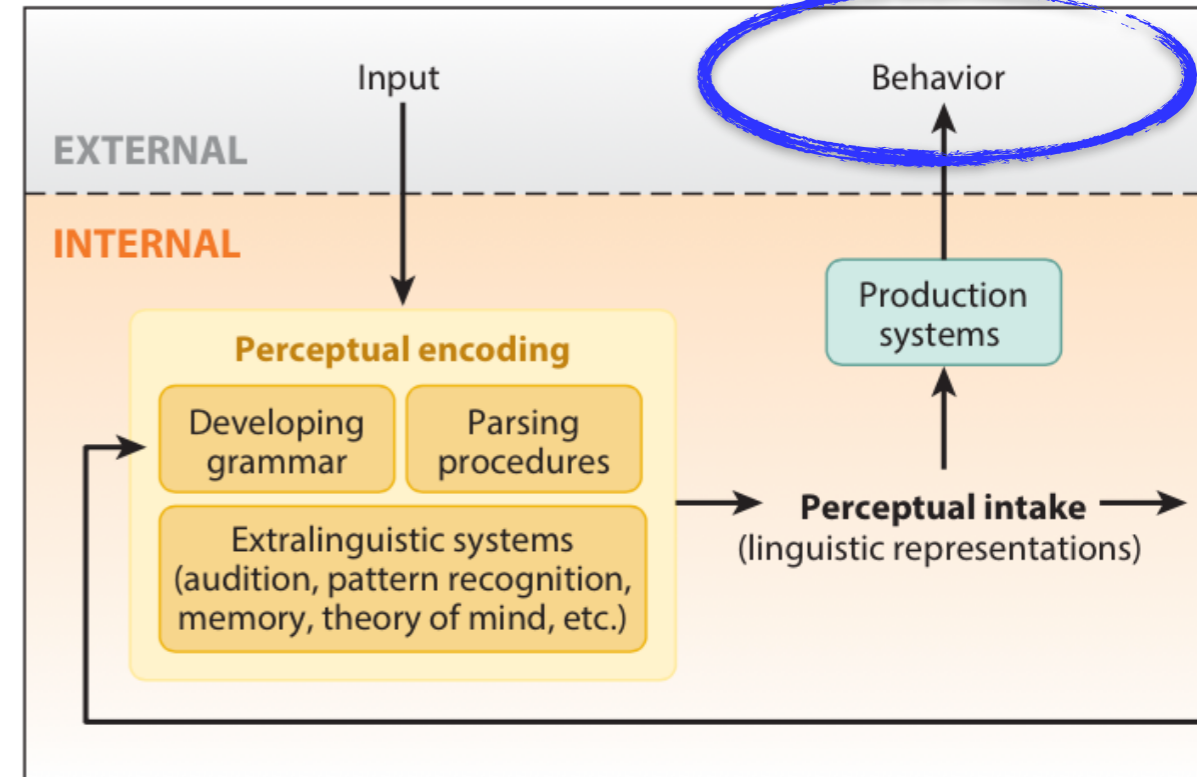
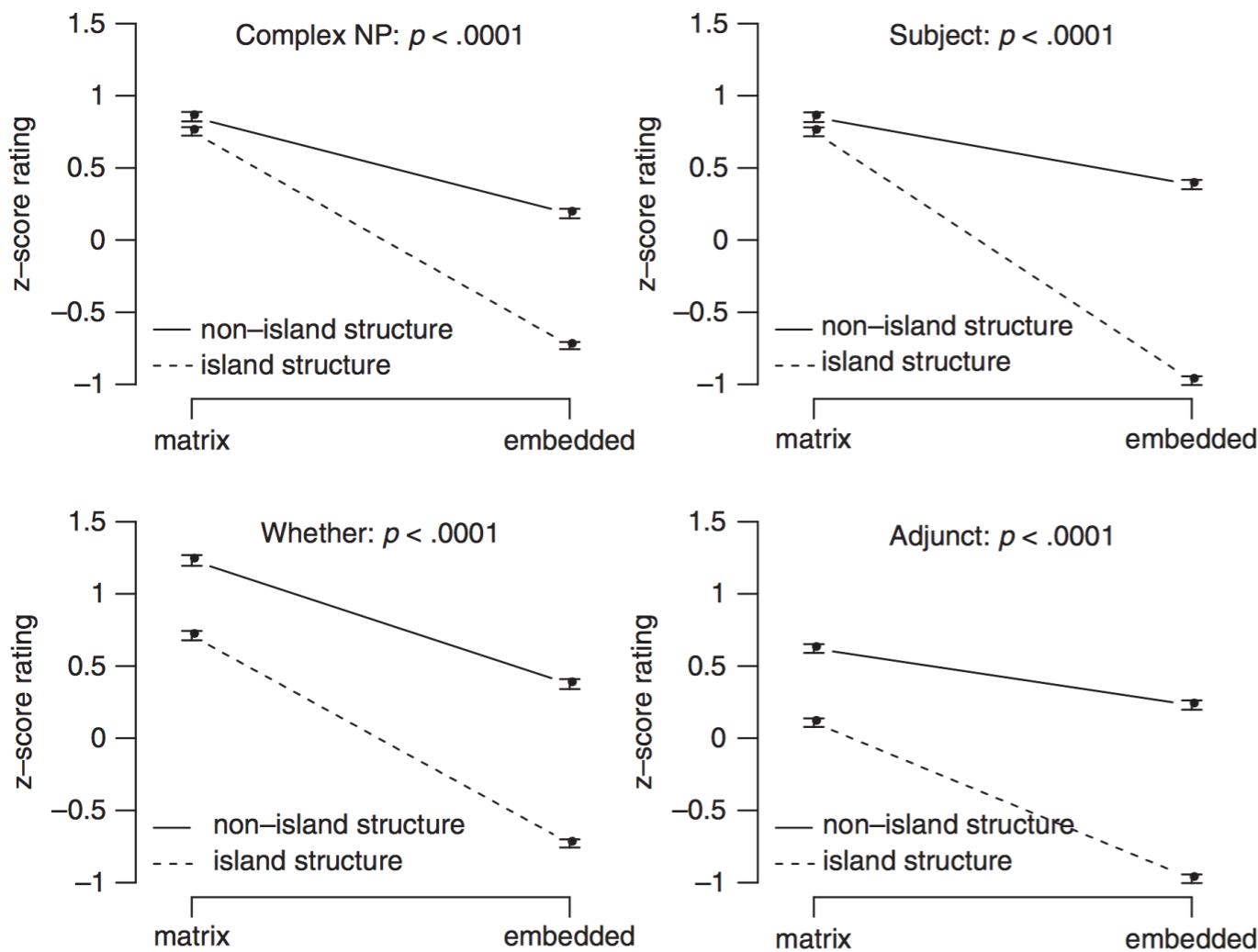
syntax



syntactic island

## Adult knowledge as measured by acceptability judgment behavior

Sprouse et al. (2012): acceptability judgments from 173 adult subjects



Lidz & Gagliardi 2015

**Superadditivity** present for all islands tested = Knowledge that dependencies cannot cross these island structures is part of adult knowledge about syntactic islands.



# Adult judgments: Target behavior



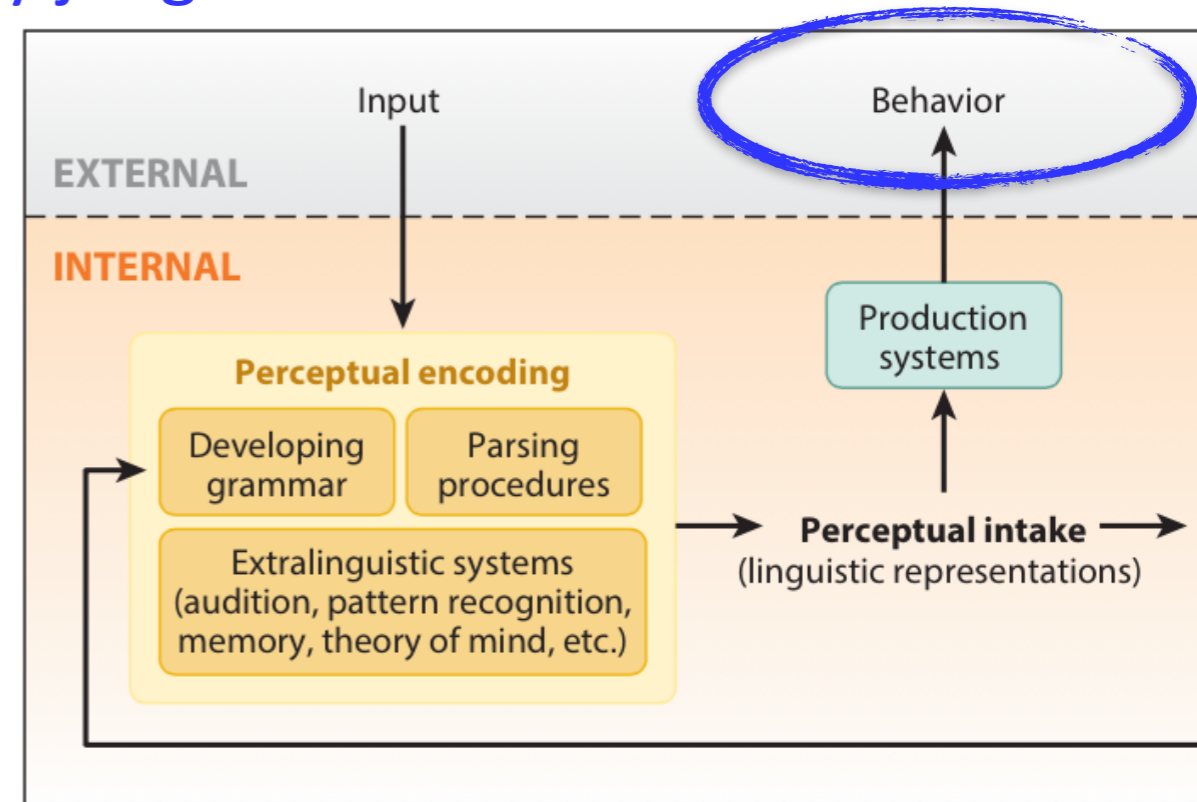
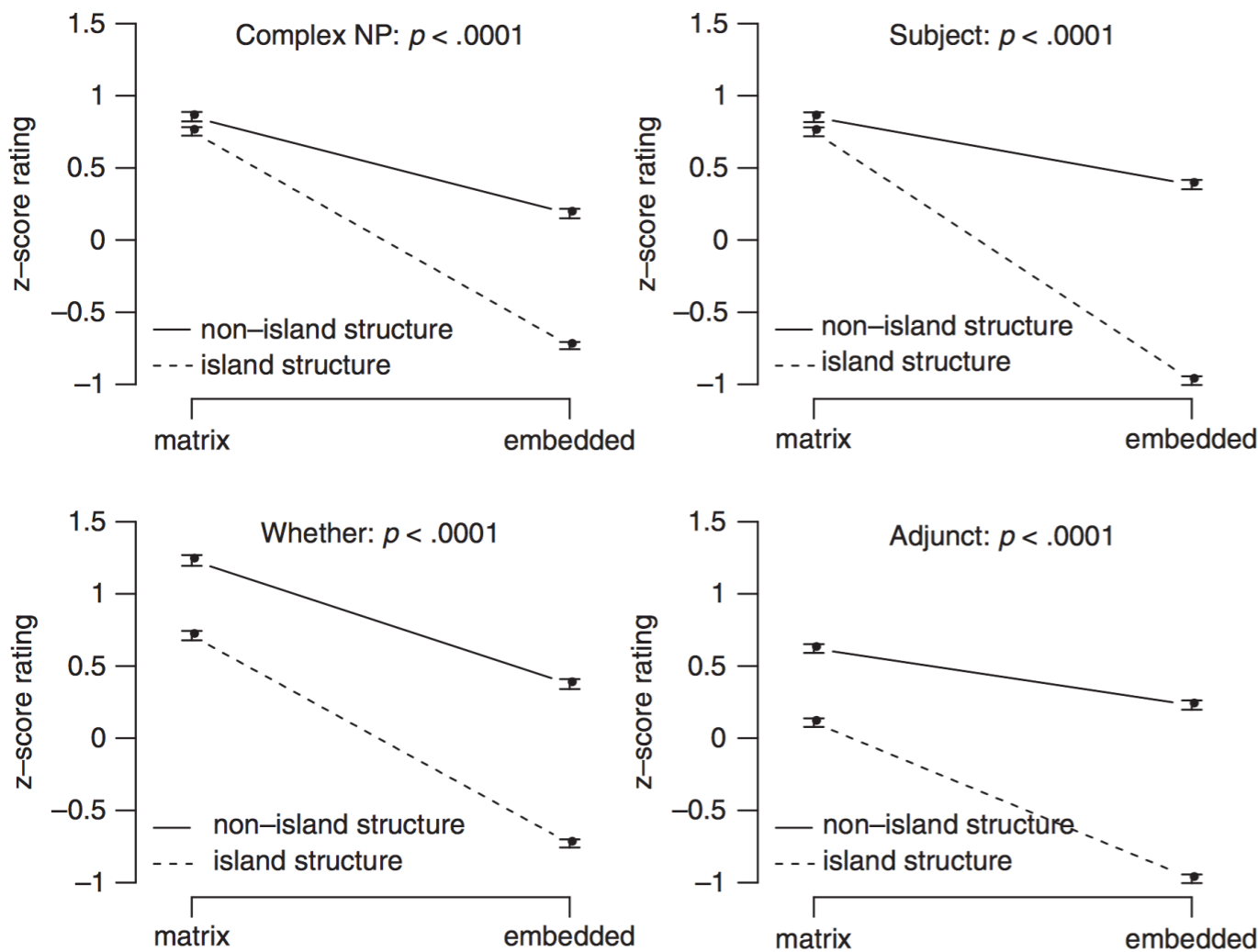
syntax



syntactic island

## Adult knowledge as measured by acceptability judgment behavior

Sprouse et al. (2012): acceptability judgments from 173 adult subjects



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Importance for acquisition: This is one kind of **target behavior** that we'd like a modeled child to produce.

# Adult judgments: Target behavior



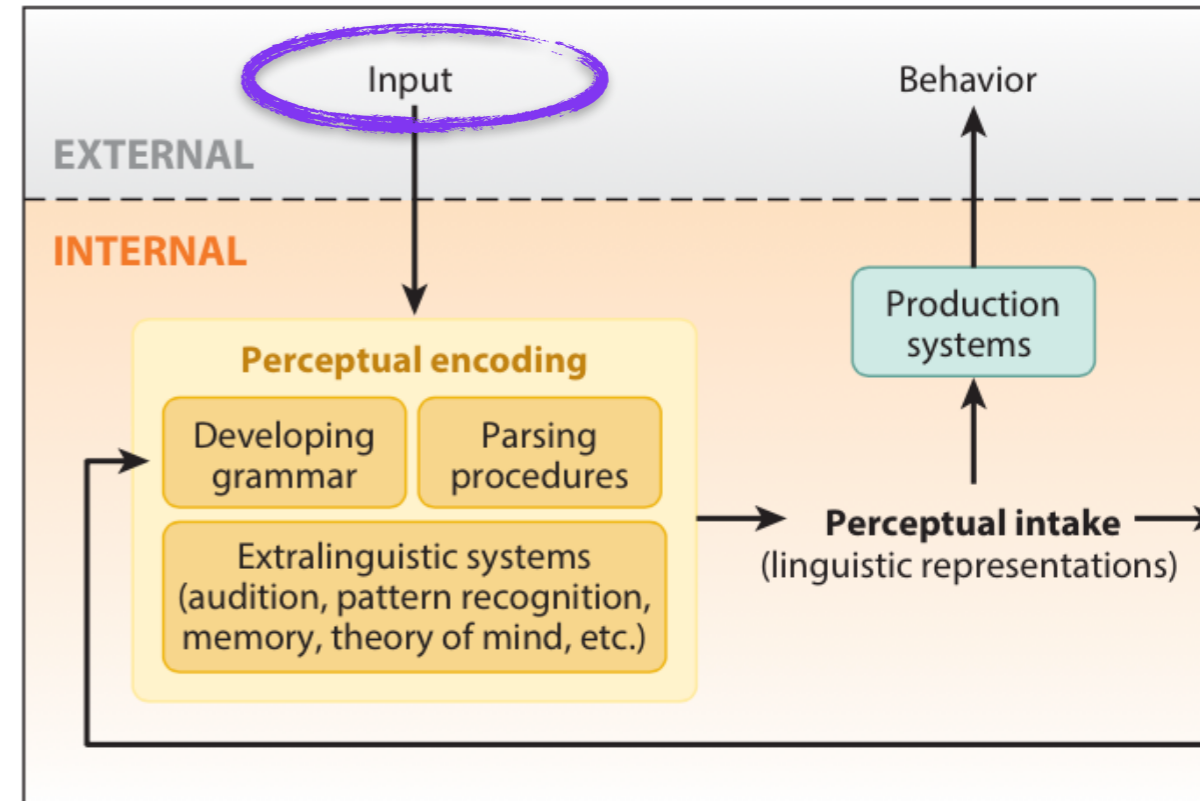
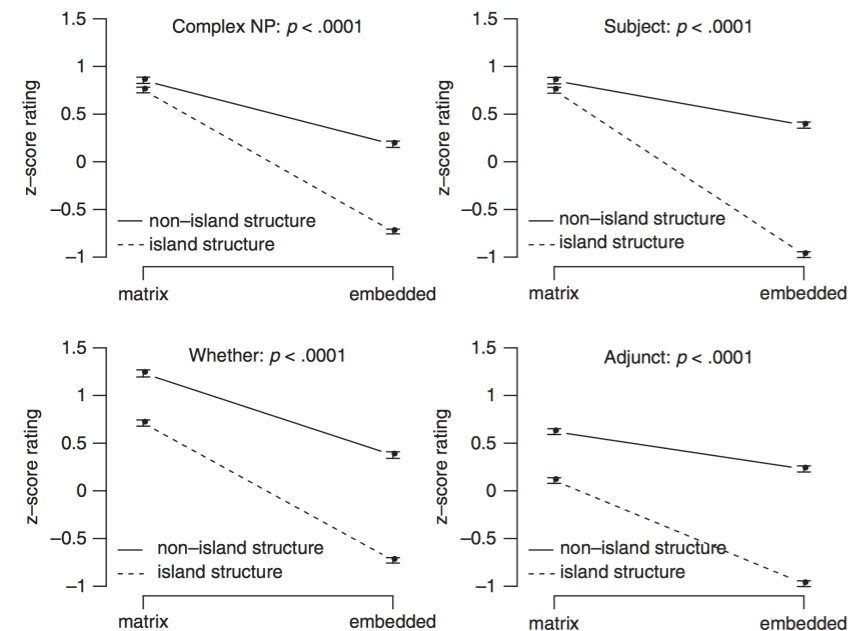
syntax



syntactic island

Adult knowledge as measured by **acceptability judgment** behavior

Sprouse et al. (2012): acceptability judgments from 173 adult subjects



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So if we're focusing on these *wh*-dependencies and that specific target state, what does **children's input** look like?



Pearl & Sprouse 2013a, 2013b, 2015

# Children's input



syntax



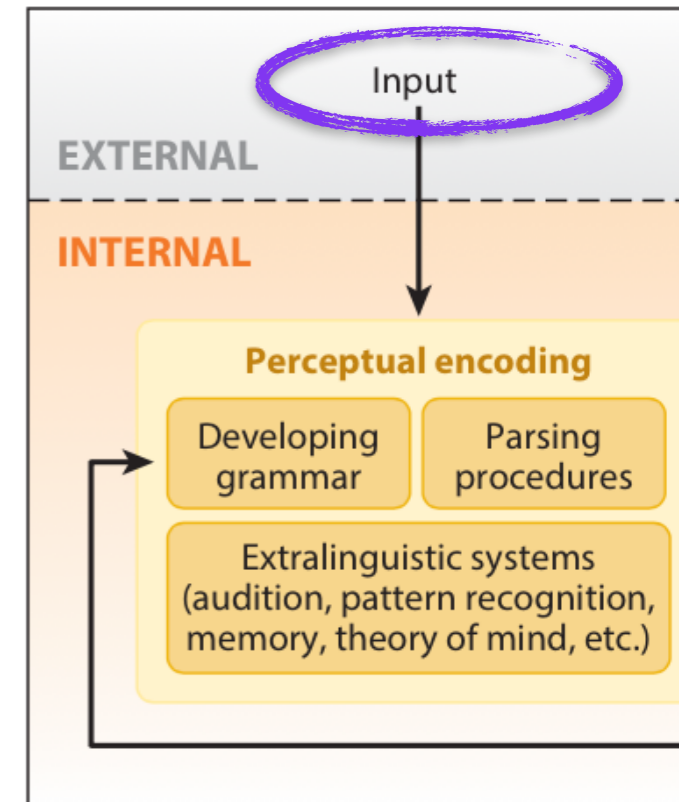
syntactic island

## Children's input really doesn't look so helpful

Data from five corpora of child-directed speech (Brown-Adam, Brown-Eve, Brown-Sarah, Suppes, Valian) from CHILDES (MacWhinney 2000): speech to 25 children between the ages of one and five years old.

= 813,036 words

= 31,247 utterances containing a *wh*-dependency



Lidz & Gagliardi 2015

# Children's input

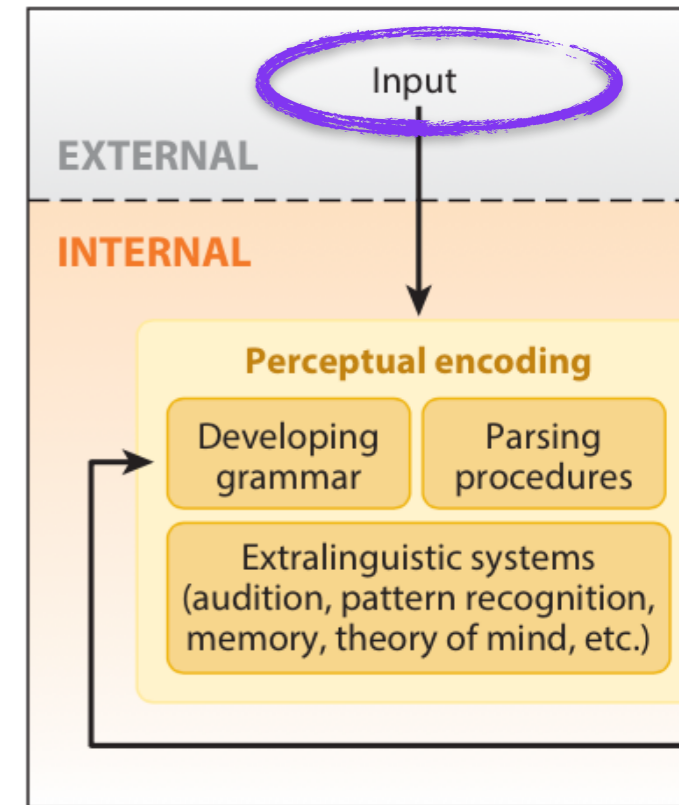


## Children's input really doesn't look so helpful

Data from five corpora of child-directed speech = **31,247** utterances containing a *wh*-dependency

	<i>grammatical stimuli</i>		<i>syntactic island</i>	
	MATRIX + NON-ISLAND	EMBEDDED + NON-ISLAND	MATRIX + ISLAND	EMBEDDED + ISLAND
Complex NP	7	295	0	0
Subject	7	29	0	0
Whether	7	295	0	0
Adjunct	7	295	15	0

These kinds of utterances are fairly rare in general - the most frequent appears about 0.9% of the time (295 of 31,247.)



Lidz & Gagliardi 2015



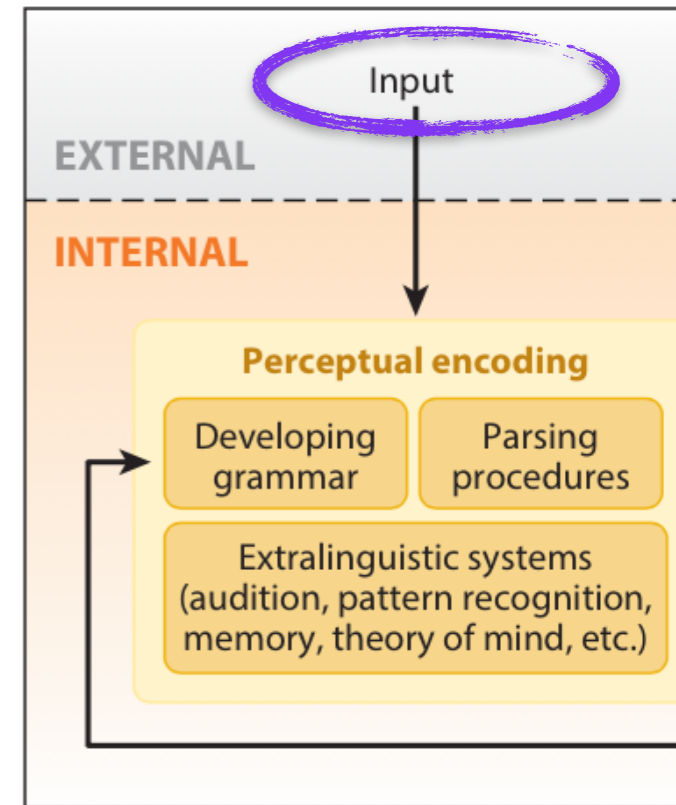
# Children's input



Children's input really doesn't look so helpful

Data from five corpora of child-directed speech = **31,247** utterances containing a *wh*-dependency

	<i>grammatical stimuli</i>		<i>syntactic island</i>	
	MATRIX + NON-ISLAND	EMBEDDED + NON-ISLAND	MATRIX + ISLAND	EMBEDDED + ISLAND
Complex NP	7	295	0	0
Subject	7	29	0	0
Whether	7	295	0	0
Adjunct	7	295	15	0



Lidz & Gagliardi 2015

Being grammatical doesn't necessarily mean an utterance will appear in the input at all.



# Children's input



syntax

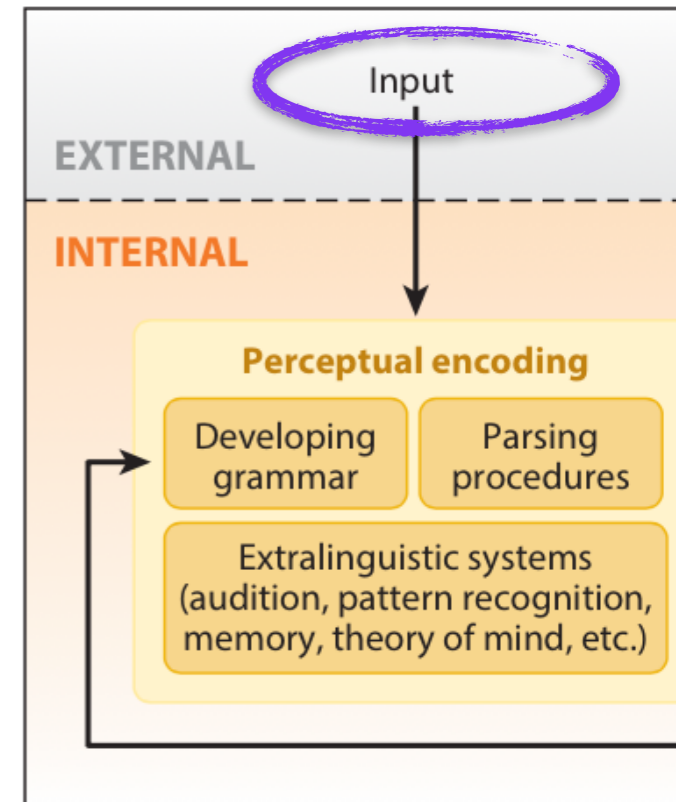


syntactic island

Children's input really doesn't look so helpful

Data from five corpora of child-directed speech = **31,247** utterances containing a *wh*-dependency

	<i>grammatical stimuli</i>		<i>syntactic island</i>	
	MATRIX + NON-ISLAND	EMBEDDED + NON-ISLAND	MATRIX + ISLAND	EMBEDDED + ISLAND
Complex NP	7	295	0	0
Subject	7	29	0	0
Whether	7	295	0	0
Adjunct	7	295	15	0



Lidz & Gagliardi 2015

Unless the child is sensitive to very small frequencies, it's difficult to tell the difference between grammatical and ungrammatical dependencies sometimes...



# Children's input



syntax

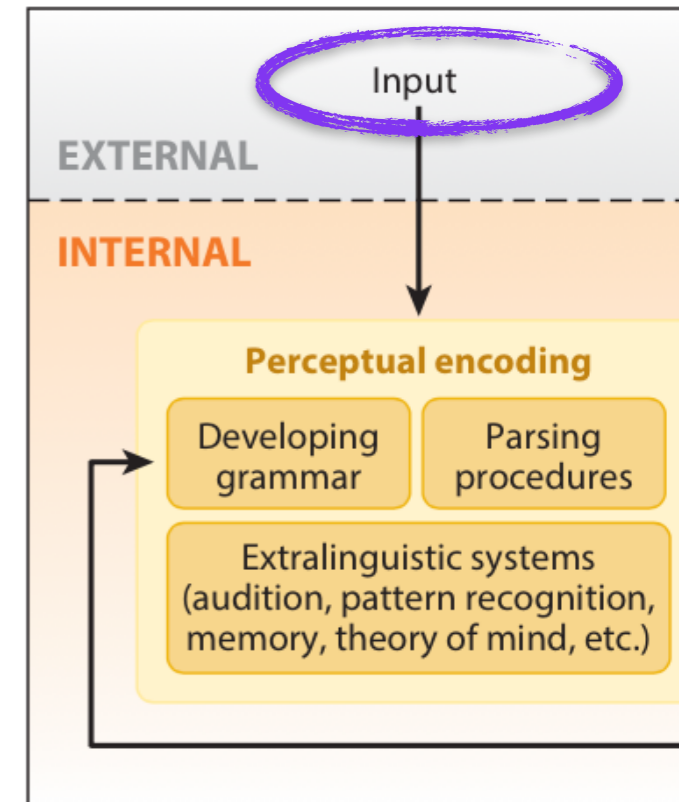


syntactic island

Children's input really doesn't look so helpful

Data from five corpora of child-directed speech = **31,247** utterances containing a *wh*-dependency

	<i>grammatical stimuli</i>		<i>syntactic island</i>	
	MATRIX + NON-ISLAND	EMBEDDED + NON-ISLAND	MATRIX + ISLAND	EMBEDDED + ISLAND
Complex NP	7	295	0	0
Subject	7	29	0	0
Whether	7	295	0	0
Adjunct	7	295	15	0



Lidz & Gagliardi 2015

...and impossible to tell no matter what the rest of the time. This looks like an **induction problem** for the language learner if we're looking for direct evidence in the input.



# Children's input



syntax

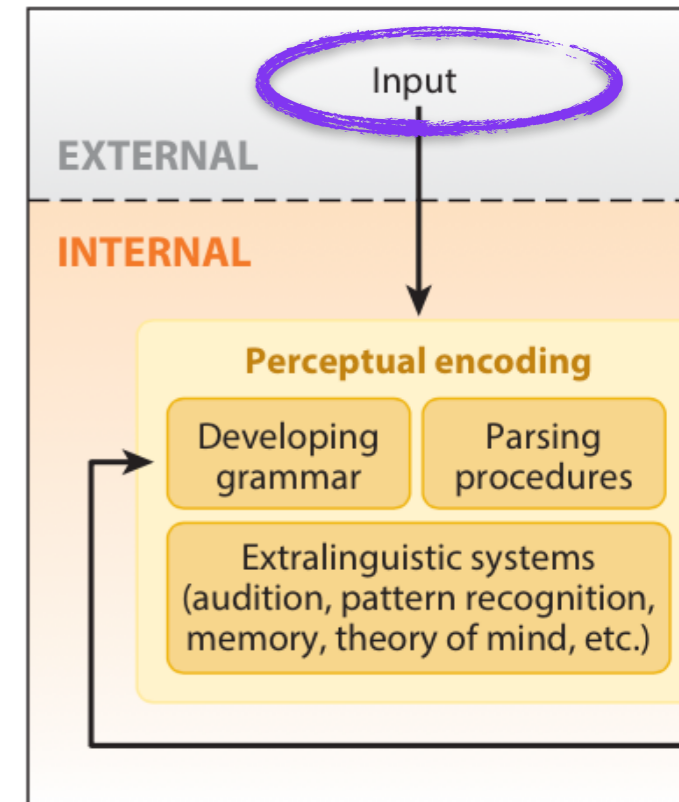


syntactic island

**Children's input really doesn't look so helpful**

Data from five corpora of child-directed speech = **31,247** utterances containing a *wh*-dependency

Important: Some grammatical utterances never appeared at all. This means that **only a subset of grammatical utterances appeared**, and the child has to **generalize appropriately from this subset**.



Lidz & Gagliardi 2015





# Children's input



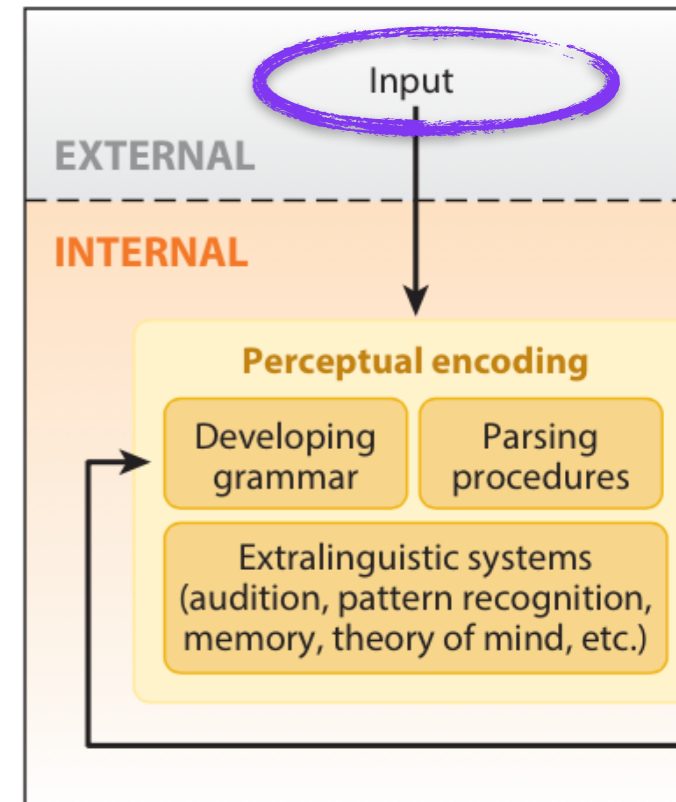
syntax



syntactic island

Data from five corpora of child-directed speech = **31,247** utterances containing a *wh*-dependency

**So what kinds of dependencies *are* in the input?**



Lidz & Gagliardi 2015



# Children's input



syntax



syntactic island

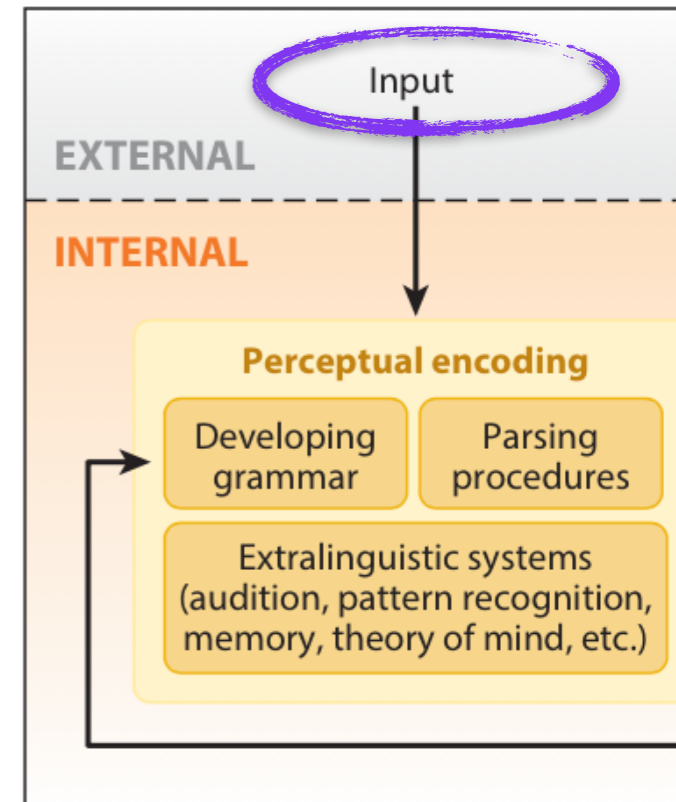
So what kinds of dependencies *are* in the input?

Data from five corpora of child-directed speech = **31,247** utterances containing a *wh*-dependency

**A lot of simpler ones!**

- 76.7% *What did you see \_\_\_?*
- 12.8% *What \_\_\_ happened?*
- 5.6% *What did she want to do \_\_\_?*
- 2.5% *What did she read from \_\_\_?*
- 1.1% *What did she think he said \_\_\_?*

...



Lidz & Gagliardi 2015



# Children's input

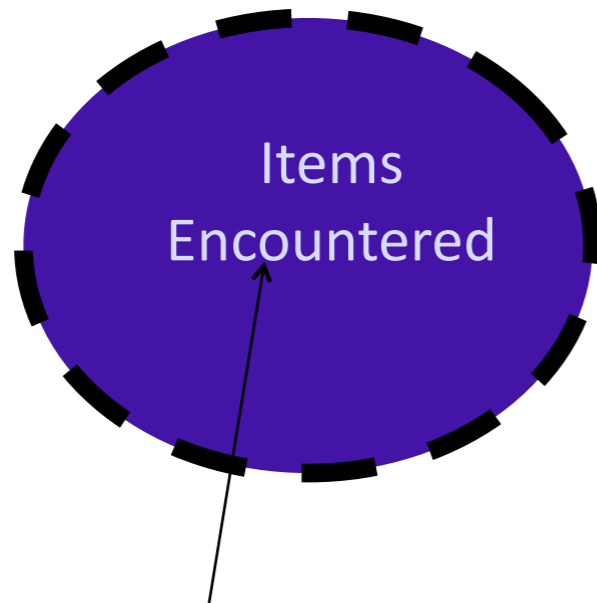


syntax



syntactic island

## The induction problem

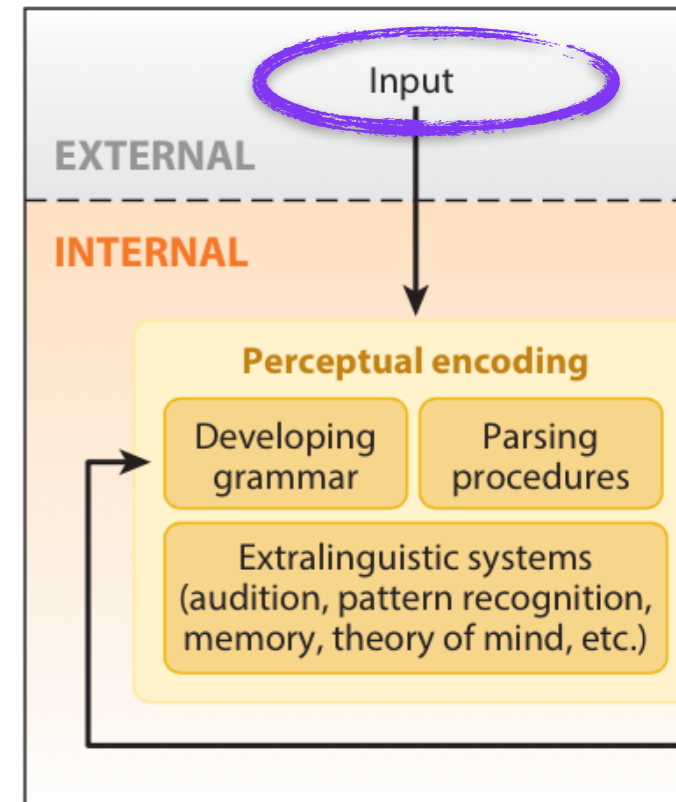


*wh*-questions in input (usually fairly simple)

What did you see \_\_\_?

What \_\_\_ happened?

...



Lidz & Gagliardi 2015



# Children's input

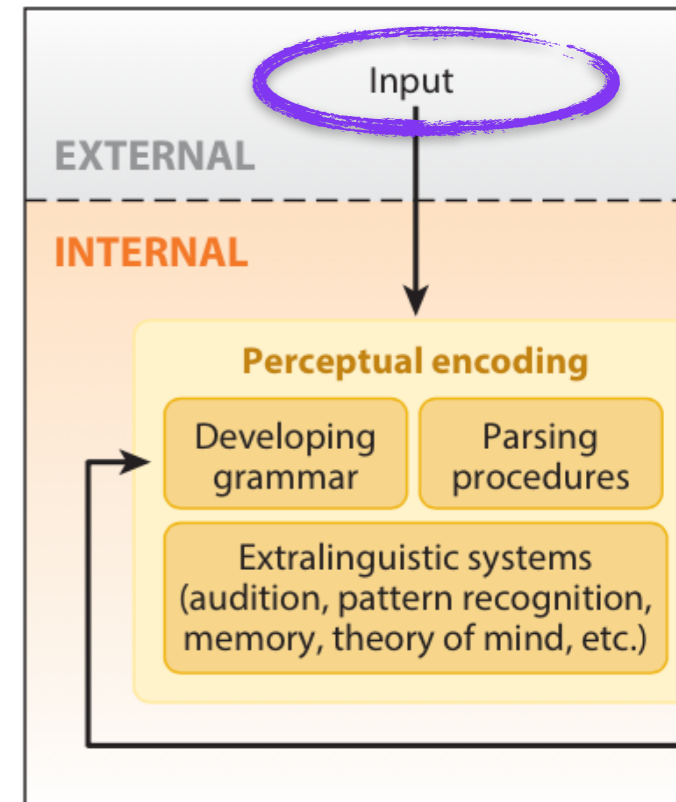
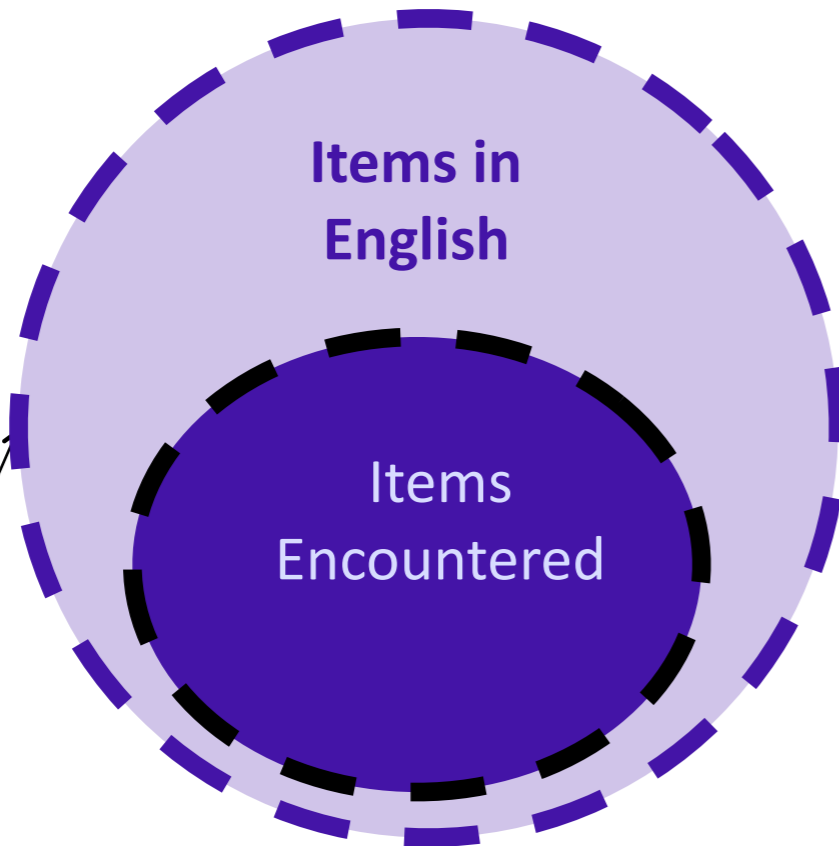


syntax



syntactic island

## The induction problem



Lidz & Gagliardi 2015

## Grammatical *wh*-questions

- What did you see \_\_\_?
- What \_\_\_ happened?
- Who did Jack think that Lily saw \_\_\_?
- What did Jack think \_\_\_ happened?



# Children's input

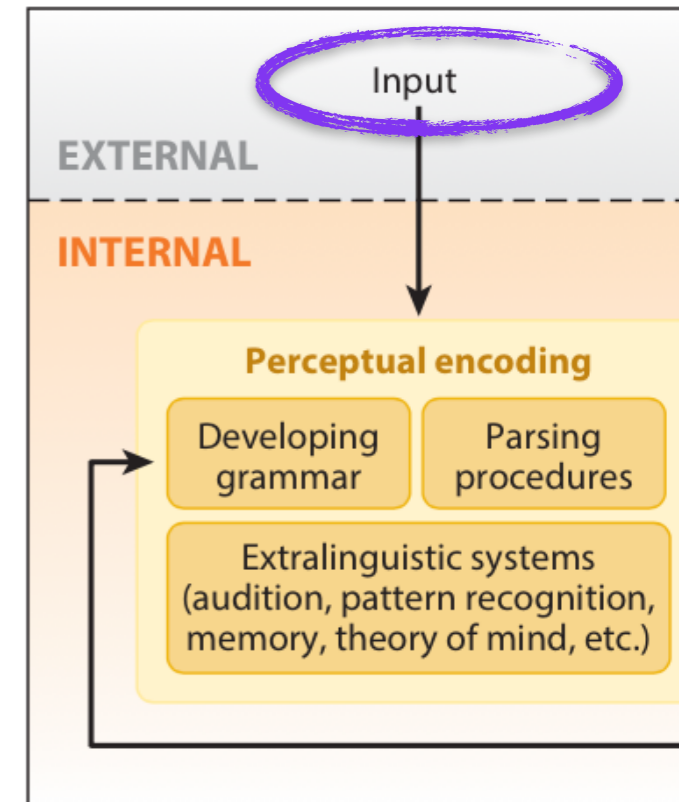
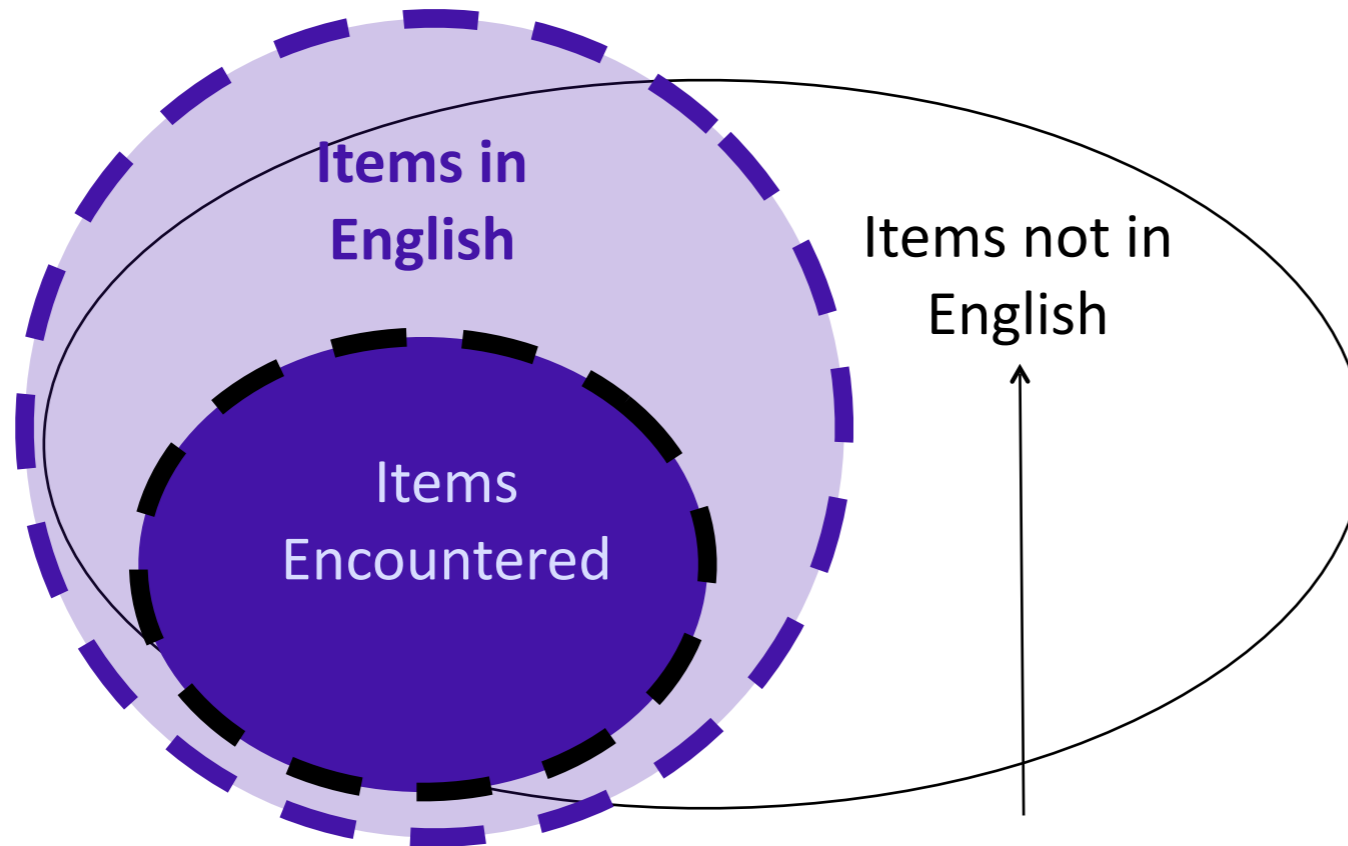


syntax



syntactic island

## The induction problem



Lidz & Gagliardi 2015

## Ungrammatical *wh*-questions: Syntactic islands

*Who does Lily think the kitty for \_\_\_ is pretty?*

*What did Jack make the claim that he bought \_\_\_ ?*

*What did Elizabeth wonder whether Jack bought \_\_\_*

*What did Elizabeth worry if Jack bought \_\_\_ ?*



Pearl & Sprouse 2013a, 2013b, 2015

# Learning strategies

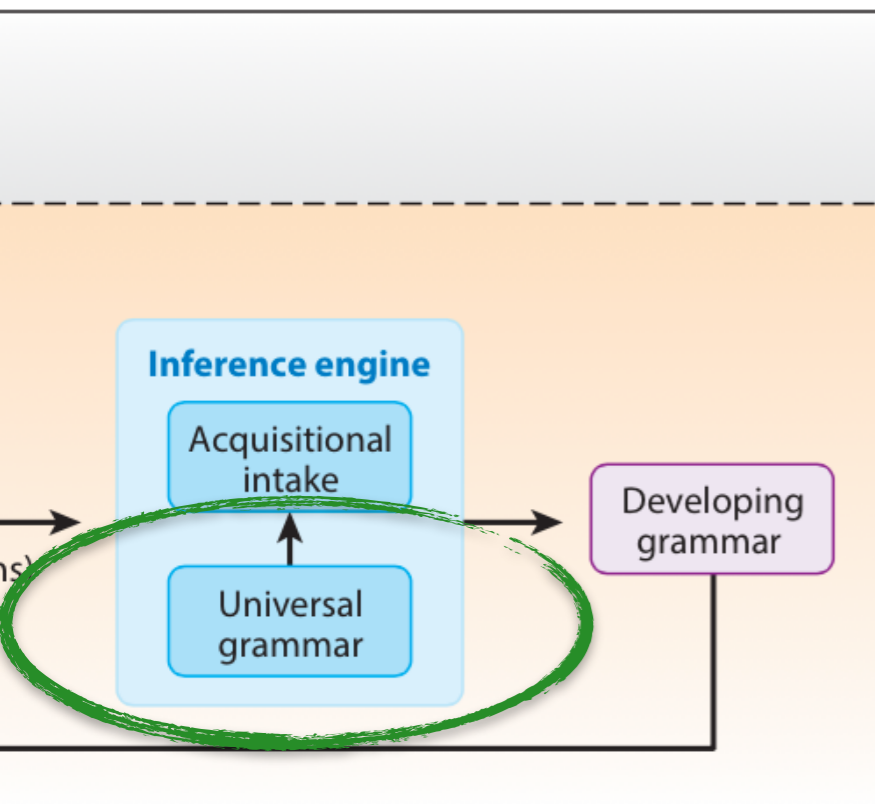


syntax



syntactic island

Previous learning theories suggested children need syntactic-island-specific innate knowledge.



# Learning strategies

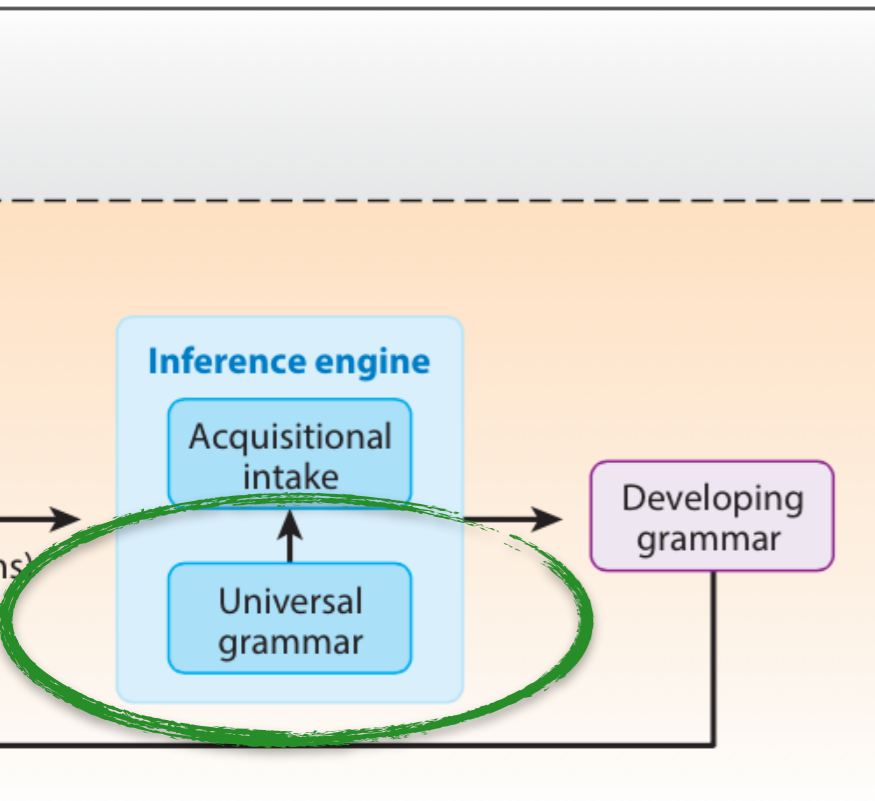
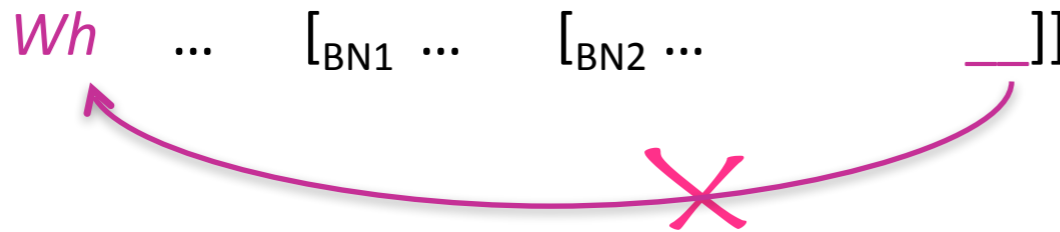


syntax

syntactic island

**Subjacency** (Chomsky 1973, Huang 1982, Lasnik & Saito 1984)

A dependency cannot cross two or more **bounding nodes**.



# Learning strategies

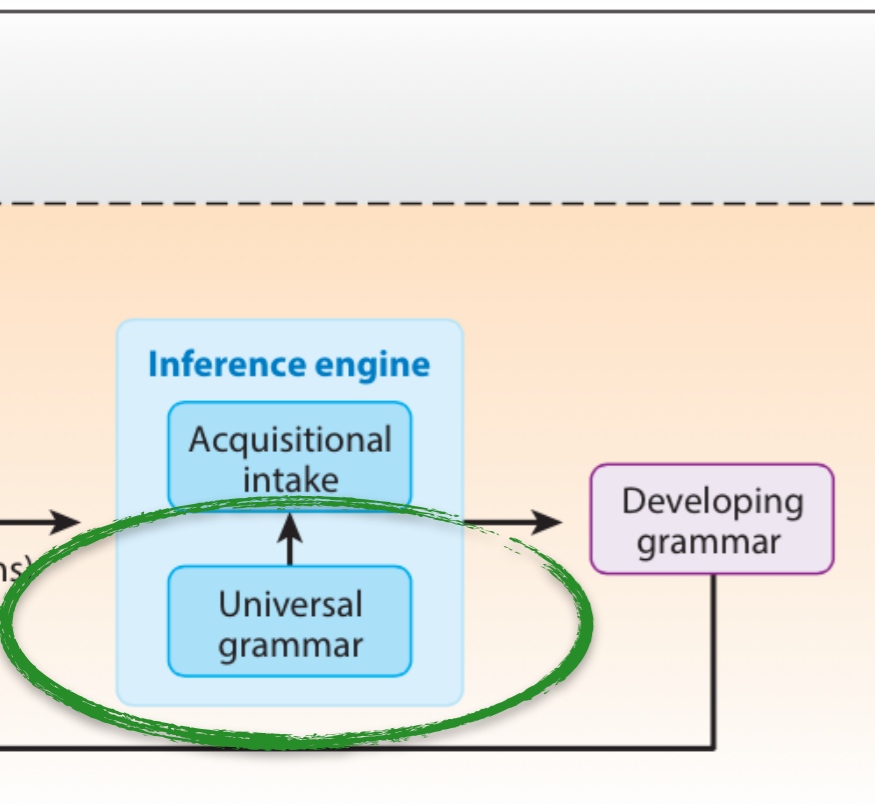
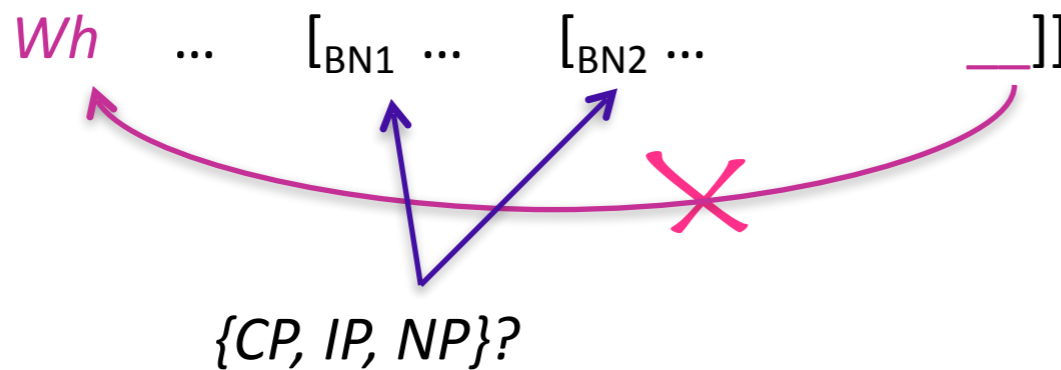


syntax

syntactic island

**Subjacency** (Chomsky 1973, Huang 1982, Lasnik & Saito 1984)

Bounding nodes come from a fixed set (CP, IP, and/or NP). The ones that act as a bounding nodes for a given language must be learned.





# Learning strategies

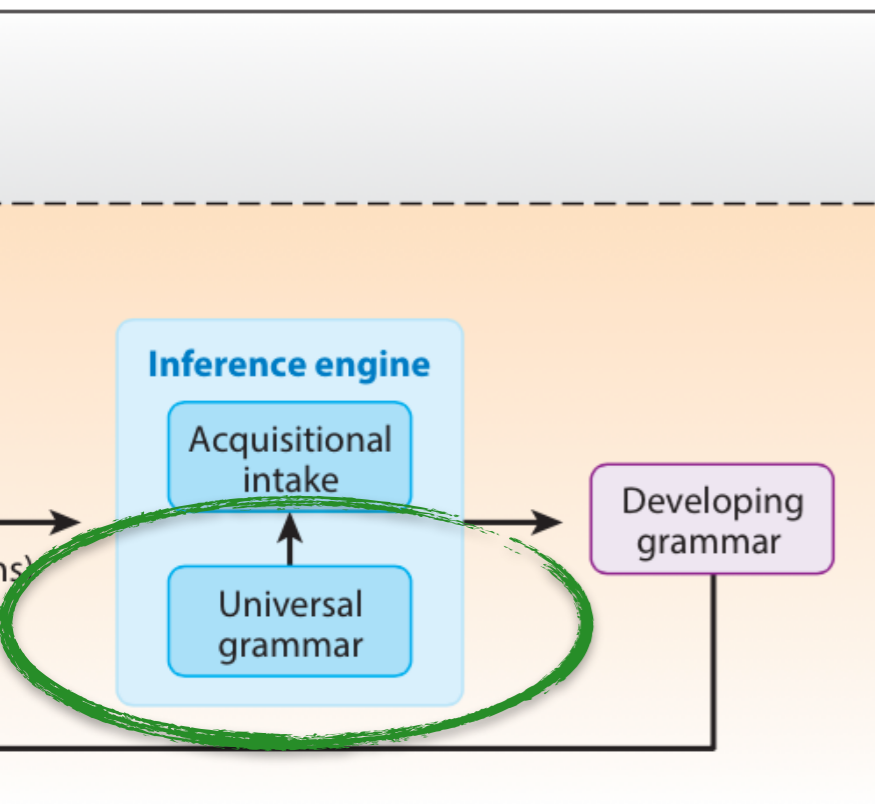
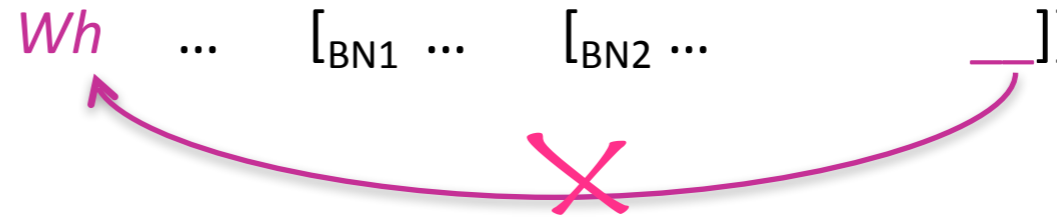


syntax

syntactic island

**Subjacency** (Chomsky 1973, Huang 1982, Lasnik & Saito 1984)

can't cross 2+ bounding nodes  
from a fixed set (CP, IP, and/or NP)



# Learning strategies

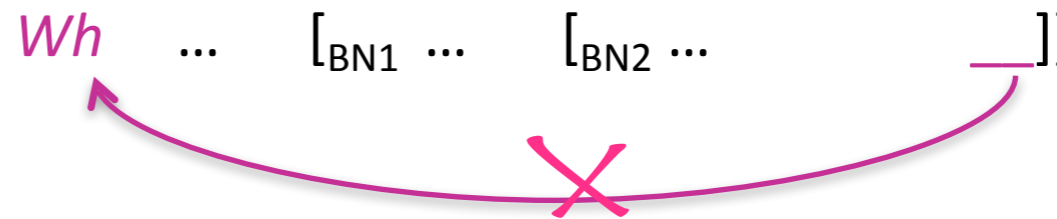


syntax

syntactic island

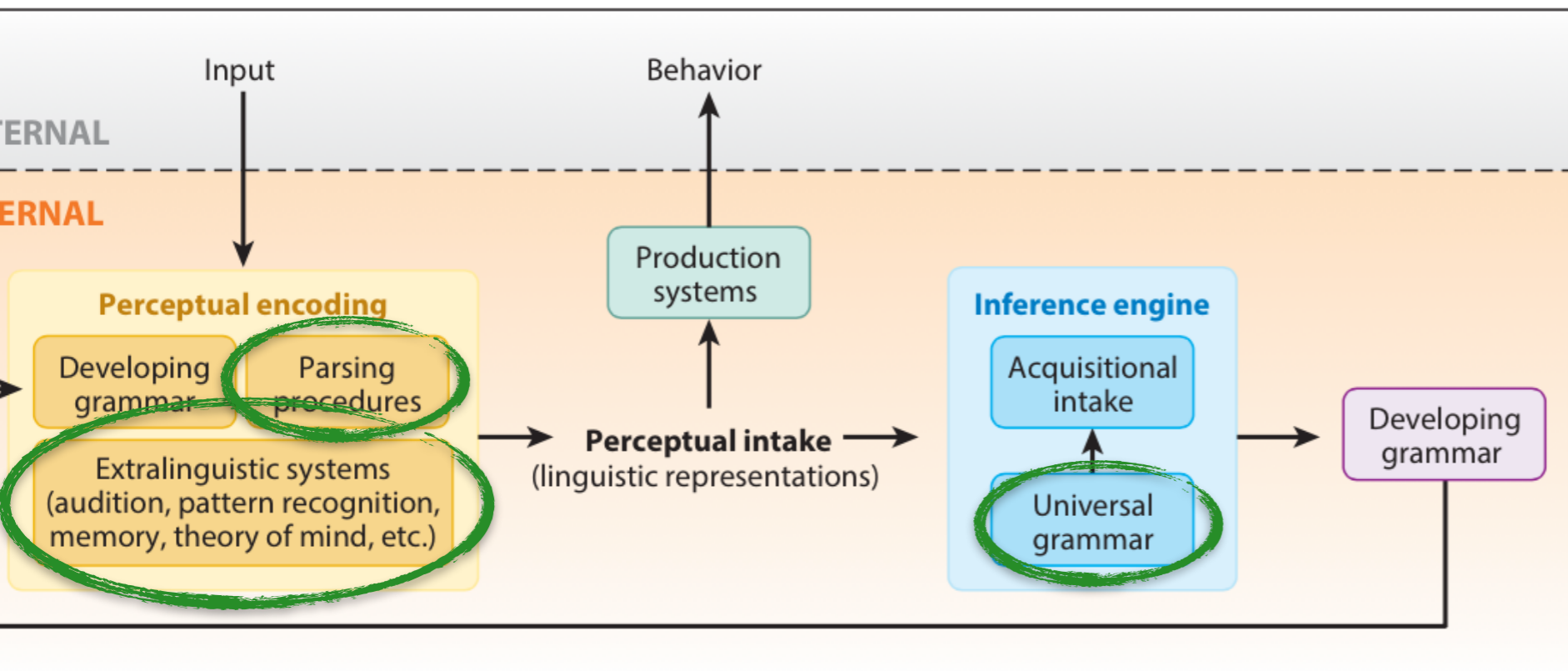
**Subjacency** (Chomsky 1973, Huang 1982, Lasnik & Saito 1984)

can't cross 2+ bounding nodes  
from a fixed set (CP, IP, and/or NP)



An alternative learning strategy proposes children need **less-specific linguistic prior knowledge** along with **probabilistic learning**.

**Subjacency-ish** (Pearl & Sprouse 2013a, 2013b, 2015)



# Learning strategies

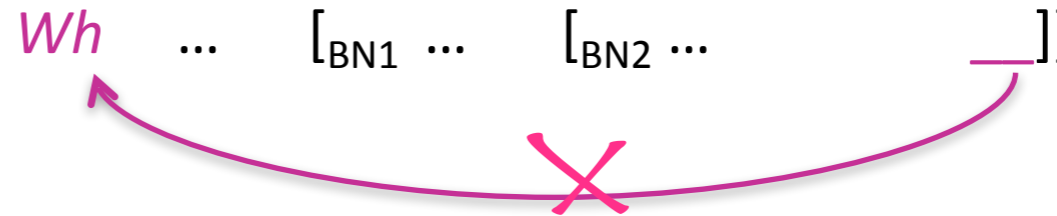


syntax

syntactic island

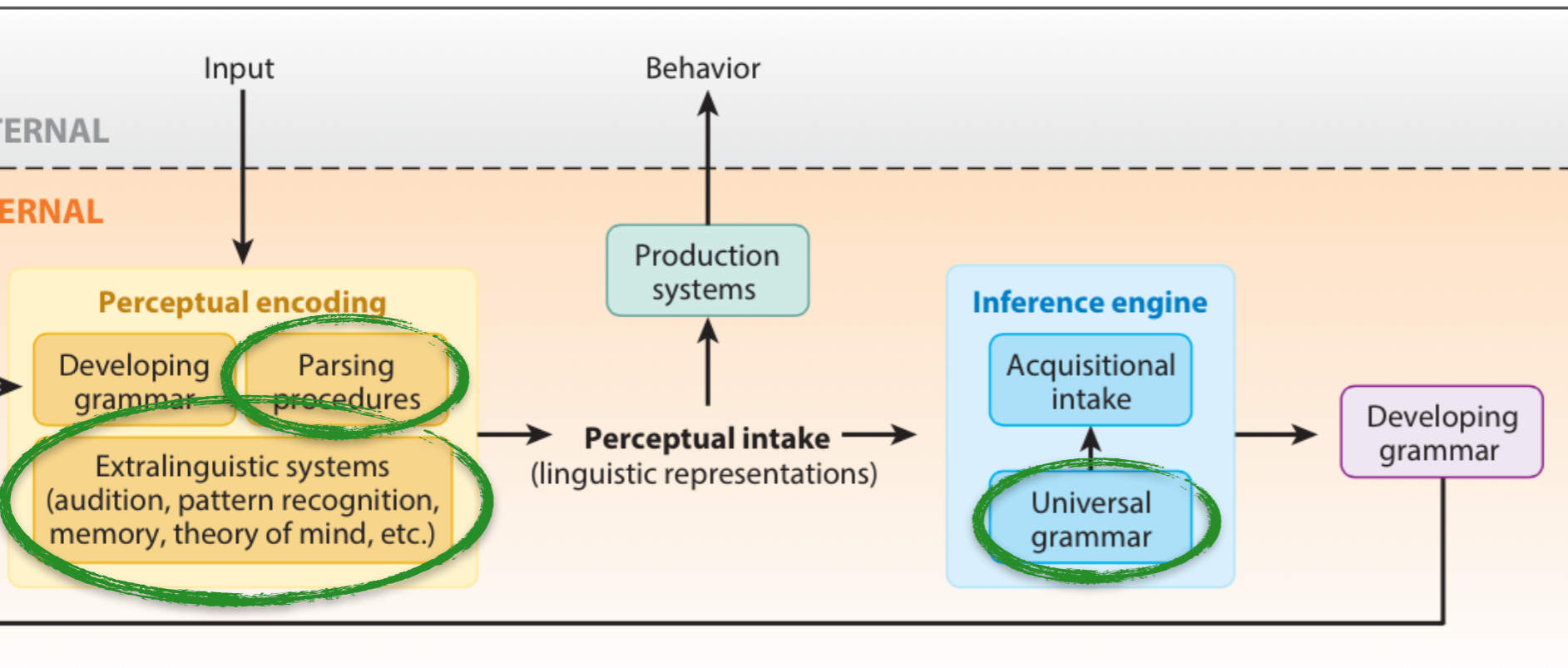
**Subjacency** (Chomsky 1973, Huang 1982, Lasnik & Saito 1984)

can't cross 2+ bounding nodes  
from a fixed set (CP, IP, and/or NP)



**Subjacency-ish** (Pearl & Sprouse 2013a, 2013b, 2015)

A dependency can't cross a very **low probability region** of structure



# Learning strategies

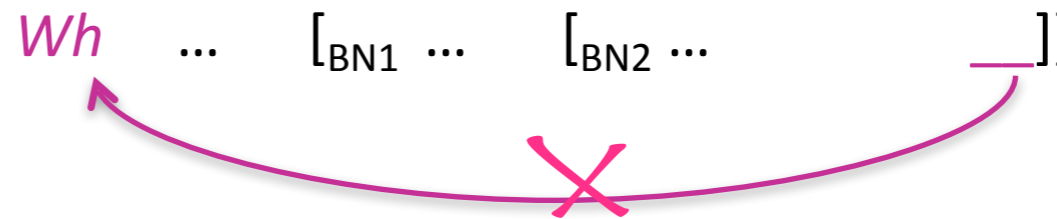


syntax

syntactic island

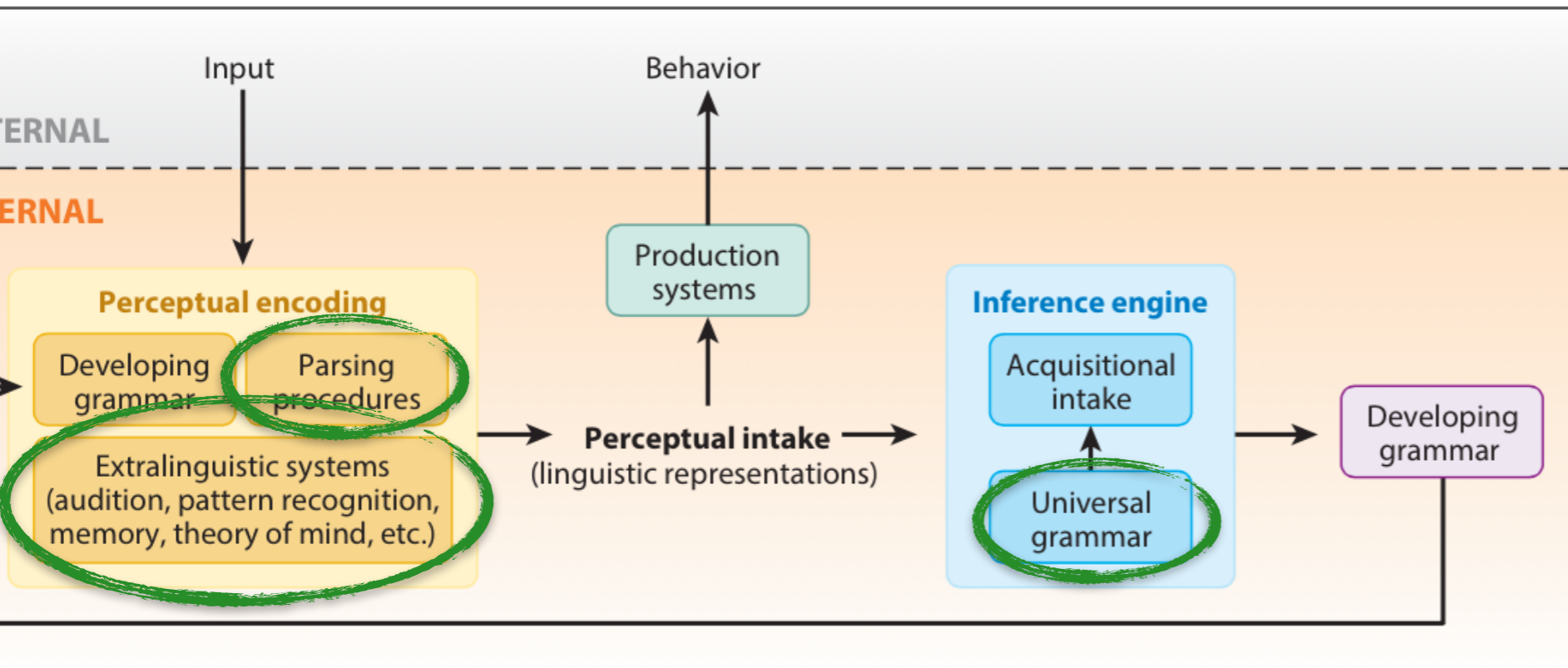
**Subjacency** (Chomsky 1973, Huang 1982, Lasnik & Saito 1984)

can't cross 2+ bounding nodes  
from a fixed set (CP, IP, and/or NP)



**Subjacency-ish** (Pearl & Sprouse 2013a, 2013b, 2015)

A dependency can't cross a very **low probability region** of structure  
Dependencies represented as a sequence of **container nodes**



# Container nodes



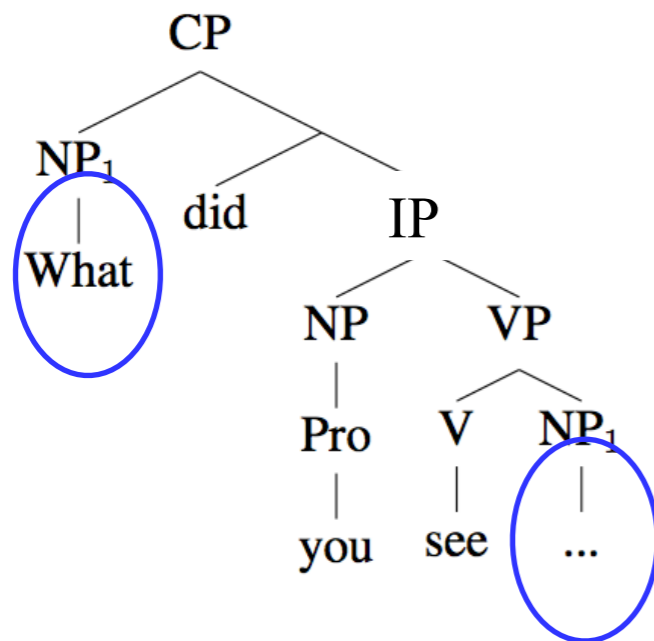
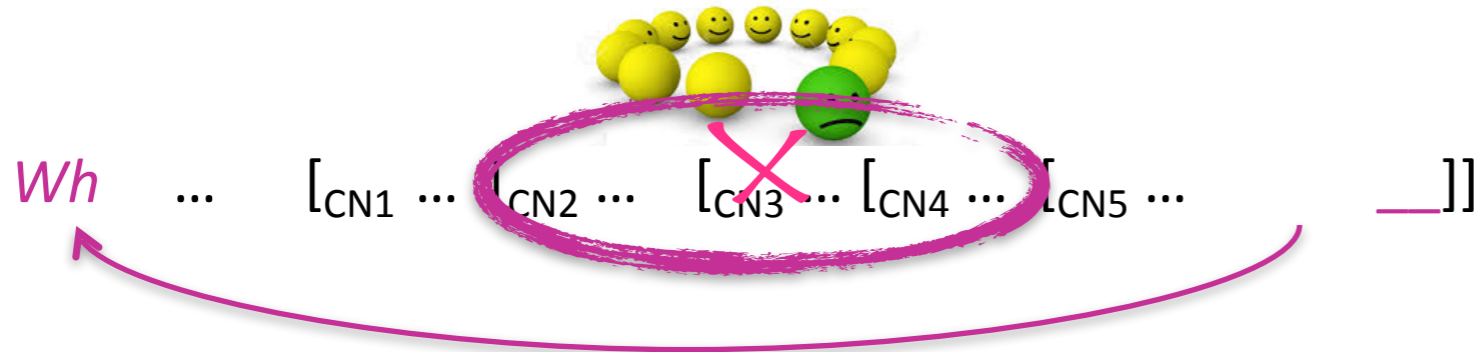
syntax

Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)

A dependency can't cross a very low probability region of structure

Dependencies represented as a sequence of **container nodes**

syntactic island



How to describe this dependency:

What phrases is the gap inside but the *wh*-word isn't inside?

# Container nodes



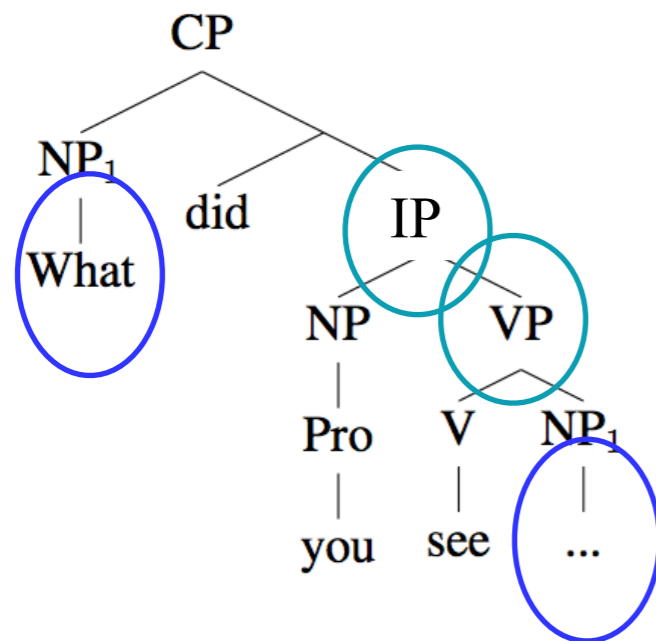
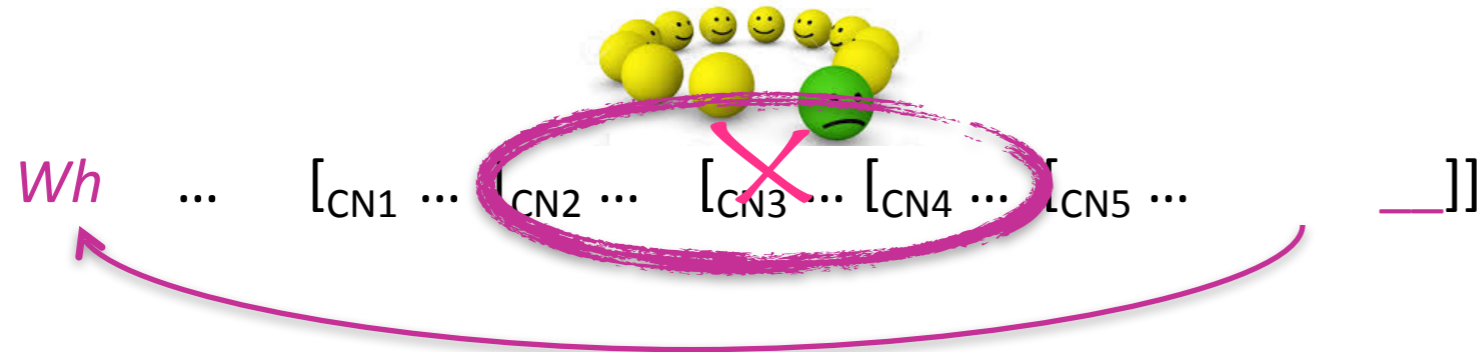
syntax

syntactic island

Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)

A dependency can't cross a very low probability region of structure

Dependencies represented as a sequence of **container nodes**



How to describe this dependency:

What phrases is the gap inside but the *wh*-word isn't inside?

What did you see \_\_\_?

= What did [IP you [VP see \_\_\_]]?

= IP-VP

# Container nodes



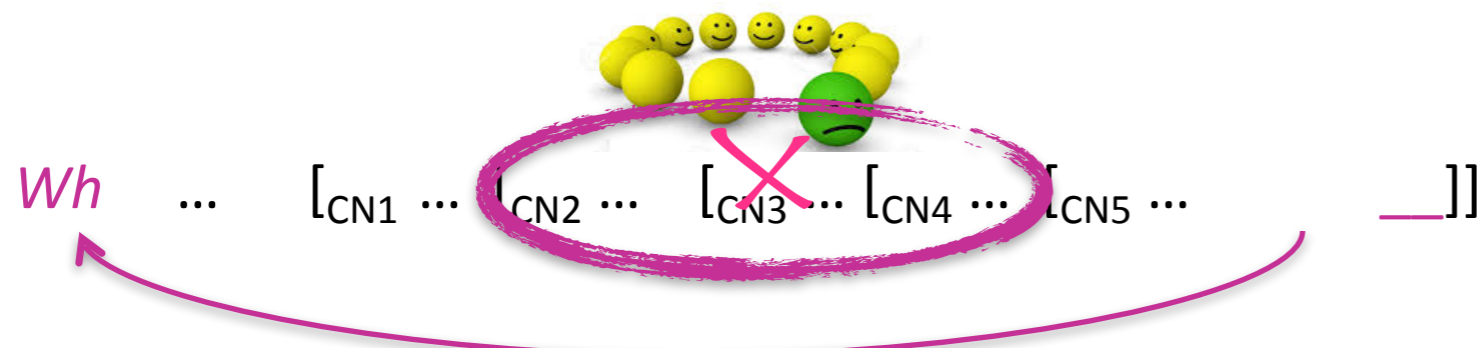
syntax

syntactic island

Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)

A dependency can't cross a very low probability region of structure

Dependencies represented as a sequence of **container nodes**



What did you see \_\_\_?

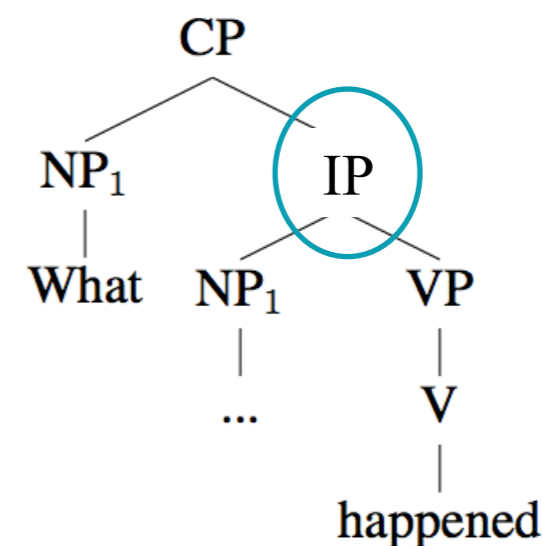
= What did [IP you [VP see \_\_\_]]?

= IP-VP

What \_\_\_ happened?

= What [IP \_\_\_ happened]?

= IP



# Container nodes



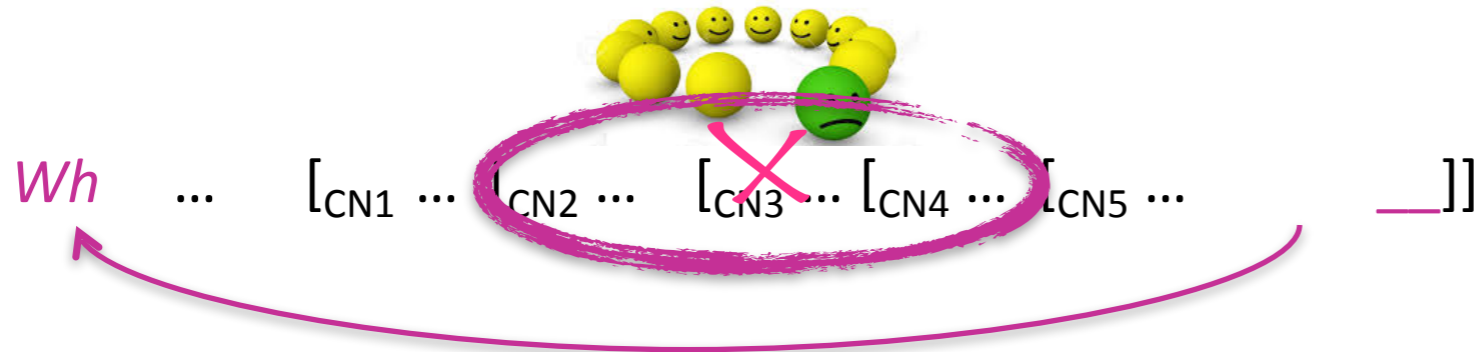
syntax

syntactic island

Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)

A dependency can't cross a very low probability region of structure

Dependencies represented as a sequence of **container nodes**



What did you see \_\_\_?

= What did [IP you [VP see \_\_\_]]?

= IP-VP

What \_\_\_ happened?

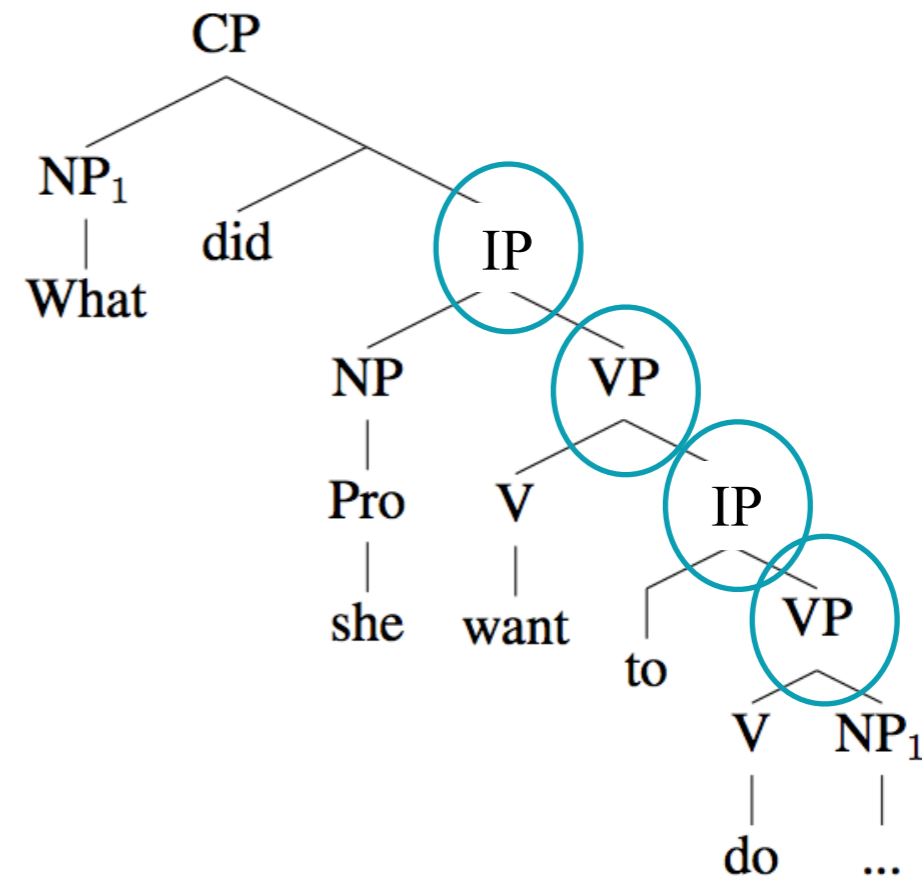
= What [IP \_\_\_ happened]?

= IP

What did she want to do \_\_\_?

= What did [IP she [VP want [IP to [VP do \_\_\_]]]]?

= IP-VP-IP-VP





# Container nodes



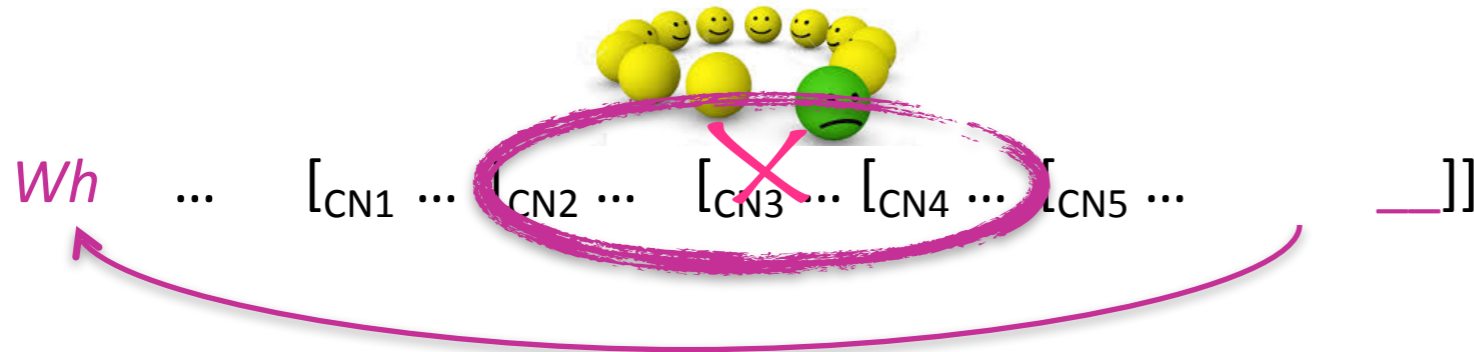
syntax

Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)

A dependency can't cross a very low probability region of structure

syntactic island

Dependencies represented as a sequence of **container nodes**

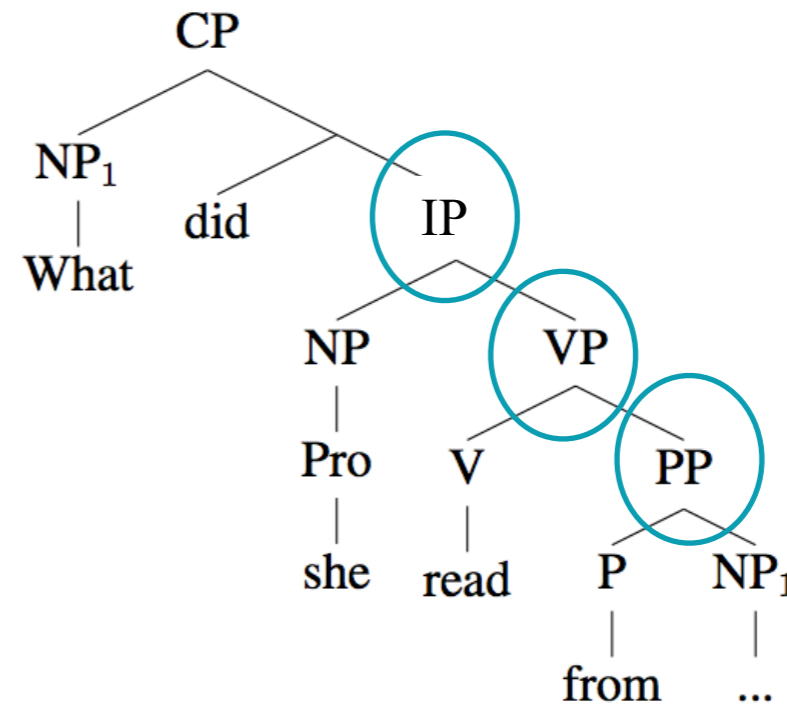


What did you see \_\_\_?  
= What did [IP you [VP see \_\_\_]]?  
= IP-VP

What \_\_\_ happened?  
= What [IP \_\_\_ happened]?  
= IP

What did she want to do \_\_\_?  
= What did [IP she [VP want [IP to [VP do \_\_\_]]]]?  
= IP-VP-IP-VP

What did she read from \_\_\_?  
= What did [IP she [VP read [PP from \_\_\_]]]]?  
= IP-VP-PP



# Learning strategies

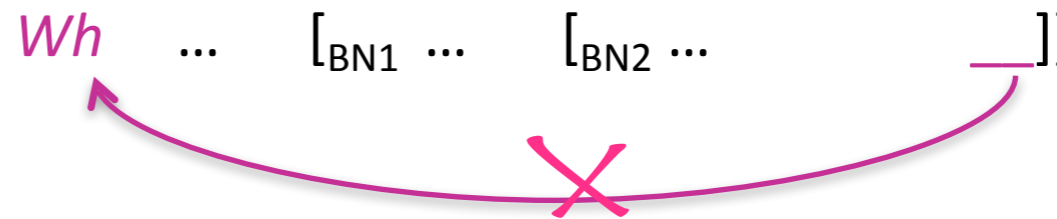


syntax

syntactic island

**Subjacency** (Chomsky 1973, Huang 1982, Lasnik & Saito 1984)

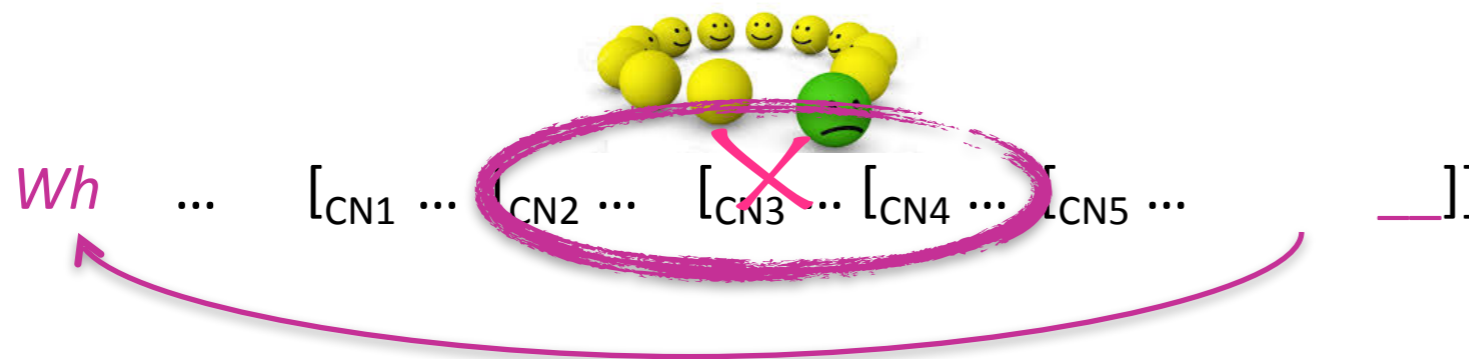
can't cross 2+ bounding nodes  
from a fixed set (CP, IP, and/or NP)



**Subjacency-ish** (Pearl & Sprouse 2013a, 2013b, 2015)

A dependency can't cross a very **low probability region** of structure

Dependencies represented as a sequence of **container nodes**



**Container node**: phrase structure node that contains dependency



# Learning strategies

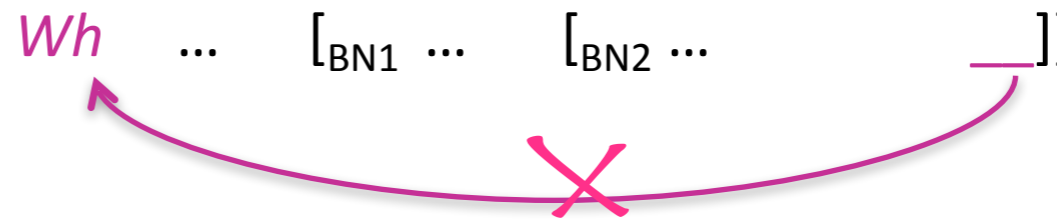


syntax

syntactic island

**Subjacency** (Chomsky 1973, Huang 1982, Lasnik & Saito 1984)

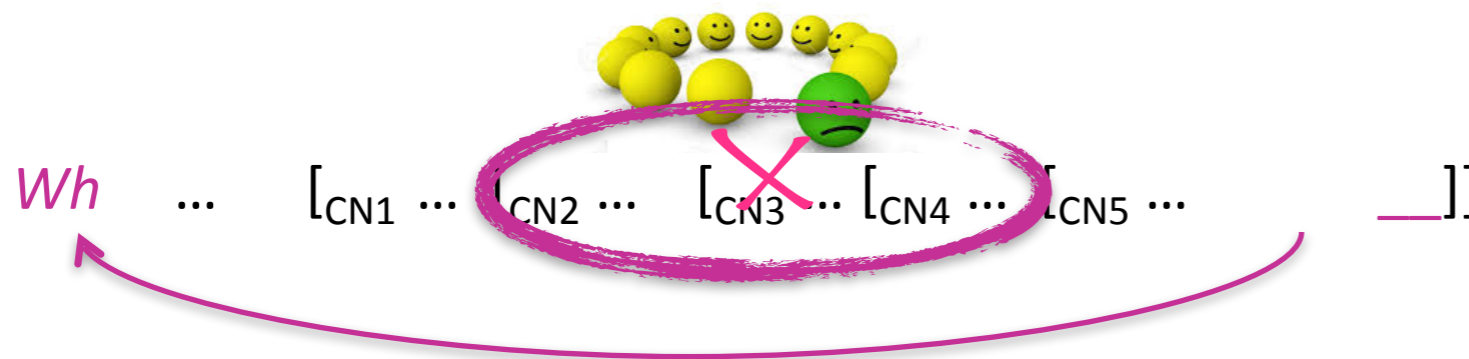
can't cross 2+ bounding nodes  
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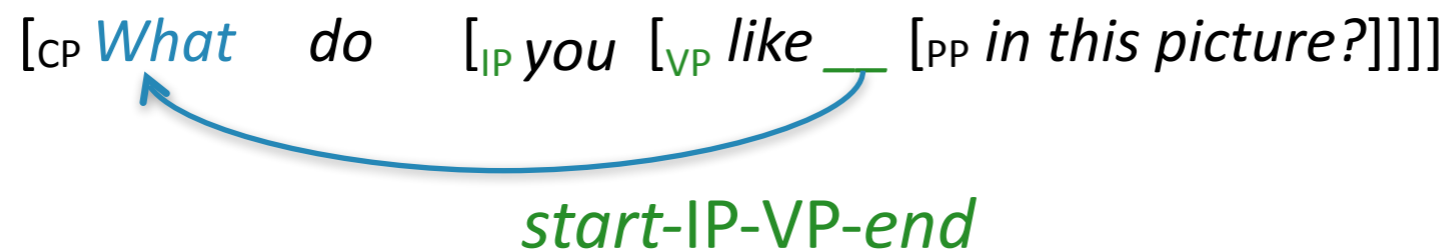
**Subjacency-ish** (Pearl & Sprouse 2013a, 2013b, 2015)

A dependency can't cross a very **low probability region** of structure

Dependencies represented as a sequence of **container nodes**



Sequence of container nodes characterizes dependencies



# Learning strategies

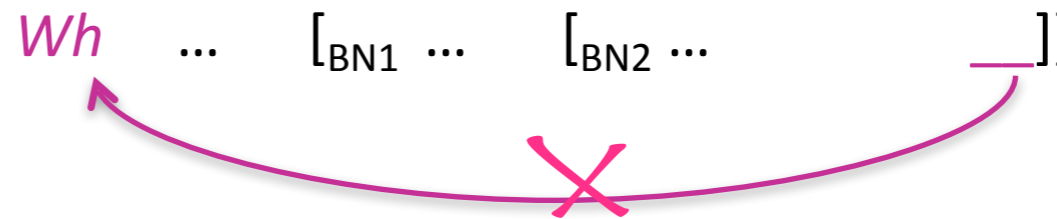


syntax

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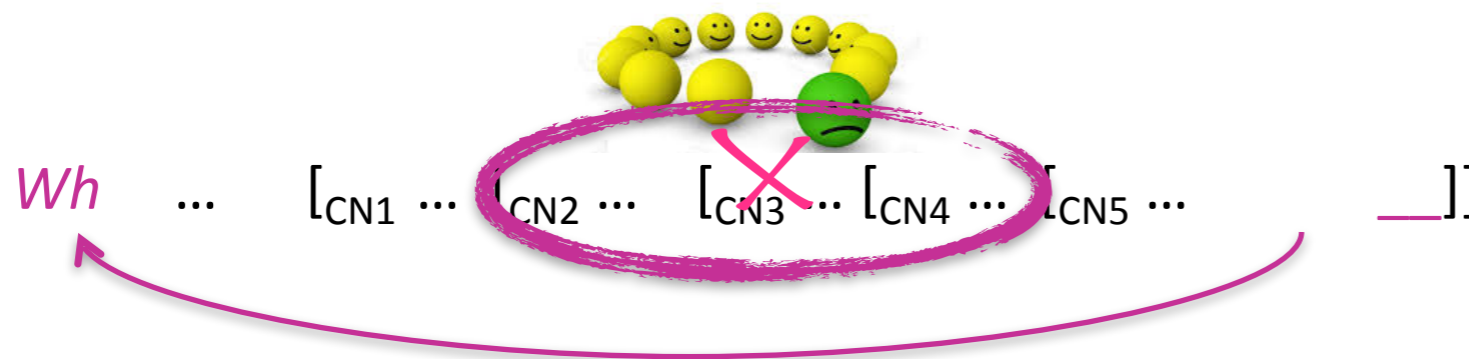
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**Subjacency-ish** (Pearl & Sprouse 2013a, 2013b, 2015)

A dependency can't cross a very **low probability region of structure**

Dependencies represented as a sequence of **container nodes**



Ungrammatical dependencies have low probability segments



# Learning strategies

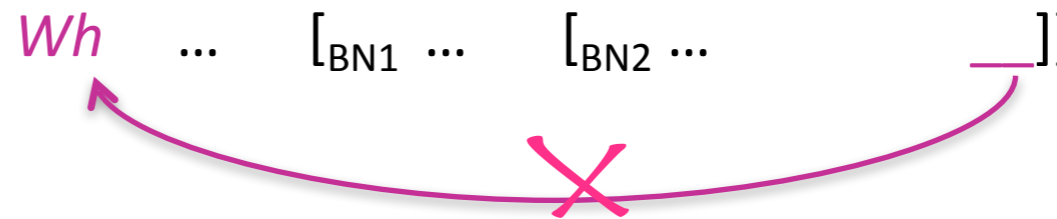


syntax

syntactic island

**Subjacency** (Chomsky 1973, Huang 1982, Lasnik & Saito 1984)

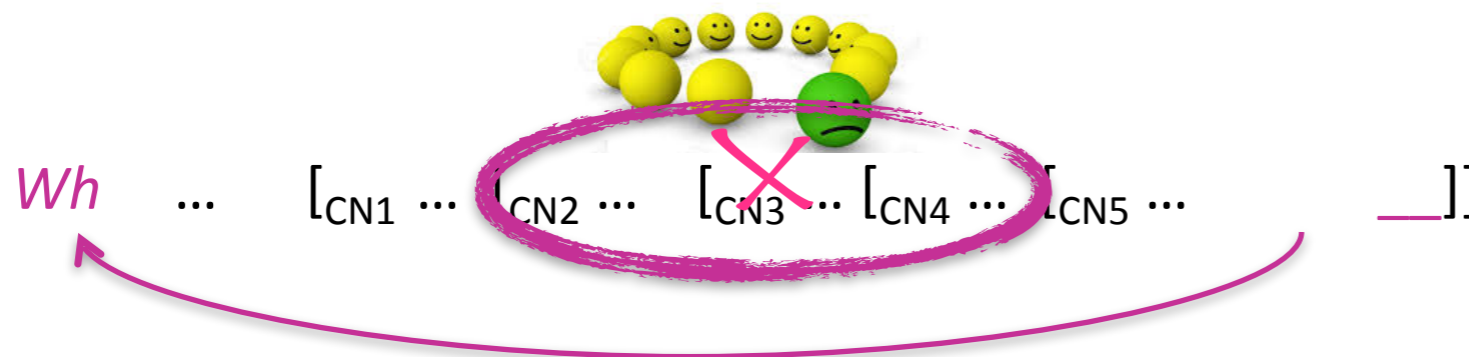
can't cross 2+ bounding nodes  
from a fixed set (CP, IP, and/or NP)



**Subjacency-ish** (Pearl & Sprouse 2013a, 2013b, 2015)

A dependency can't cross a very **low probability region of structure**

Dependencies represented as a sequence of **container nodes**



**Low probability container node sequences** have to be learned for the language

# Learning strategies

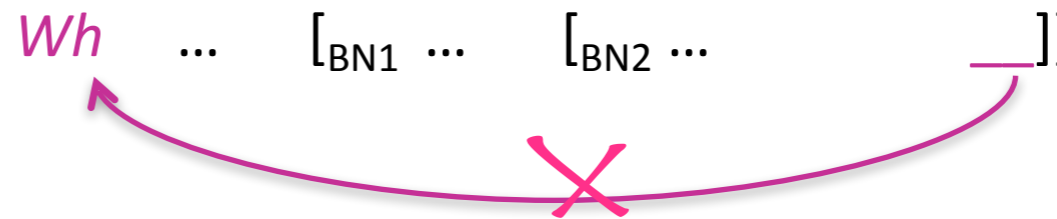


syntax

syntactic island

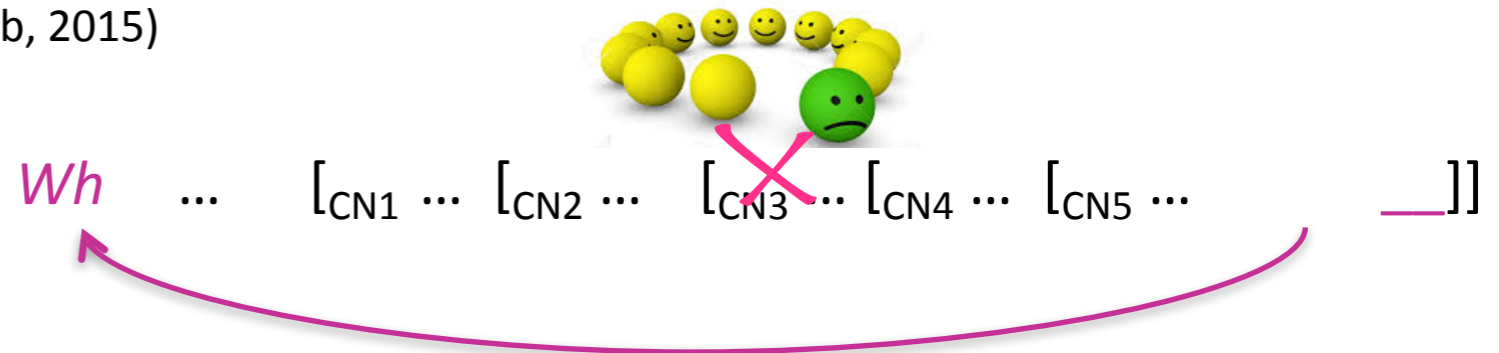
**Subjacency** (Chomsky 1973, Huang 1982, Lasnik & Saito 1984)

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**Subjacency-ish** (Pearl & Sprouse 2013a, 2013b, 2015)

A dependency can't cross a very  
low probability sequence of  
container nodes



**In common: Local structural anomaly is the problem**

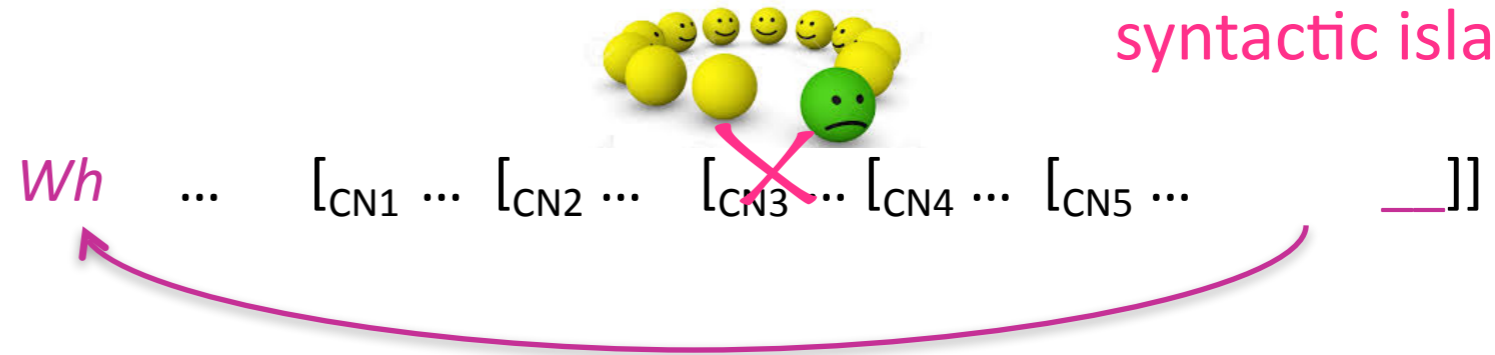
# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island

A dependency can't cross a very low probability sequence of container nodes



Implemented in an **algorithmic-level** learning model that learned from **realistic samples of child-directed speech**.



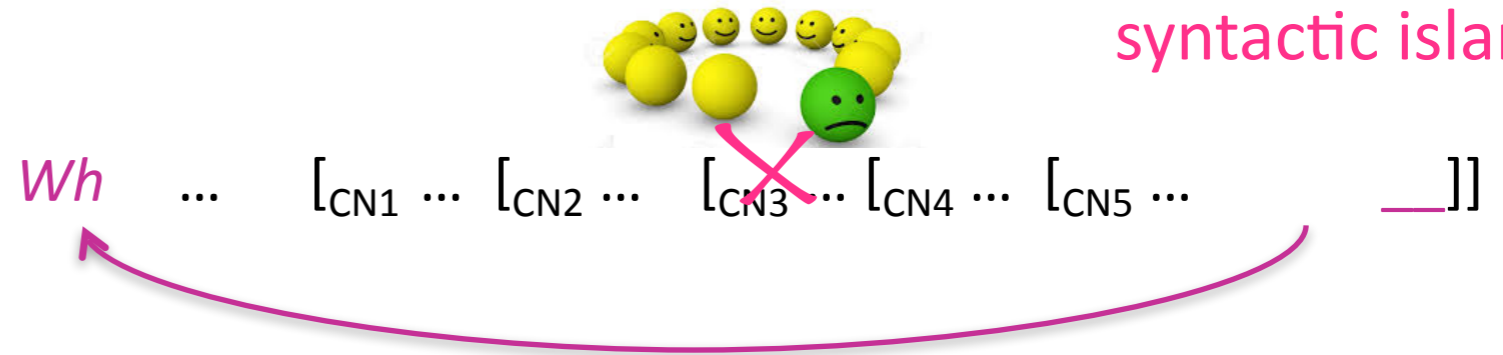
# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island

A dependency can't cross a very low probability sequence of container nodes



Intuition: Learn what you can from the dependencies you do actually observe in the data and apply it to make a judgment about the dependencies you haven't seen before, like these syntactic islands.

EXTERNAL

Input

Behavior

INTERNAL



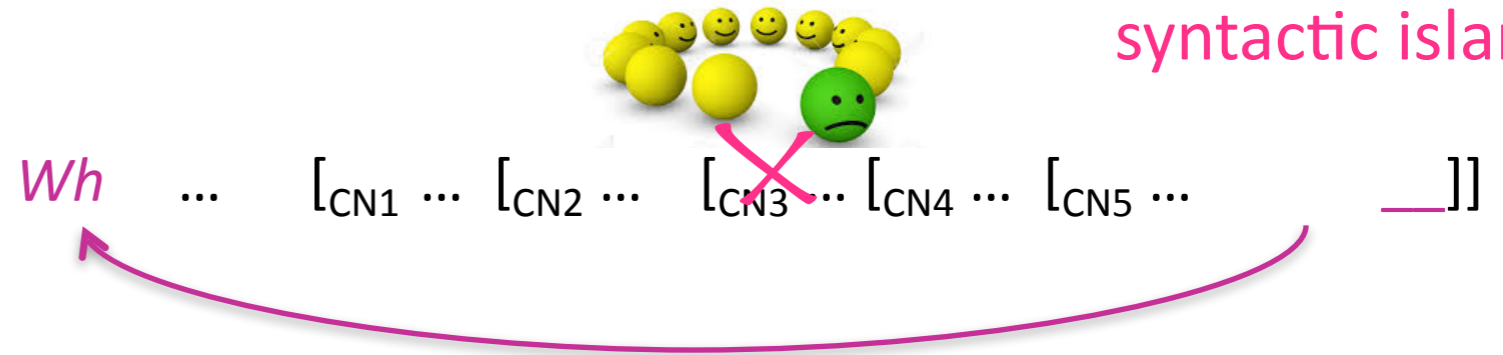
# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island

A dependency can't cross a very low probability sequence of container nodes



Intuition: Learn what you can from the dependencies you do actually observe in the data and apply it to make a judgment about the dependencies you haven't seen before, like these syntactic islands.

That is, leverage a broader set of data to make syntactic generalizations.

EXTERNAL

Input

Behavior

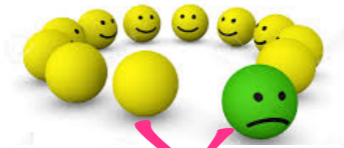
INTERNAL

# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [~~CN3~~ ... [CN4 ... [CN5 ... ]]]]



What information is there to leverage exactly?

Input

Behavior

EXTERNAL

INTERNAL

# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island

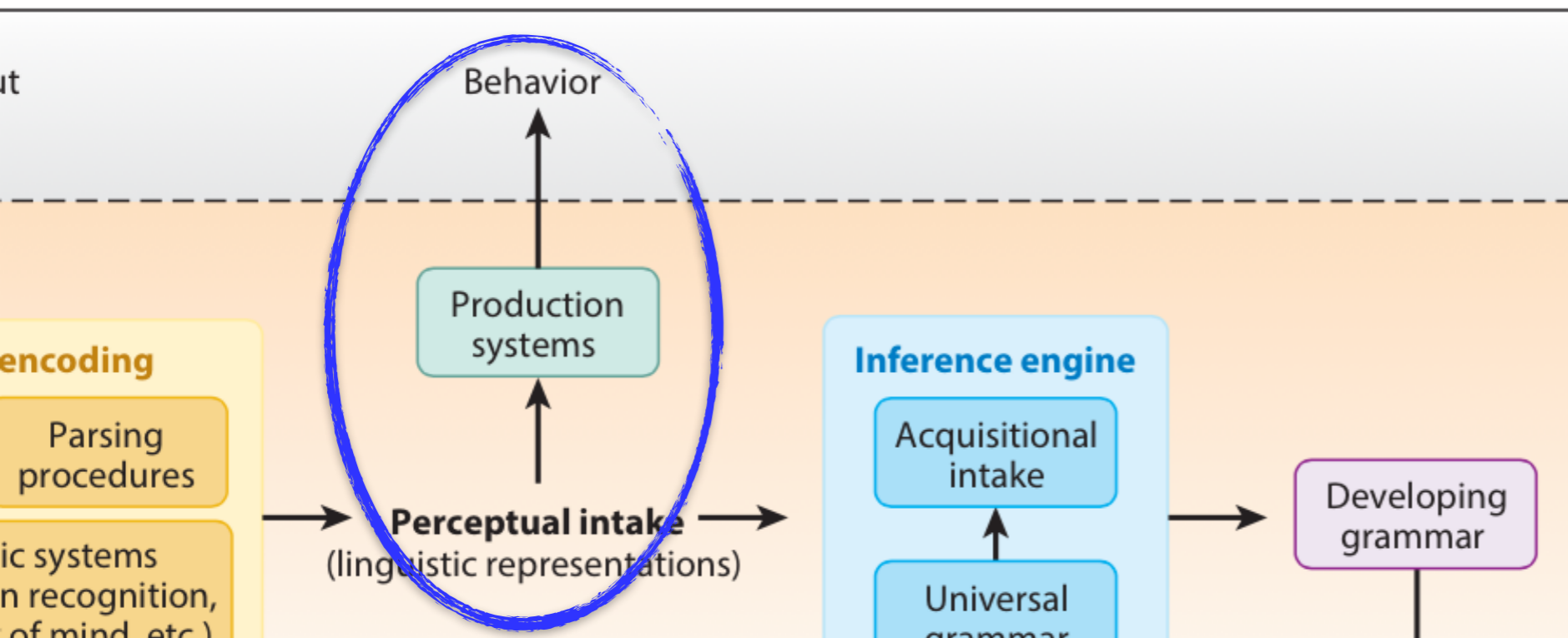


Wh ... [CN1 ... [CN2 ... [~~CN3~~ ... [CN4 ... [CN5 ... ]]]]



What information is there to leverage exactly?

This relates to the strategy children use for learning and then generating predictions about the grammaticality of dependencies.

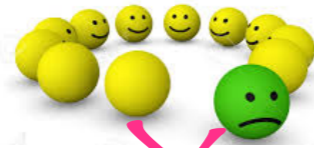


# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]]]]

What information is there to leverage exactly?

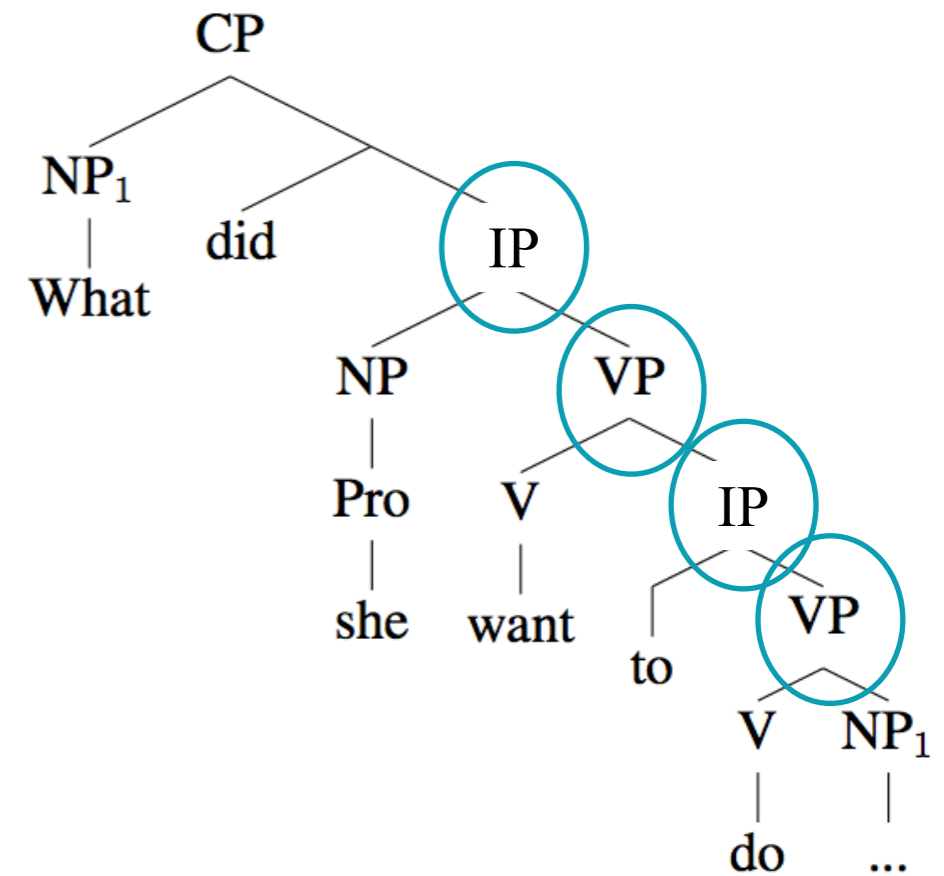
## Strategy

(1) Pay attention to the structure of dependencies.

What did she want to do \_\_\_ ?

= What did [IP she [VP want [IP to [VP do \_\_\_]]]]?

= IP-VP-IP-VP

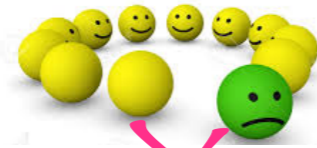


# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]

What information is there to leverage exactly?

## Strategy

(1) Pay attention to dependency structure.

(2) Break these dependency structures into smaller pieces made up of three units (trigrams) that you can track the frequency of in the input you encounter.

IP-VP =

*begin-IP-VP*

*IP-VP-end*

IP =

*begin-IP-end*

IP-VP-IP-VP

= *begin-IP-VP*

*IP-VP-IP*

*VP-IP-VP*

*IP-VP-end*

IP-VP-PP

= *begin-IP-VP*

*IP-VP-PP*

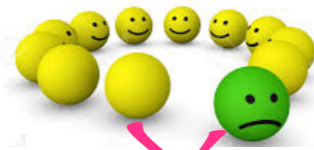
*VP-PP-end*

# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]]

What information is there to leverage exactly?

## Strategy

(1) Pay attention to dependency structure.

(2) Break these dependency structures into smaller pieces made up of three units (**trigrams**) that you can track the frequency of in the input you encounter.

IP-VP =  
begin-IP-VP  
IP-VP-end

IP =  
begin-IP-end

begin-IP-VP = 86/225  
IP-VP-end = 83/225  
begin-IP-end = 13/225

IP-VP-IP-VP  
= begin-IP-VP

IP-VP-PP  
= begin-IP-VP

IP-VP-IP = 6/225  
VP-IP-VP = 6/225

IP-VP-IP

IP-VP-PP

IP-VP-PP = 3/225

VP-IP-VP

VP-PP-end

VP-PP-end = 3/225

IP-VP-end

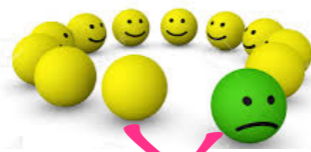
...

# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]]

What information is there to leverage exactly?

## Strategy

(1) Pay attention to dependency structure.

(2) Break these dependency structures into smaller pieces made up of three units (trigrams) that you can track the frequency of in the input you encounter.

IP-VP =

*begin-IP-VP*

*IP-VP-end*

IP-VP-IP-VP

= *begin-IP-VP*

IP-VP-IP

VP-IP-VP

*IP-VP-end*

IP =

*begin-IP-end*

IP-VP-PP

= *begin-IP-VP*

IP-VP-PP

VP-PP-end

*begin-IP-VP* = 86/225

*IP-VP-end* = 83/225

*begin-IP-end* = 13/225

IP-VP-IP = 6/225

VP-IP-VP = 6/225

IP-VP-PP = 3/225

VP-PP-end = 3/225

...

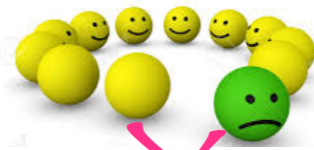
Note that some of these trigrams appear in multiple dependencies that commonly occur in children's input. This will be helpful!

# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



*Wh* ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]

What information is there to leverage exactly?

## Strategy

- (1) Pay attention to dependency structure.
- (2) Break dependency structures into **trigrams** that you can track the frequency of.
- (3) Use trigram frequency to calculate the **probability of that trigram** occurring in a dependency.

$$\textit{begin-IP-VP} = 86/225$$

$$p(\textit{begin-IP-VP}) = 0.38$$

$$\textit{IP-VP-end} = 83/225$$

$$p(\textit{IP-VP-end}) = 0.37$$

$$\textit{begin-IP-end} = 13/225$$

$$p(\textit{begin-IP-end}) = 0.06$$

$$\textit{IP-VP-IP} = 6/225$$

$$p(\textit{IP-VP-IP}) = 0.03$$

$$\textit{VP-IP-VP} = 6/225$$

$$p(\textit{VP-IP-VP}) = 0.03$$

$$\textit{IP-VP-PP} = 3/225$$

$$p(\textit{IP-VP-PP}) = 0.01$$

$$\textit{VP-PP-end} = 3/225$$

$$p(\textit{VP-PP-end}) = 0.01$$

...

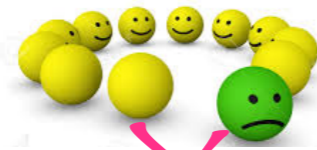


# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]

What information is there to leverage exactly?

## Strategy

- (1) Pay attention to dependency structure.
- (2) Break dependency structures into **trigrams** that you can **track the frequency** of.
- (3) Calculate the **trigram probability** in a dependency.
- (4) When you see a **new dependency**, break it down into its trigrams and then **calculate its probability, based on the trigram probabilities**.

What does Jack want \_\_\_?

= What does [IP Jack [VP want \_\_\_]]?

= IP-VP

= *begin-IP-VP*

*IP-VP-end*

$$p(\text{IP-VP}) = p(\textit{begin-IP-VP}) * p(\text{IP-VP-end})$$

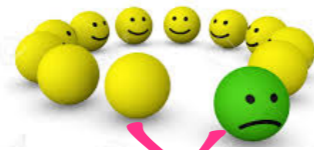
$$= 0.38 * 0.37 = 0.14$$

# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]

What information is there to leverage exactly?

## Strategy

- (1) Pay attention to dependency structure.
- (2) Break dependency structures into **trigrams** that you can **track the frequency** of.
- (3) Calculate the **trigram probability** in a dependency.
- (4) When you see a **new dependency**, break it down into its trigrams and then **calculate its probability, based on the trigram probabilities**.

What does Jack want to do that for \_\_\_?

= What does [IP Jack [VP want [IP to [VP do that [PP for \_\_\_]]]?

= IP-VP-IP-VP-PP

= *begin*-IP-VP

IP-VP-IP

VP-IP-VP

IP-VP-PP

VP-PP-*end*

$$p(\text{IP-VP-IP-VP-PP}) = p(\textit{begin}\text{-IP-VP}) * p(\text{IP-VP-IP}) * p(\text{VP-IP-VP}) * p(\text{IP-VP-PP}) * p(\text{VP-PP-}\textit{end})$$

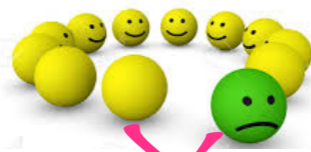
$$= 0.38 * 0.03 * 0.03 * 0.01 * 0.01 = 0.000000034$$

# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]

What information is there to leverage exactly?

## Strategy

- (1) Pay attention to dependency structure.
- (2) Break dependency structures into **trigrams** that you can **track the frequency** of.
- (3) Calculate the **trigram probability** in a dependency.
- (4) When you see a **new dependency**, break it down into its trigrams and then **calculate its probability, based on the trigram probabilities**.

### Subject island dependency

What do you think that the joke about \_\_\_ offended Jack?

= What do [IP you [VP think [CP that [IP [NP the joke [PP about \_\_\_]]]]]] offended Jack?

= IP-VP-CP-NP-PP

= *begin*-IP-VP

IP-VP-CP

VP-CP-IP

CP-IP-NP

IP-NP-PP

NP-PP-*end*

$$p(\text{IP-VP-CP-IP-NP-PP}) = p(\textit{begin}\text{-IP-VP}) * p(\text{IP-VP-CP}) * p(\text{VP-CP-S}) * p(\text{CP-IP-NP}) * p(\text{IP-NP-PP}) * p(\text{NP-PP-}\textit{end})$$

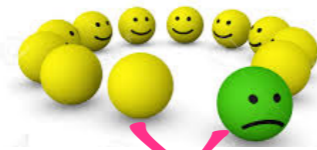
$$= 0.86 * 0.01 * 0.001 * 0.00 * 0.00 * 0.02 = 0.00$$

# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]

What information is there to leverage exactly?

## Strategy

- (1) Pay attention to dependency structure.
- (2) Break dependency structures into **trigrams** that you can **track the frequency** of.
- (3) Calculate the **trigram probability** in a dependency.
- (4) Break a **new dependency** into its trigrams and **calculate its probability**.
- (5) Use calculated dependency probabilities as the **basis for grammaticality judgments**. **Lower probability dependencies are dispreferred**, compared to **higher probability dependencies**.



$$p(\text{IP-VP}) = 0.14$$

$$p(\text{IP-VP-IP-VP-PP}) = 0.000000034$$



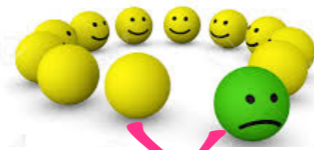
$$p(\text{IP-VP-CP-IP-NP-PP}) = 0.00$$

# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

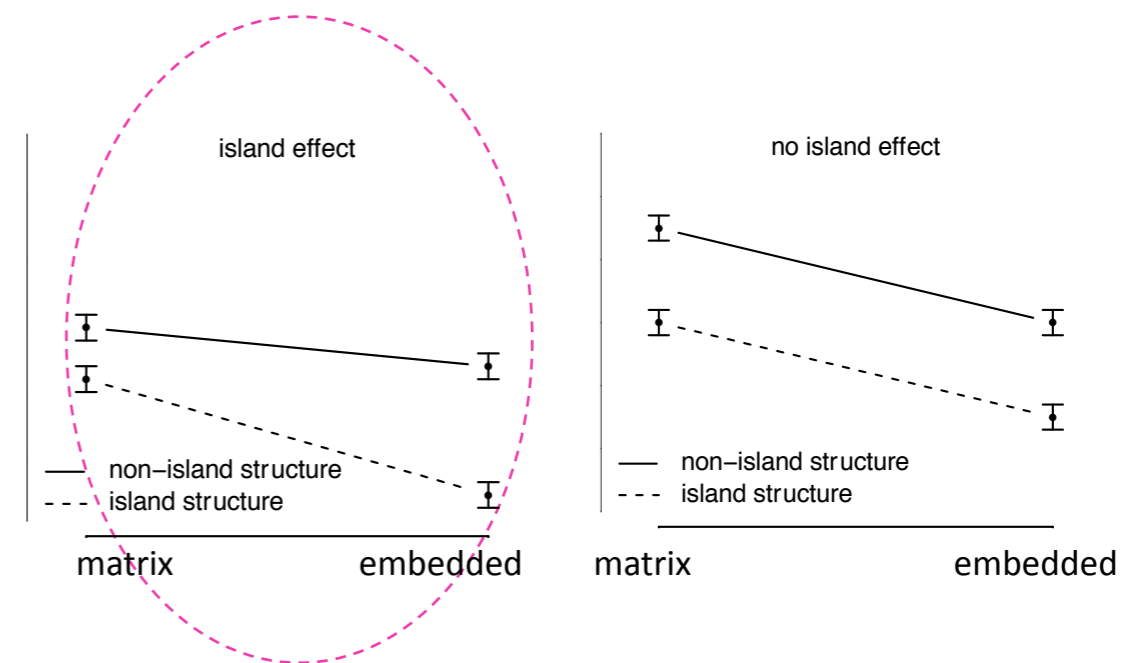
syntactic island



Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]]]

Use calculated dependency probabilities as the **basis for grammaticality judgments**. **Lower probability dependencies are dispreferred**, compared to **higher probability dependencies**.

For each set of island stimuli from Sprouse et al. (2012), we generate grammaticality preferences for the modeled learner based on the **dependency's perceived probability** and use this as a stand-in for acceptability.



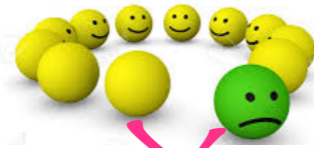
Looking for **superadditivity** as a sign of syntactic island knowledge

# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... \_\_\_]]]]

Use calculated dependency probabilities as the basis for grammaticality judgments. Lower probability dependencies are dispreferred, compared to higher probability dependencies.



non-island

Who \_\_\_ claimed that Lily forgot the necklace?

What did the teacher claim that Lily forgot \_\_\_?



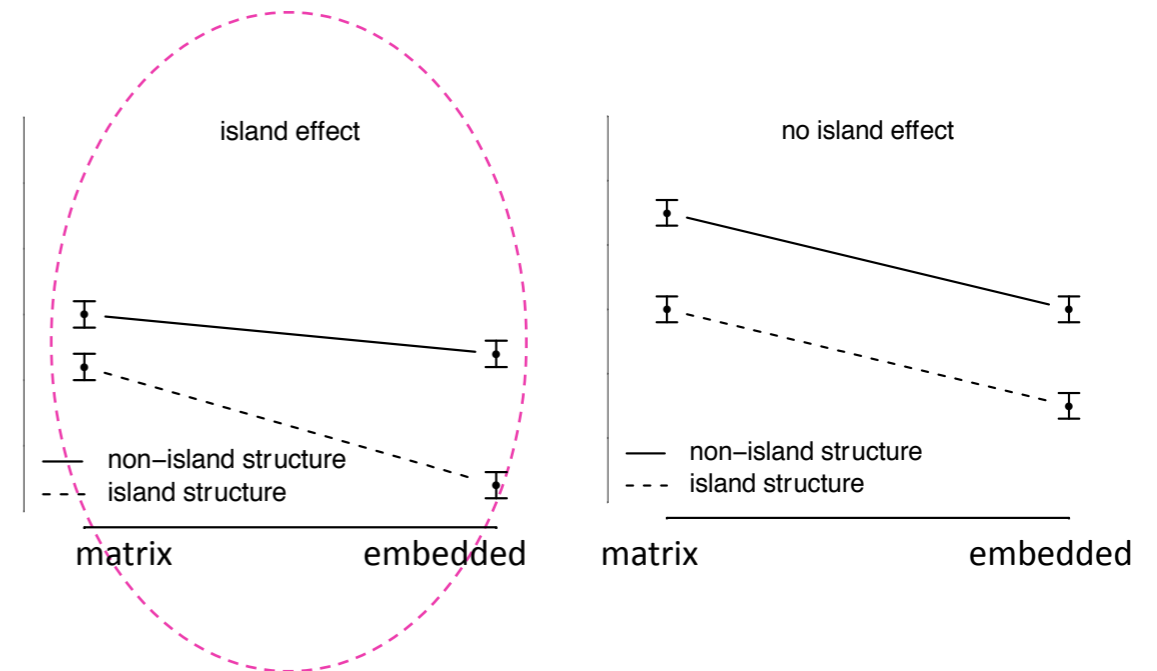
island

Who \_\_\_ made the claim that Lily forgot the necklace?

\*What did the teacher make the claim that Lily forgot \_\_\_?

matrix

embedded



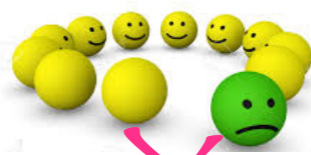
Looking for **superadditivity** as a sign of syntactic island knowledge

# Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



*Wh* ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]]]]

Use calculated dependency probabilities as the basis for grammaticality judgments. Lower probability dependencies are dispreferred, compared to higher probability dependencies.

non-island



*IP*



*IP-VP-CP<sub>that</sub>-IP-VP*



*IP*

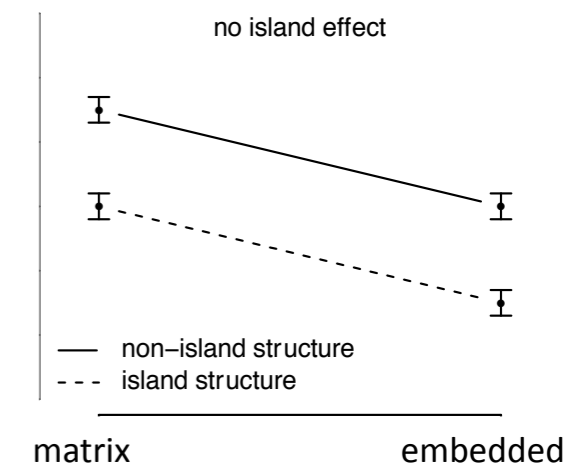
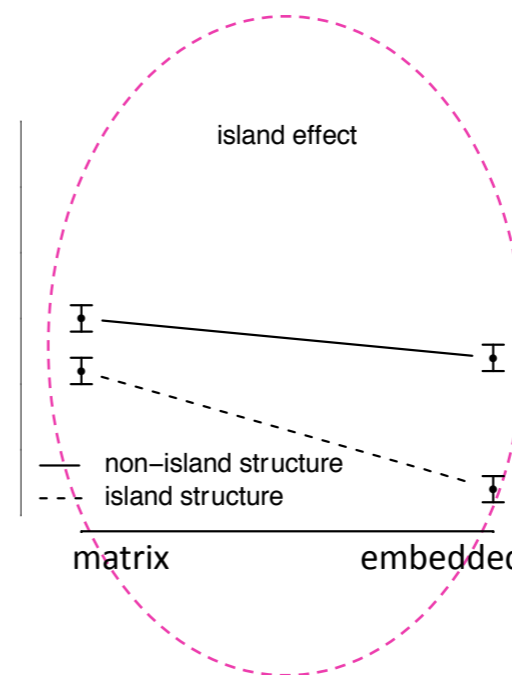


\**IP-VP-NP-CP<sub>that</sub>-IP-VP*

island

matrix

embedded



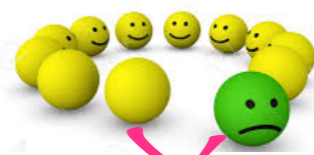
Each dependency is characterized by a container node sequence, whose probability can be calculated and then plotted.

# ✓ Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



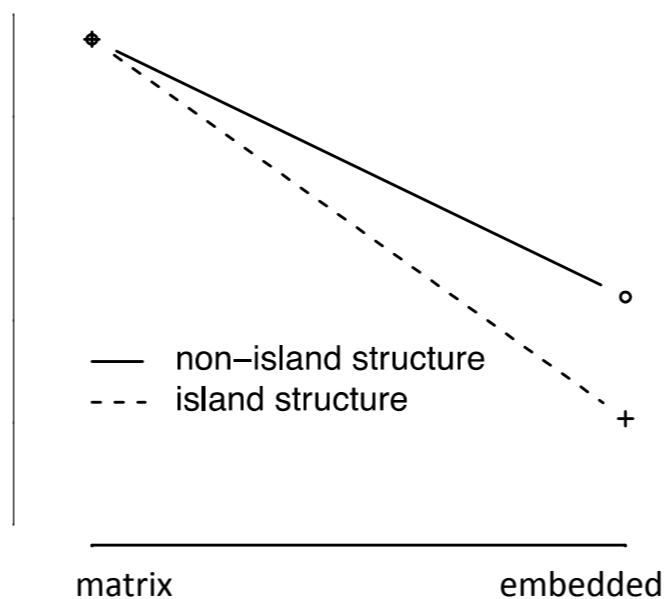
Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]]]

Superadditivity observed for all four islands — the qualitative behavior suggests that this learner has knowledge of these syntactic islands.

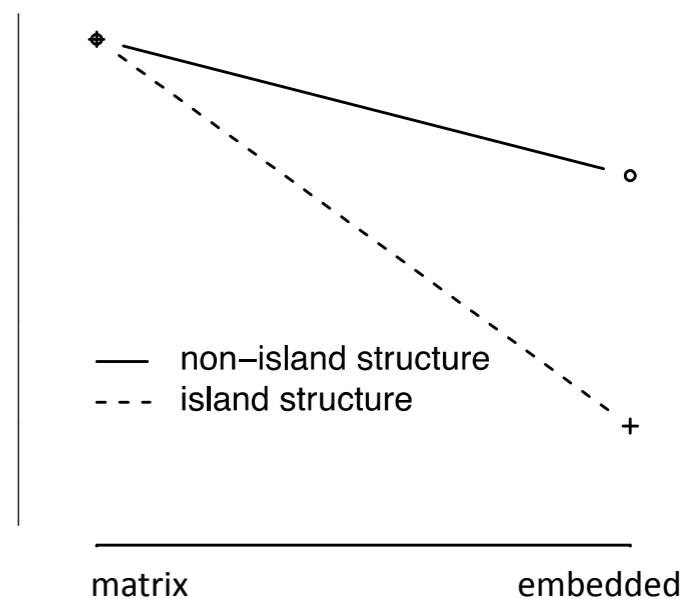
The Subjacency-ish representation that relies on container node trigram probabilities can solve this learning problem using this learning strategy.



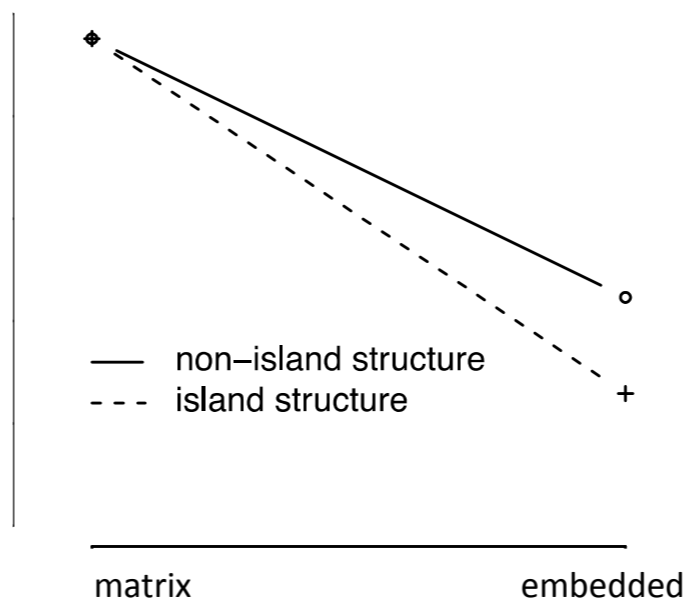
## Complex NP



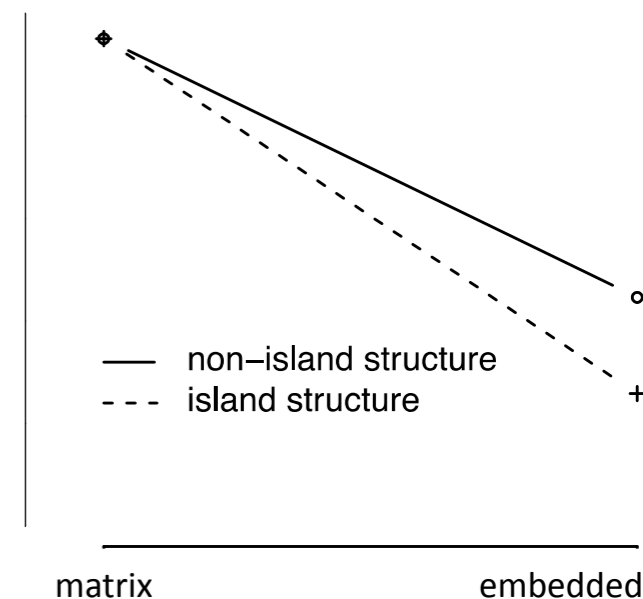
## Subject



## Whether



## Adjunct



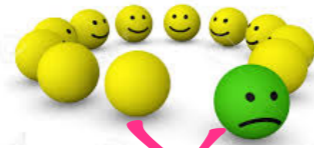


# ✓ Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island

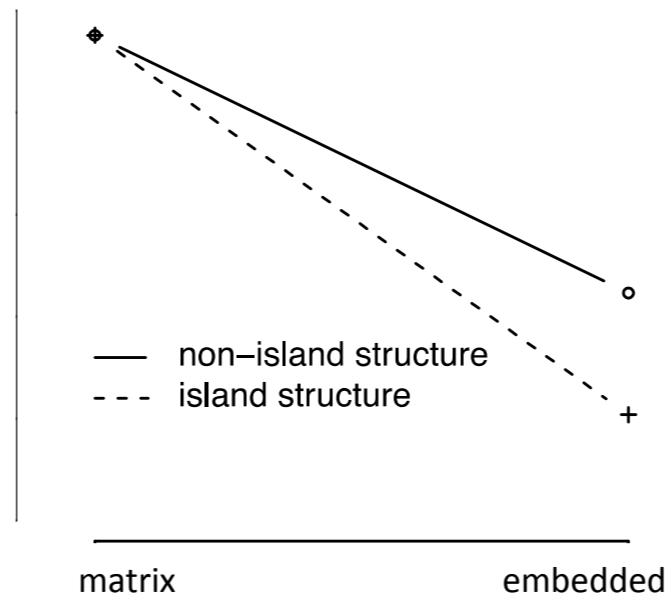


Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]]]

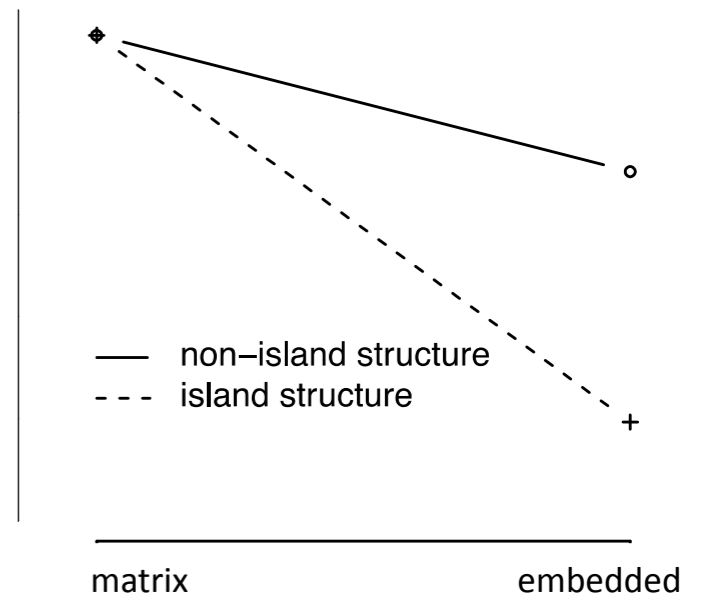


Note: We're careful to say "qualitative" behavior fit because there are lots of other factors that impact acceptability judgment behavior, and we've only modeled one (presumably) large part of them, which is the grammaticality of the dependency.

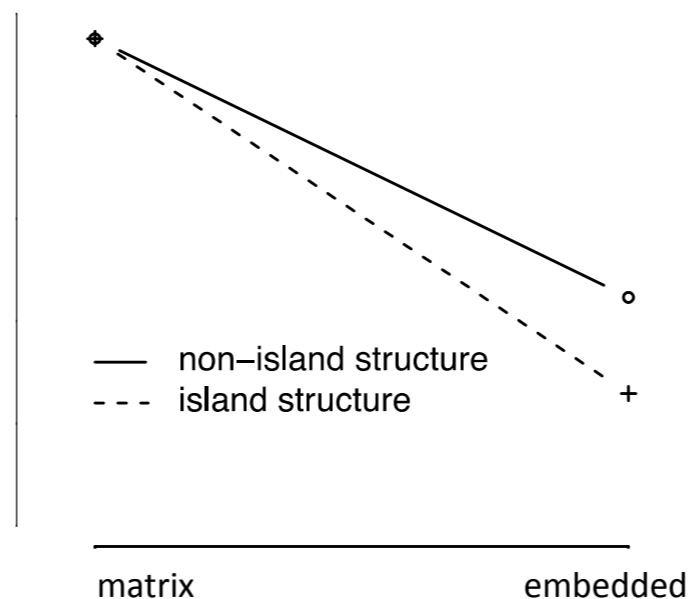
## Complex NP



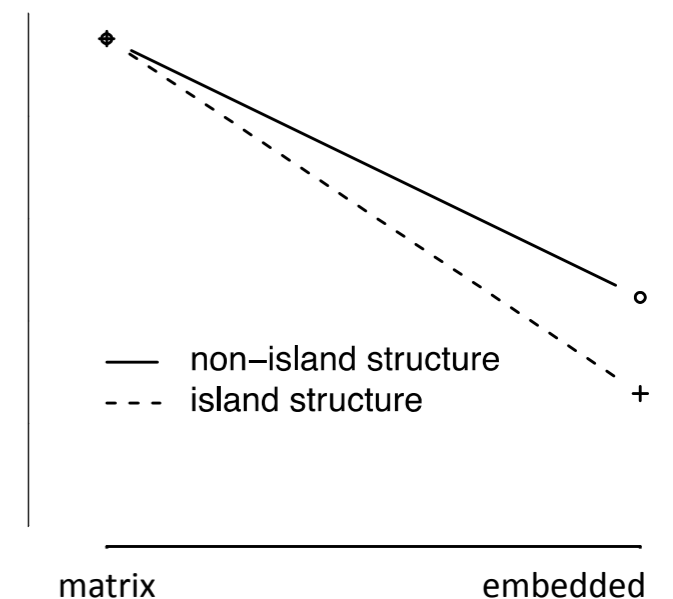
## Subject



## Whether



## Adjunct

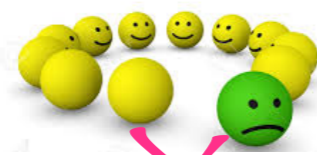


# ✓ Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



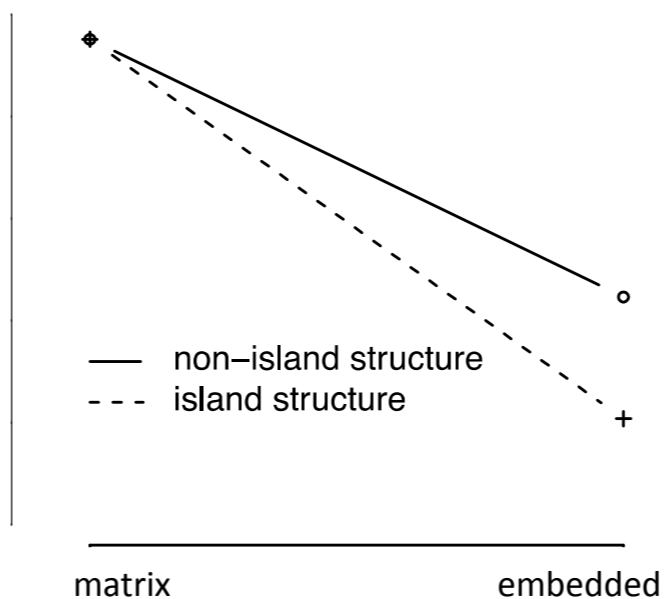
Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]]]

But is this all we can say?

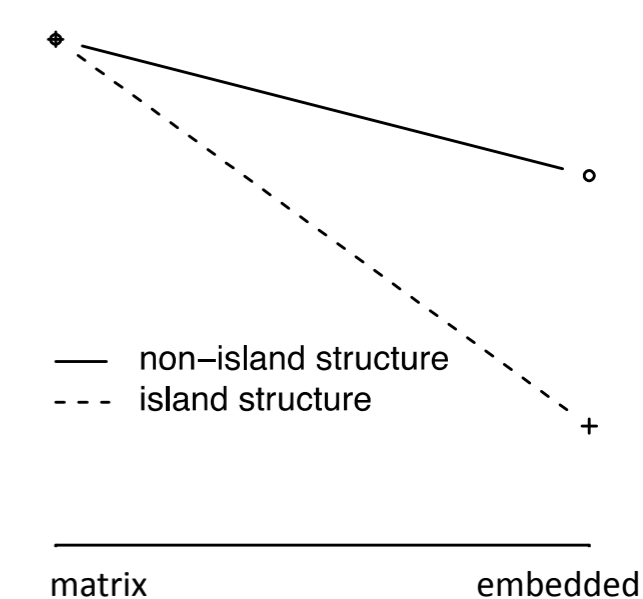
No! One useful aspect of models is that we can look inside the modeled child to see *why* it's behaving the way that it is. (This is something that's harder to do with real children — that is, opening up their minds and seeing how they work.)



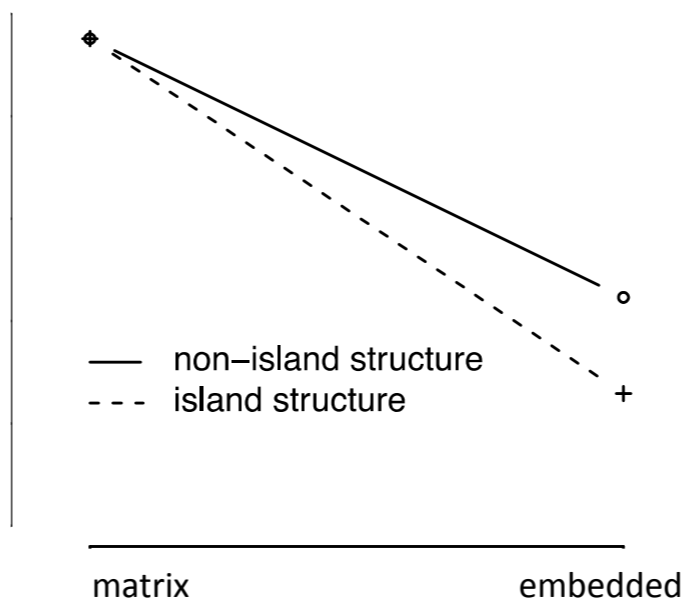
## Complex NP



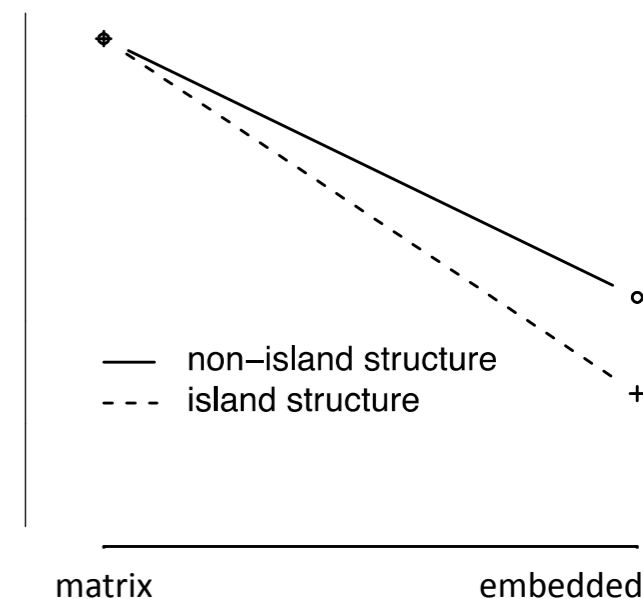
## Subject



## Whether



## Adjunct

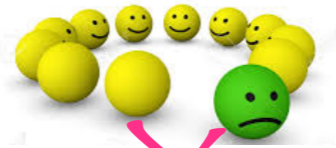


# ✓ Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [~~CN3~~ ... [CN4 ... [CN5 ... ]]]]



## What's going on?

Why are the island-spanning dependencies so much worse than the grammatical ones?

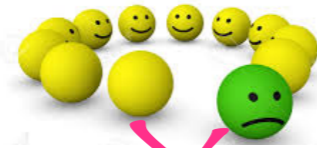


# ✓ Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [~~CN3~~ ... [CN4 ... [CN5 ... ]]]]



## What's going on?

Why are the island-spanning dependencies so much worse than the grammatical ones?

Let's look inside them and see!

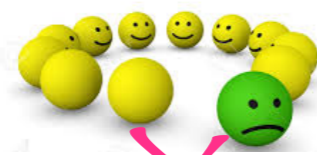


# ✓ Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]]]



Let's look inside them and see!

It turns out that each island-spanning dependency contains **at least one very low probability container node trigram**. So these are the **relevant "island" representations**.

a. Complex NP

(i) \* What did [<sub>IP</sub> the teacher [<sub>VP</sub> make [<sub>NP</sub> the claim <sub>CP<sub>that</sub></sub> that [<sub>IP</sub> Lily <sub>VP</sub> forgot \_\_ ]]]]]?

(ii) *start-IP-VP-NP-CP<sub>that</sub>-IP-VP-end*

(iii) Low probability:

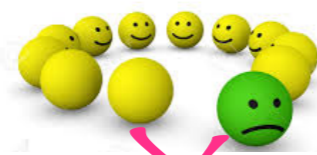
VP-NP-CP<sub>that</sub>  
NP-CP<sub>that</sub>-IP

# ✓ Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]



Let's look inside them and see!

It turns out that each island-spanning dependency contains **at least one very low probability container node trigram**. So these are the **relevant "island" representations**.

## b. Subject

(i) \* Who does [<sub>IP</sub> Jack [<sub>VP</sub> think [<sub>CP<sub>null</sub></sub> [<sub>IP</sub> [<sub>NP</sub> the necklace [<sub>PP</sub> for \_\_ ] ] is expensive]]]]?

(ii) *start-IP-VP-CP<sub>null</sub>-IP-NP-PP-end*

(iii) Low probability:

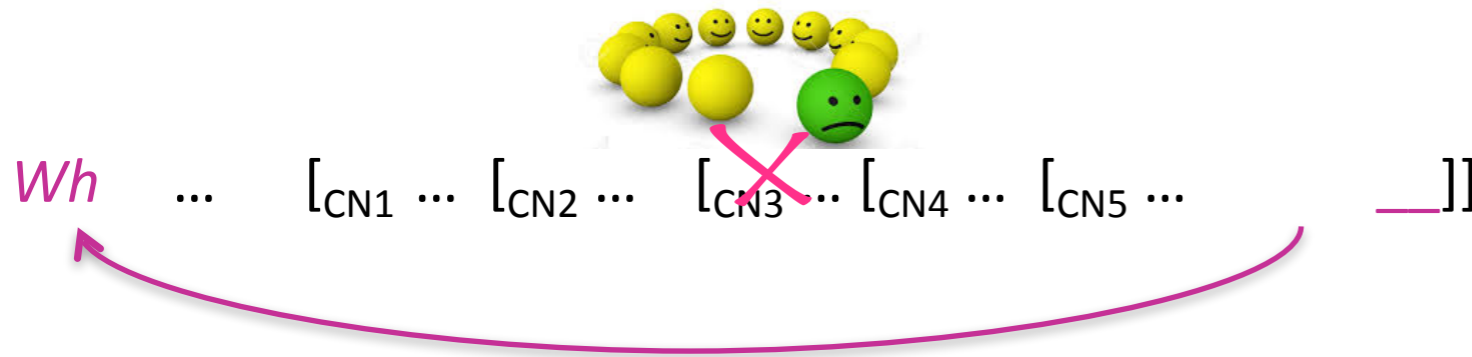
*CP<sub>null</sub>-IP-NP*

# ✓ Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Let's look inside them and see!

It turns out that each island-spanning dependency contains **at least one very low probability container node trigram**. So these are the **relevant "island" representations**.

c. Whether

- (i) \* What does [<sub>IP</sub> the teacher [<sub>VP</sub> wonder [<sub>CP<sub>whether</sub></sub> whether [<sub>IP</sub> Jack [<sub>VP</sub> stole \_\_ ]]]]]?
- (ii) *start-IP-VP-CP<sub>whether</sub>-IP-VP-end*
- (iii) Low probability:

- IP-VP-CP<sub>whether</sub>
- VP-CP<sub>whether</sub>-IP
- CP<sub>whether</sub>-IP-VP

# ✓ Subjacency-ish (Pearl & Sprouse 2013a, 2013b, 2015)



syntax

syntactic island



Wh ... [CN1 ... [CN2 ... [CN3 ... [CN4 ... [CN5 ... ]]]]



Let's look inside them and see!

It turns out that each island-spanning dependency contains **at least one very low probability container node trigram**. So these are the **relevant "island" representations**.

## d. Adjunct

(i) \* What does [<sub>IP</sub> the teacher [<sub>VP</sub> worry [<sub>CP<sub>if</sub></sub> if [<sub>IP</sub> Lily [<sub>VP</sub> forgot \_ ]]]]]?

(ii) *start-IP-VP-CP<sub>if</sub>-IP-VP-end*

(iii) Low probability:

IP-VP-CP<sub>if</sub>  
VP-CP<sub>if</sub>-IP  
CP<sub>if</sub>-IP-VP



# Learning strategies

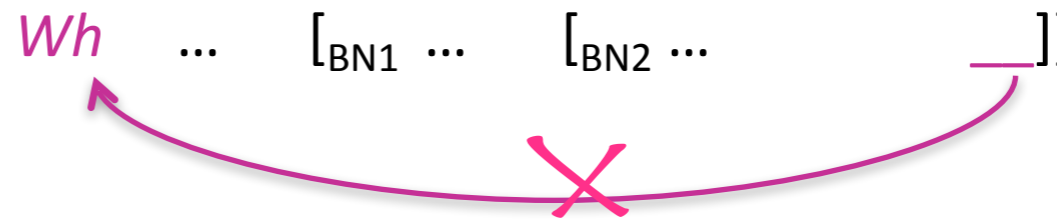


syntax

syntactic island

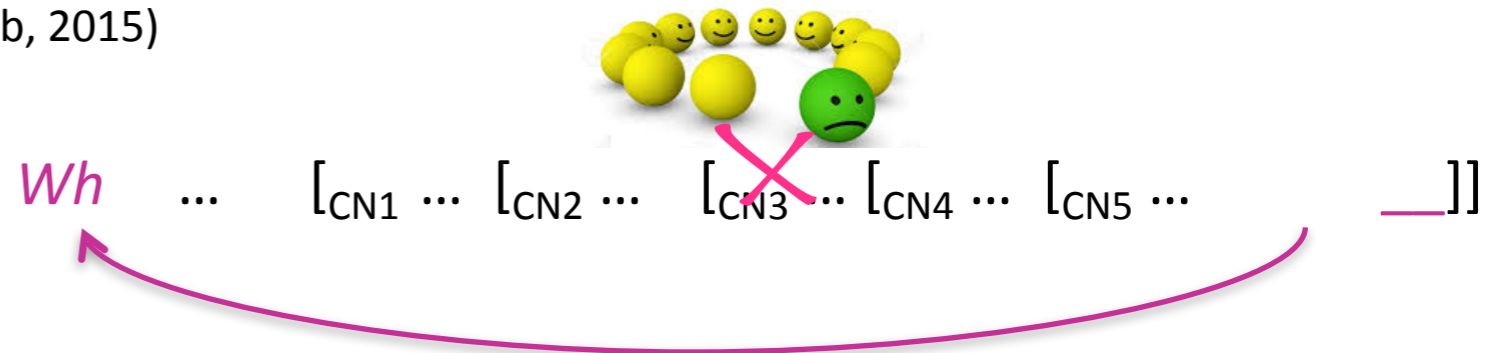
**Subjacency** (Chomsky 1973, Huang 1982, Lasnik & Saito 1984)

can't cross 2+ bounding nodes  
from a fixed set (CP, IP, and/or NP)



✓ **Subjacency-ish** (Pearl & Sprouse 2013a, 2013b, 2015)

A dependency can't cross a very  
low probability sequence of  
container nodes



**In common: Local structural anomaly is the problem**

The way Subjacency-ish implements this local structural anomaly can allow the development of syntactic island knowledge **without relying on prior knowledge about bounding nodes and how many a dependency is limited to crossing.**



**Less reliance on island-specific prior knowledge**

# Learning strategies



syntax

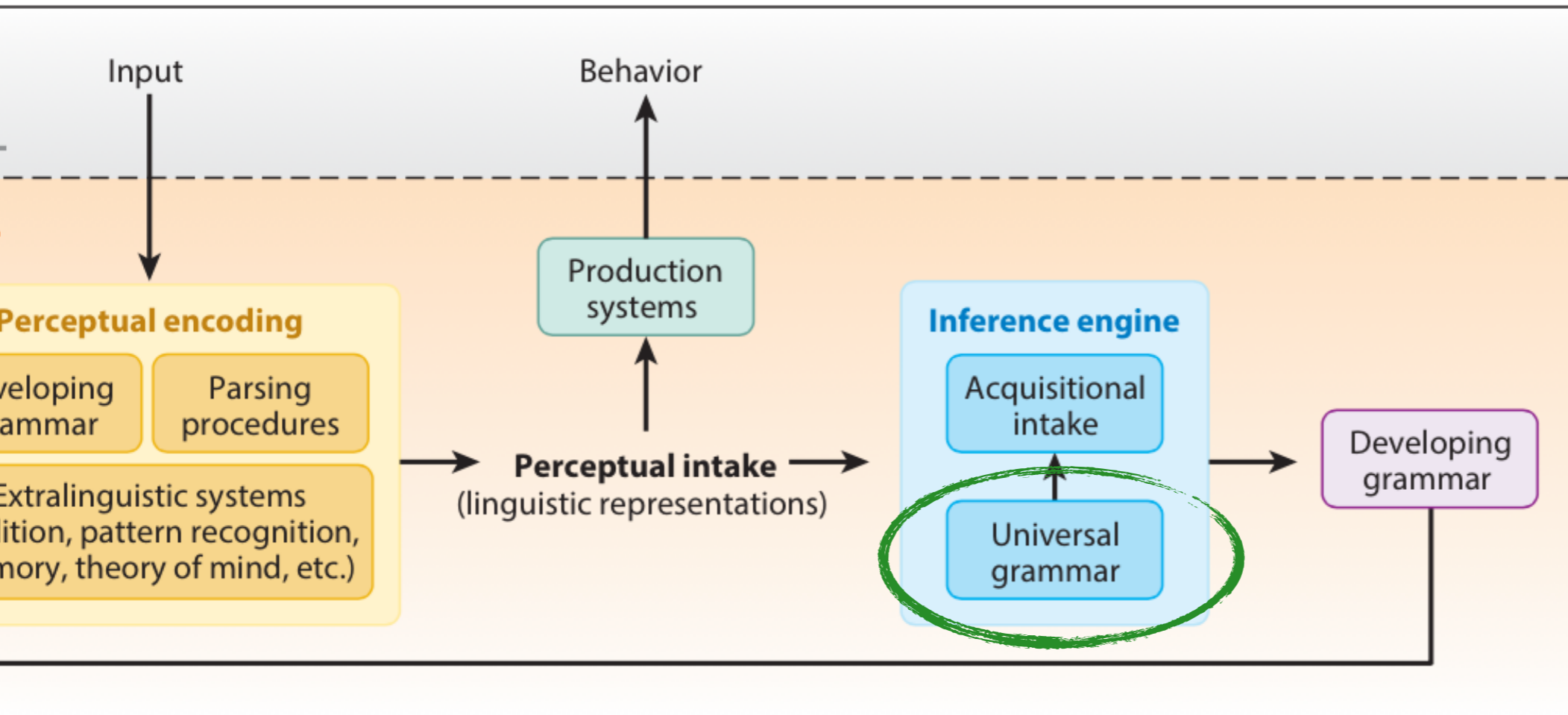
syntactic island

**Subjacency-ish** (Pearl & Sprouse 2013a, 2013b, 2015)



*Wh* ... [CN1 ... [CN2 ... [~~CN3~~ ... [CN4 ... [CN5 ... ]]]]

Less reliance on island-specific prior knowledge



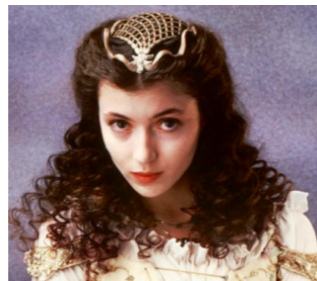
# Today's Plan:

## Computational models of syntactic acquisition

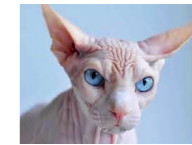
### I. Some non-parametric examples

Who does  ...  is pretty?

syntax



another one



syntax, semantics

# Pronoun interpretation

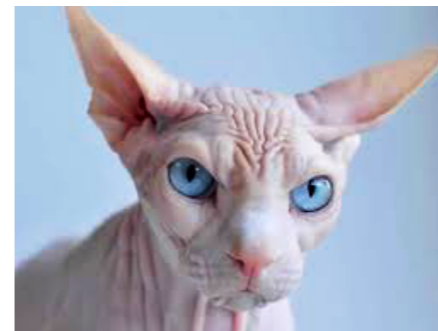
syntax, semantics

*another one*

“Oh look — a pretty kitty!”



“Look — there’s another **one**!”



# Pronoun interpretation

syntax, semantics

*another one*

antecedent

“Oh look — a pretty kitty!”



“Look — there’s another one!”

Interpretation: another pretty kitty

same

syntactic category

as antecedent

???

# Pronoun interpretation

syntax, semantics

*another one*

antecedent

“Oh look — a pretty kitty!”



“Look — there’s another one!”

Interpretation: another

same

syntactic category  
as antecedent

???

bigger than a plain Noun

Noun

pretty **kitty**

# Pronoun interpretation

syntax, semantics

another one

antecedent

“Oh look — a pretty kitty!”



“Look — there’s another one!”

Interpretation: another ~~the~~ pretty kitty

same syntactic category as antecedent

???

smaller than a full Noun Phrase

Noun Phrase

the

Noun

pretty kitty

# Pronoun interpretation

syntax, semantics

another *one*

antecedent

“Oh look — a pretty kitty!”



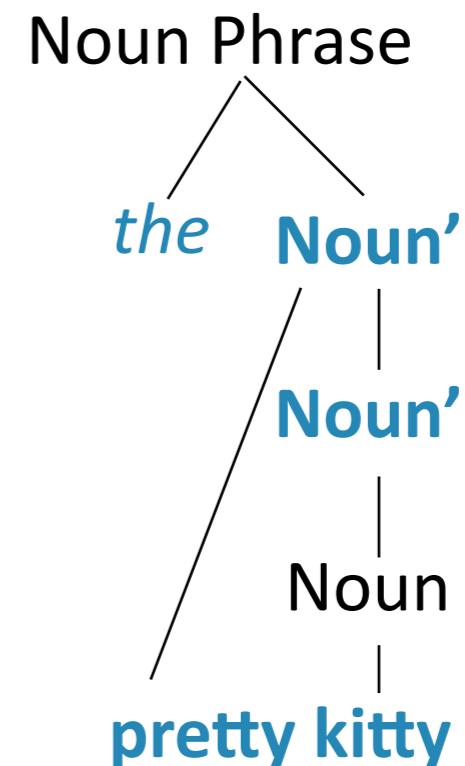
“Look — there’s another *one*!”

Interpretation: another

same  
syntactic category  
as antecedent

???

In-between category **Noun'**  
that includes strings with nouns  
and modifiers+nouns





# Pronoun interpretation

syntax, semantics

another *one*

antecedent

“Oh look — a pretty **kitty!**”

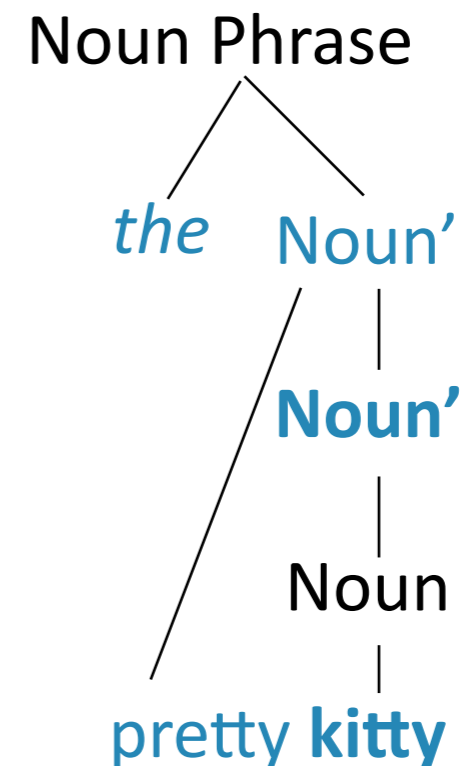
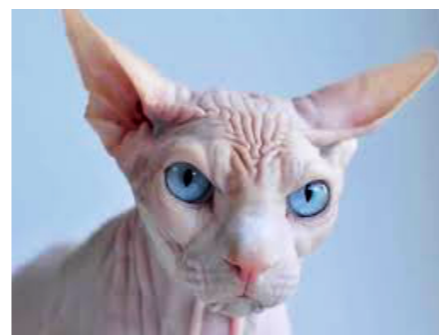


“Look — there’s another **one!**”

Interpretation: another

same  
syntactic category  
as antecedent

This is why we can also interpret **one** as just **kitty**.



# Pronoun interpretation

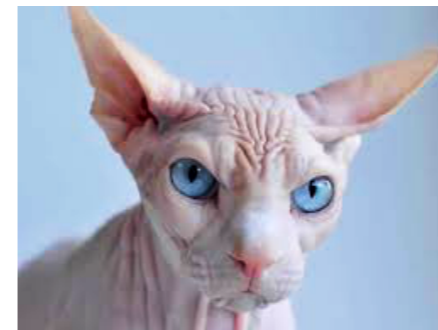
syntax, semantics

*another one*

“Oh look — a pretty kitty!”



“Do you see another one?”



Lidz, Waxman, & Freedman 2003:  
18-month-old interpretations

# Pronoun interpretation

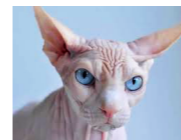
syntax, semantics

*another one*

“Oh look — a pretty kitty!”



“Do you see another *one*?”



Lidz, Waxman, & Freedman 2003:  
18-month-old interpretations

# Pronoun interpretation

syntax, semantics

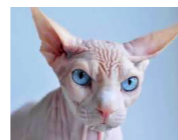
another one

“Oh look — a pretty kitty!”



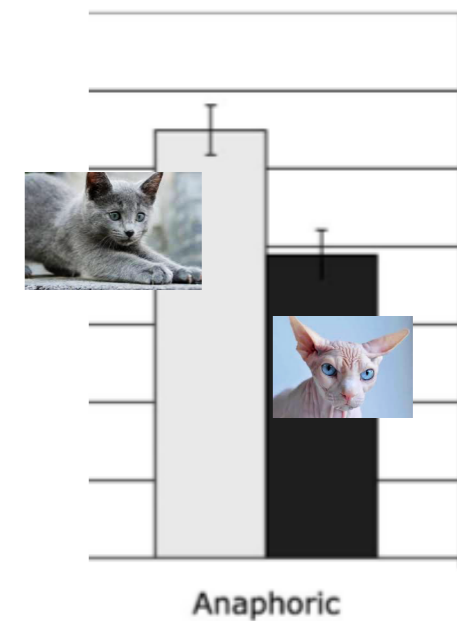
“Do you see another one?”

pretty kitty  
Noun'



*J. Lidz et al. / Cognition 89 (2003) B65–B73*

Mean Looking Time (seconds)



Lidz, Waxman, & Freedman 2003:  
18-month-old interpretations

# Pronoun interpretation

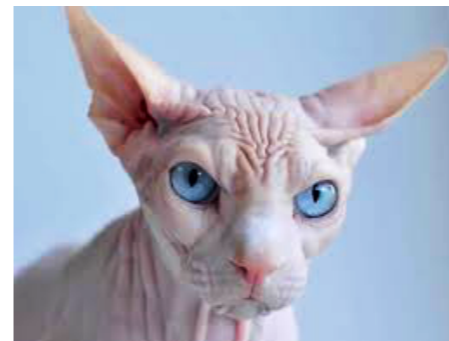
syntax, semantics

*another one*

“Oh look — a pretty kitty!”



“What do you see now?”



another *one*  
*pretty kitty*  
Noun'



Lidz, Waxman, & Freedman 2003:  
18-month-old interpretations

# Pronoun interpretation

syntax, semantics

*another one*

“Oh look — a pretty kitty!”



“What do you see now?”



another *one*  
*pretty kitty*  
Noun'



Lidz, Waxman, & Freedman 2003:  
18-month-old interpretations

# Pronoun interpretation

syntax, semantics

another one

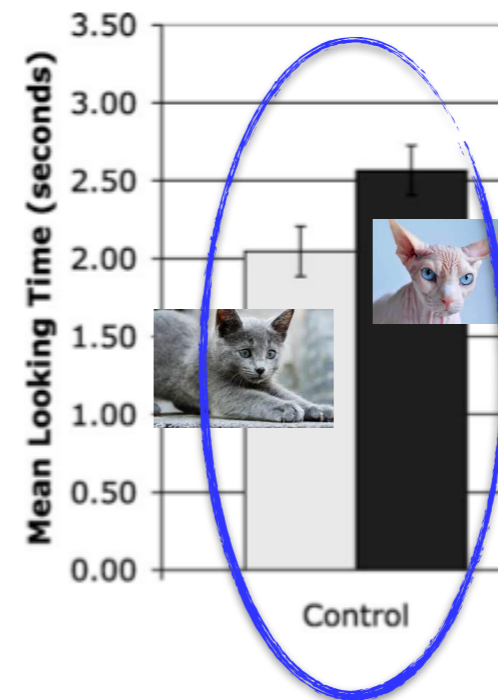
“Oh look — a pretty kitty!”



Shows baseline  
looking preference

*J. Lidz et al. / Cognition 89 (2003) B65–B73*

“What do you see now?”



another one  
pretty kitty  
Noun'



Lidz, Waxman, & Freedman 2003:  
18-month-old interpretations

# Pronoun interpretation

syntax, semantics

another one

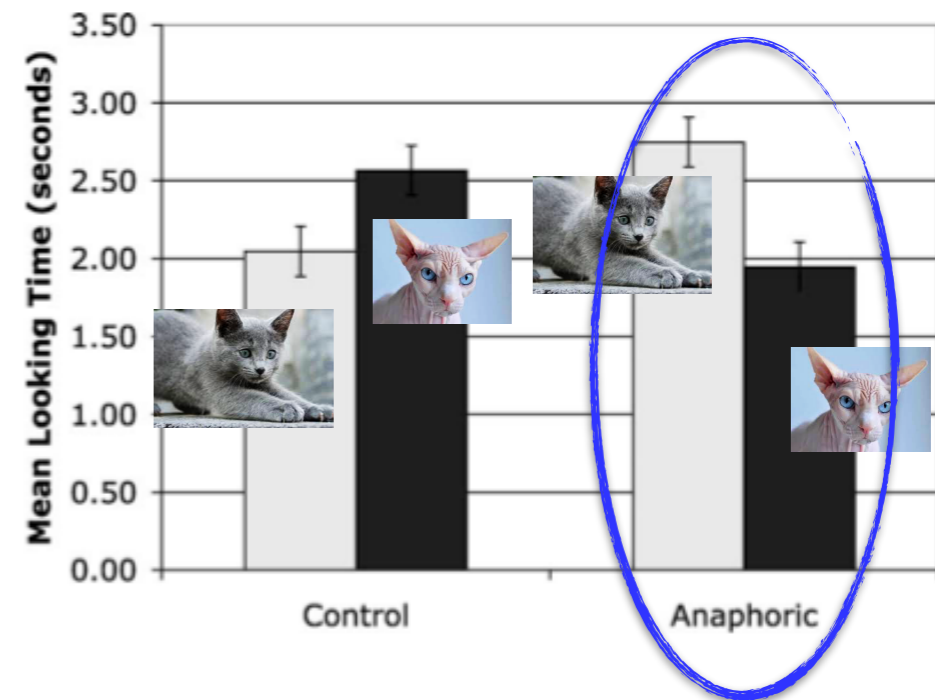
“Oh look — a pretty kitty!”



Shows baseline looking preference which is counteracted with “Do you see another one?”

*J. Lidz et al. / Cognition 89 (2003) B65–B73*

“What do you see now?”



another one  
pretty kitty  
Noun'



Lidz, Waxman, & Freedman 2003:  
18-month-old interpretations



# Pronoun interpretation

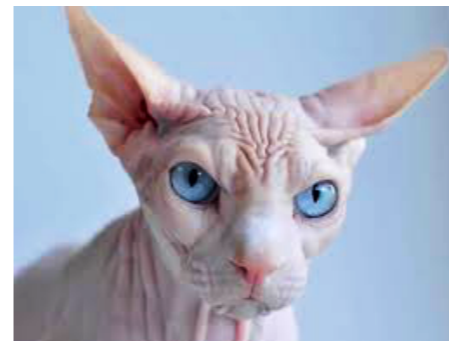
syntax, semantics

*another one*

“Oh look — a pretty kitty!”



“Do you see another kitty?”



another *one*  
*pretty kitty*  
Noun'



Lidz, Waxman, & Freedman 2003:  
18-month-old interpretations

# Pronoun interpretation

syntax, semantics

*another one*

“Oh look — a pretty kitty!”



“Do you see another kitty?”



another *one*  
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Lidz, Waxman, & Freedman 2003:  
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# Pronoun interpretation

syntax, semantics

another one

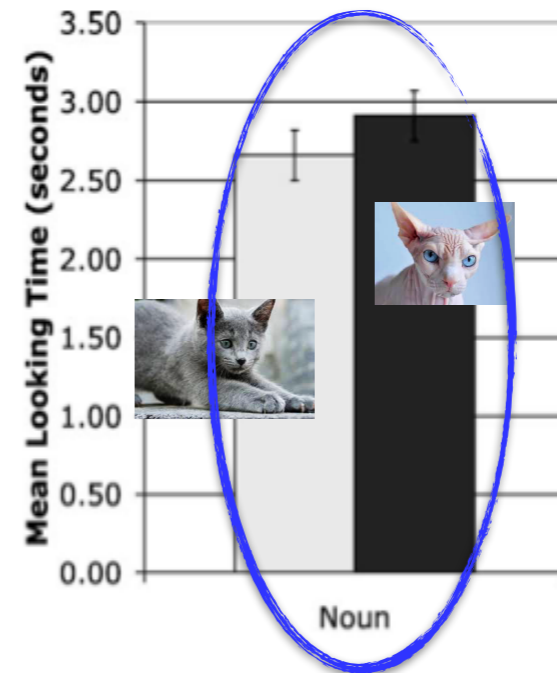
“Oh look — a pretty kitty!”



Shows baseline  
looking preference

*J. Lidz et al. / Cognition 89 (2003) B65–B73*

“Do you see another kitty?”



another one  
pretty kitty  
Noun'



Lidz, Waxman, & Freedman 2003:  
18-month-old interpretations

# Pronoun interpretation

syntax, semantics

*another one*

“Oh look — a pretty kitty!”



“Do you see another pretty kitty?”



another *one*  
*pretty kitty*  
Noun'



Lidz, Waxman, & Freedman 2003:  
18-month-old interpretations

# Pronoun interpretation

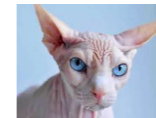
syntax, semantics

*another one*

“Oh look — a pretty kitty!”



“Do you see another pretty kitty?”



another *one*  
*pretty kitty*  
Noun'



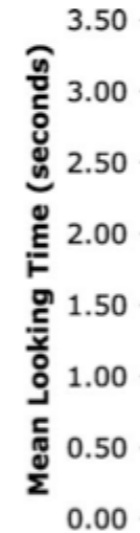
Lidz, Waxman, & Freedman 2003:  
18-month-old interpretations

# Pronoun interpretation

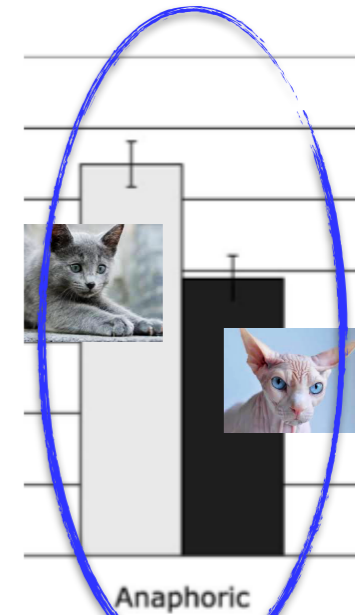
syntax, semantics

another one

“Oh look — a pretty kitty!”

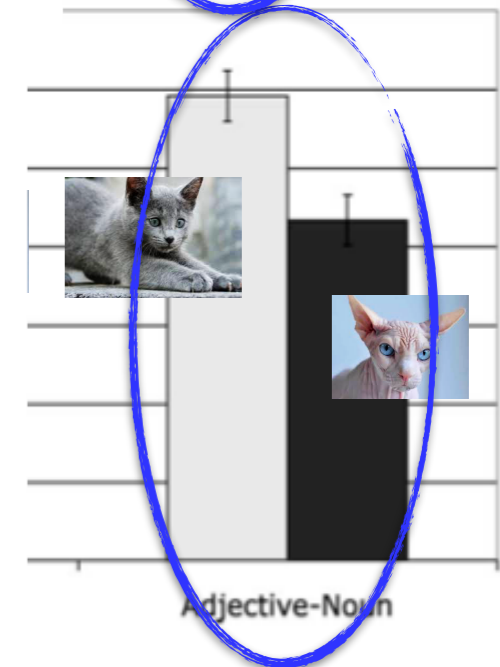
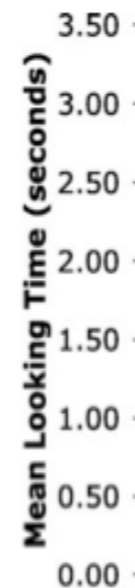
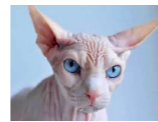


J. Lidz et al. / Cognition 89 (2003) B65–B73



Same looking pattern as “another one”

“Do you see another pretty kitty?”



another one  
pretty kitty  
Noun'



Lidz, Waxman, & Freedman 2003:  
18-month-old interpretations

# Pronoun interpretation

syntax, semantics

another one

“Oh look — a pretty kitty!”



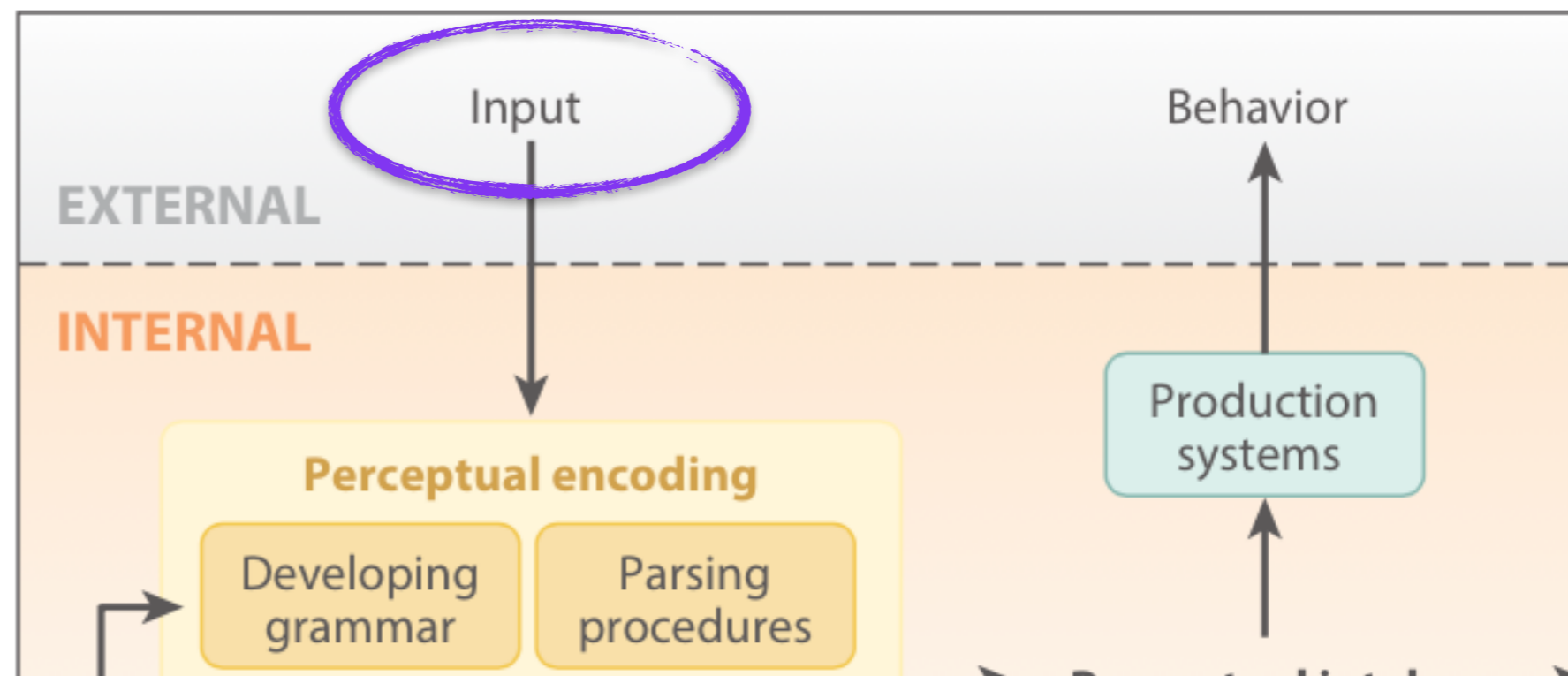
Noun'  
pretty kitty

“Do you see another one ?”



Several learning strategies implemented with **algorithmic-level** modeled learners, given **realistic** samples of English child-directed speech.

Pearl & Mis 2016



# Pronoun interpretation

syntax, semantics

another one



Noun'  
pretty kitty

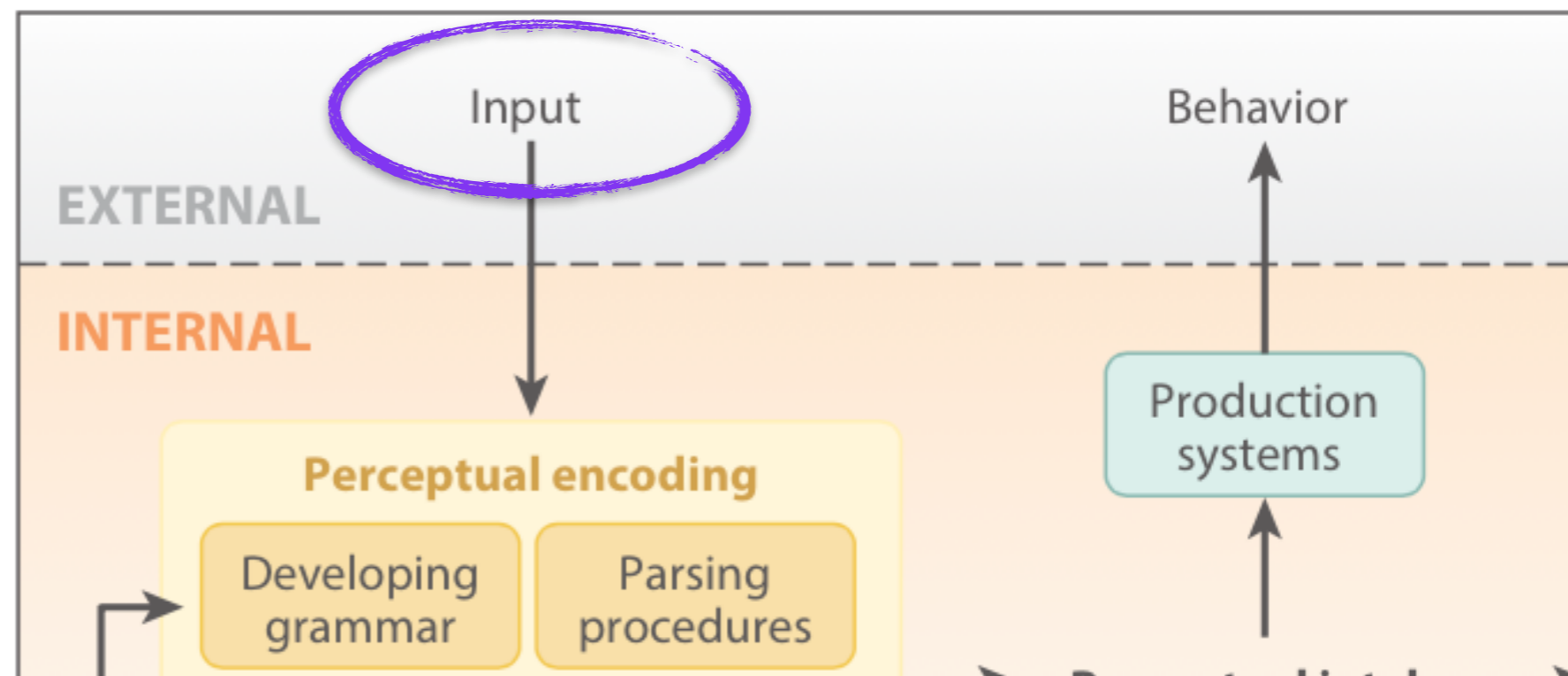
## English child-directed speech

Problem: Most direct evidence children encounter is ambiguous.

## Syntactically (SYN) ambiguous data

(92% according to corpus study by Pearl & Mis 2011, 2016):

“Look – a kitty! Oh, look – another one.”





# Pronoun interpretation

syntax, semantics

another one



Noun'  
pretty kitty

## English child-directed speech

Problem: Most direct evidence children encounter is ambiguous.

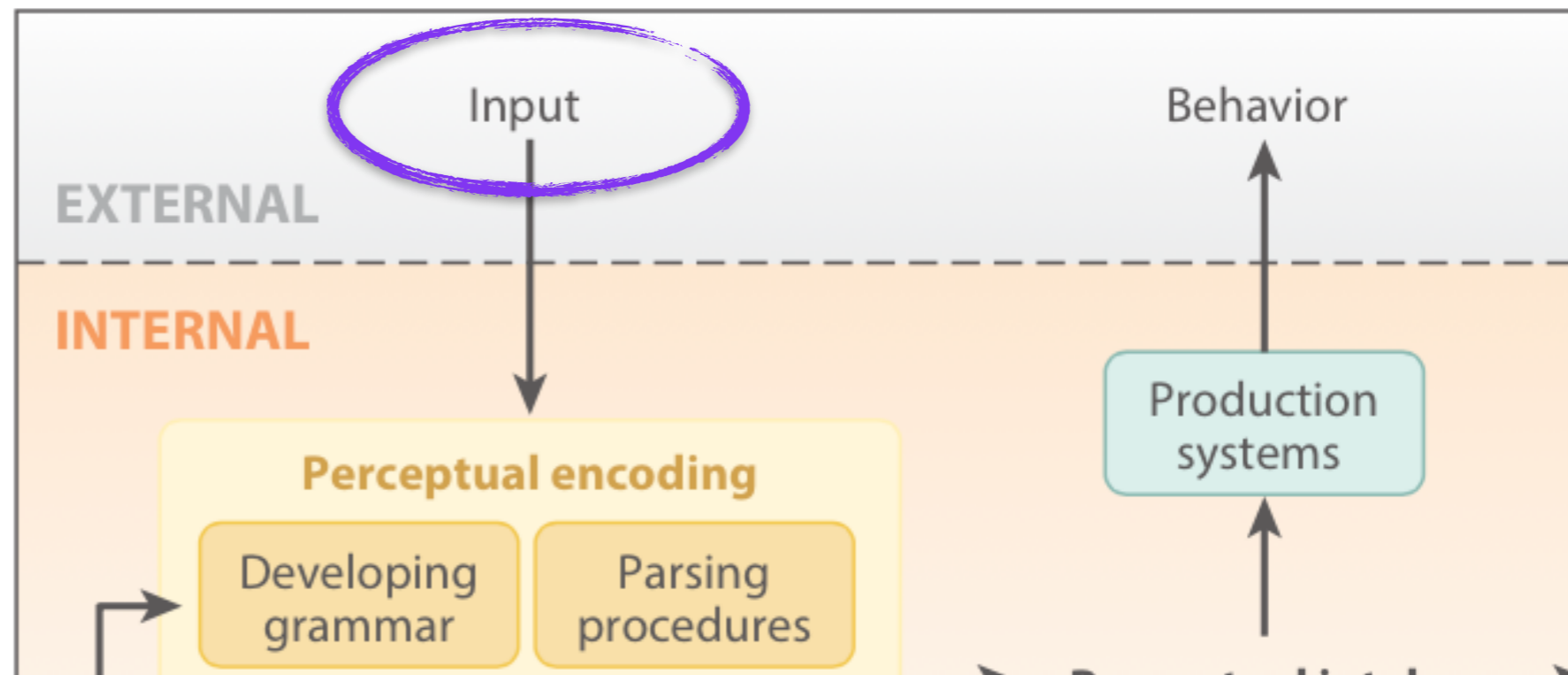
## Syntactically (SYN) ambiguous data

(92% according to corpus study by Pearl & Mis 2011, 2016):

“Look – a **kitty**! Oh, look – another **one**.”

Antecedent = “kitty”

Referent



# Pronoun interpretation

syntax, semantics

another one



Noun'  
pretty kitty

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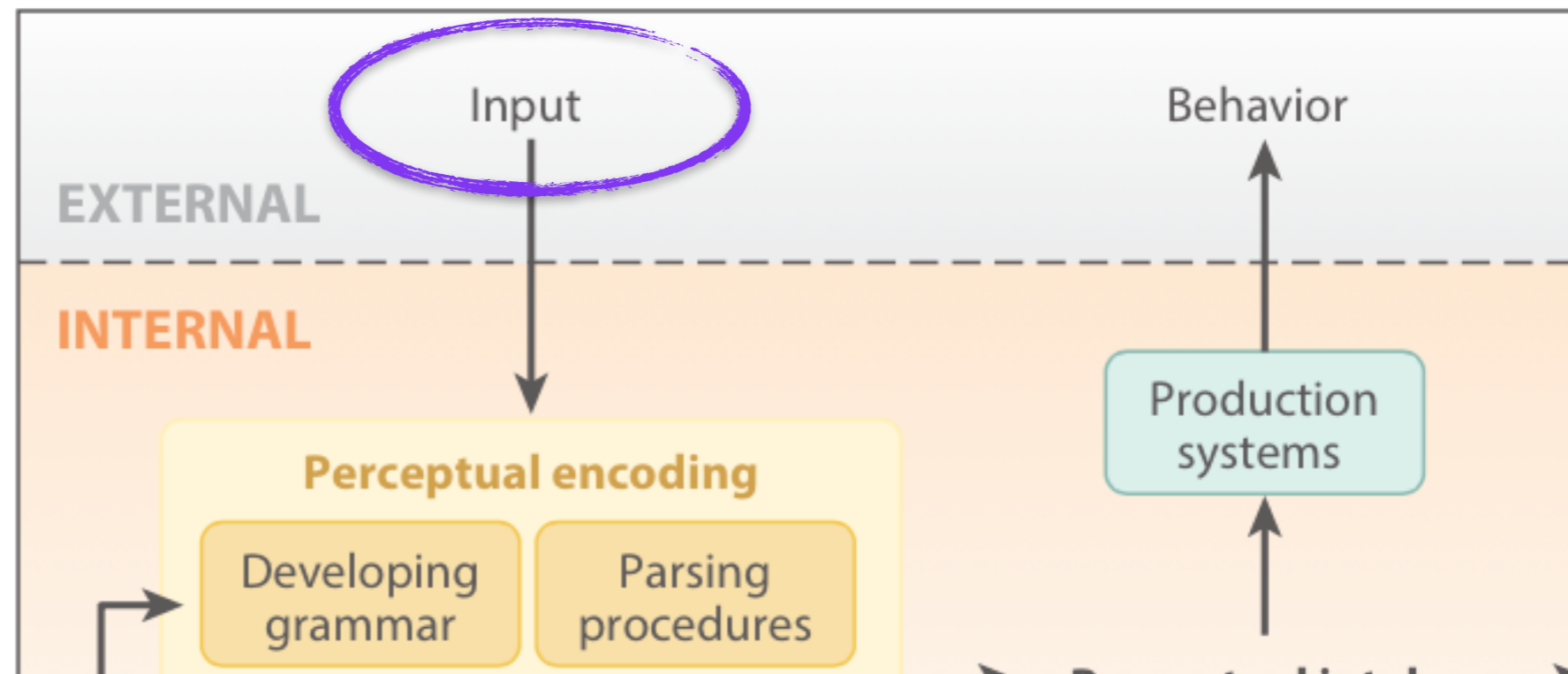
Antecedent = “kitty”

Referent



Syntactic category?

Noun'  
Noun  
kitty



# Pronoun interpretation

syntax, semantics

another one



92% SYN ambiguous

Noun'  
pretty kitty

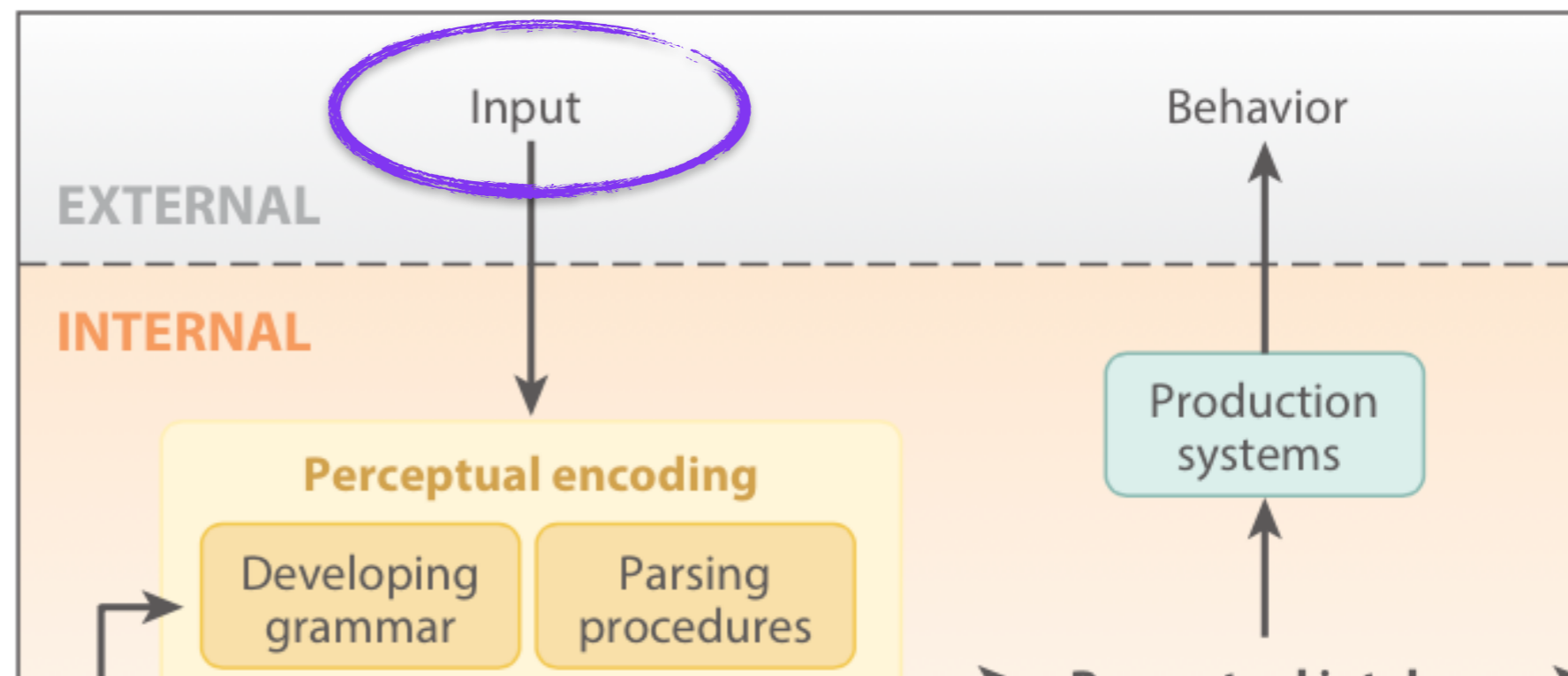
## English child-directed speech

Problem: Most direct evidence children encounter is ambiguous.

Referentially and syntactically (REF-SYN) ambiguous

(8% according to corpus study by Pearl & Mis 2011, 2016)

“Look – a pretty kitty! Oh, look – another one.”



# Pronoun interpretation

syntax, semantics

another one



92% SYN ambiguous

Noun'

pretty kitty

## English child-directed speech

Problem: Most direct evidence children encounter is ambiguous.

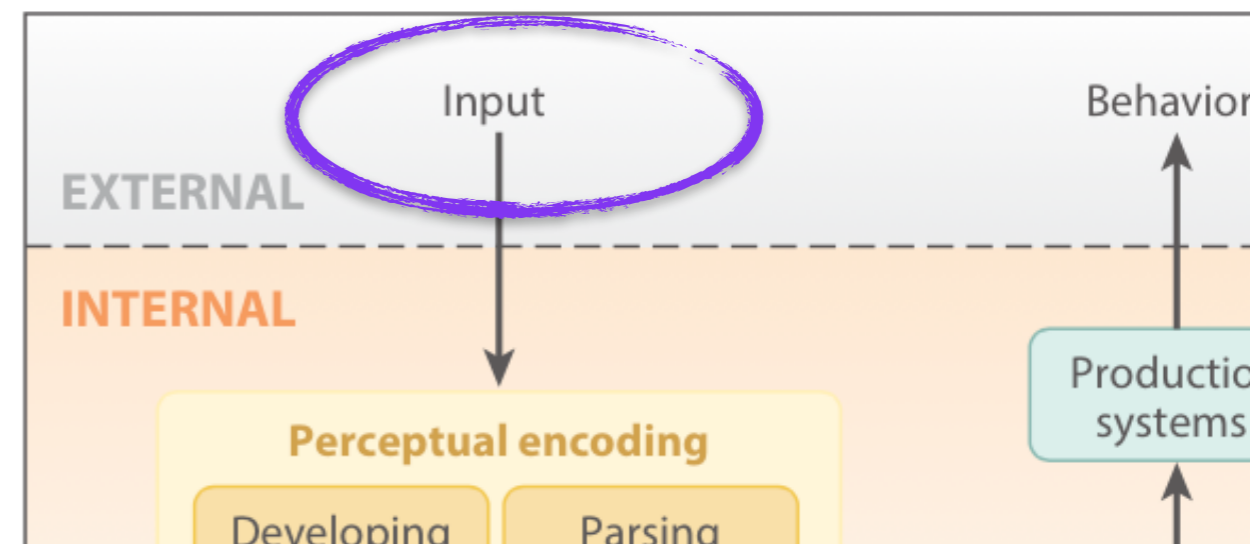
Referentially and syntactically (REF-SYN) ambiguous

(8% according to corpus study by Pearl & Mis 2011, 2016)

“Look – a pretty **kitty!** Oh, look – another **one.**”



Referent



# Pronoun interpretation

syntax, semantics

another *one*



92% SYN ambiguous

Noun'

pretty kitty

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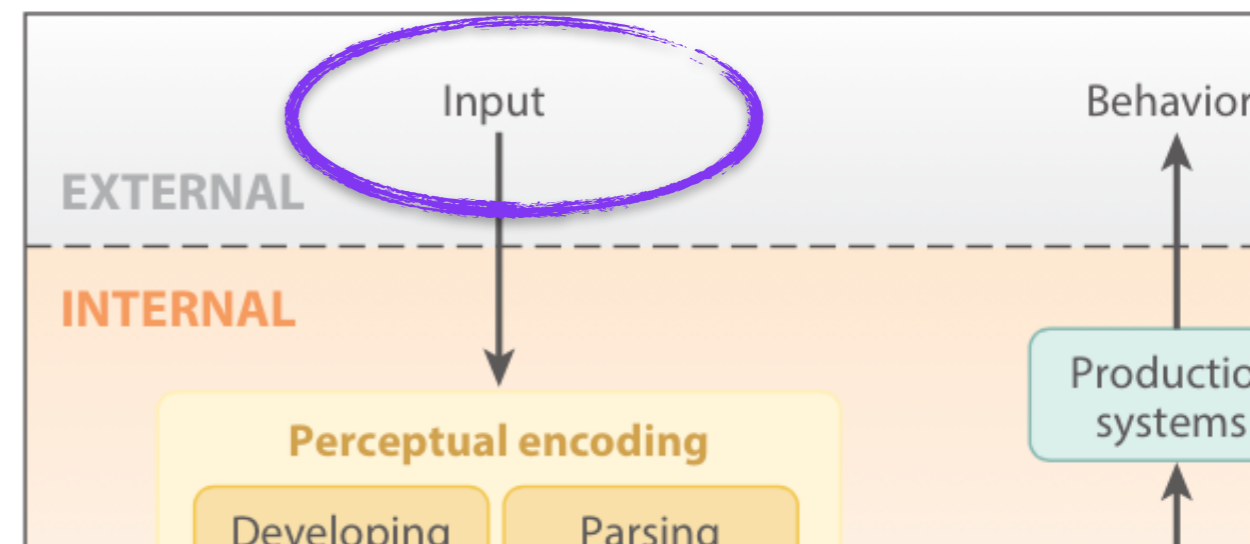
“Look – a **pretty kitty!** Oh, look – another **one.**”

Antecedent = “pretty kitty”

OR

Antecedent = “kitty”

Referent



# Pronoun interpretation

syntax, semantics

another *one*



92% SYN ambiguous

Noun'  
pretty kitty

## English child-directed speech

Problem: Most direct evidence children encounter is ambiguous.

Referentially and syntactically (REF-SYN) ambiguous

(8% according to corpus study by Pearl & Mis 2011, 2016)

“Look – a **pretty kitty!** Oh, look – another **one.**”

Antecedent = “pretty kitty”  
???

Antecedent = “kitty”

Referent



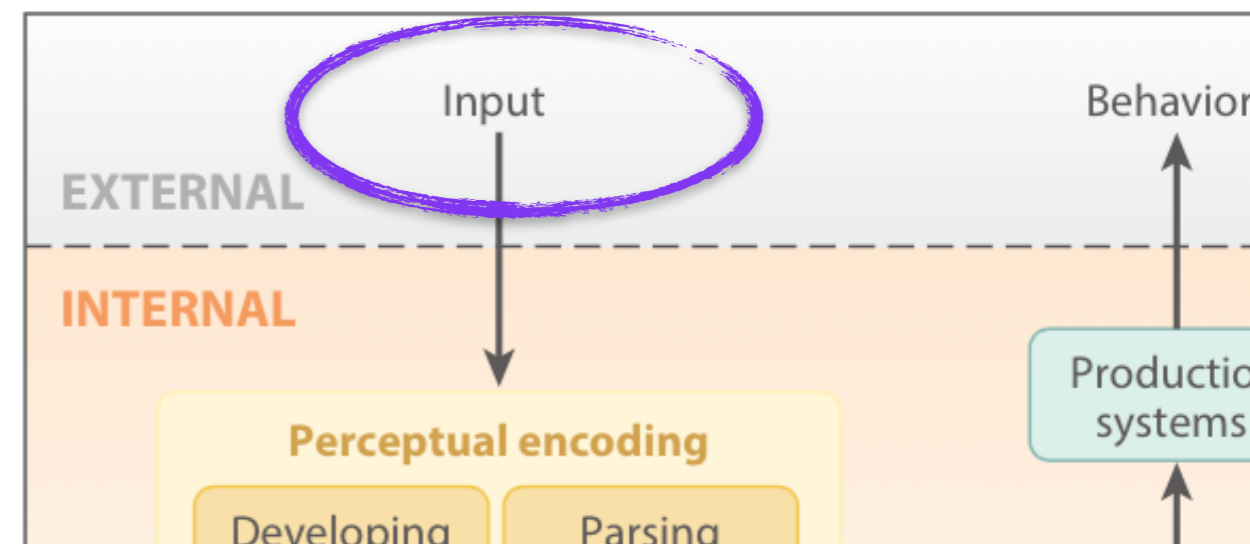
Syntactic category?

???

Noun'

Noun

kitty



# Pronoun interpretation

syntax, semantics

another one



92% SYN ambiguous

Noun'  
pretty kitty

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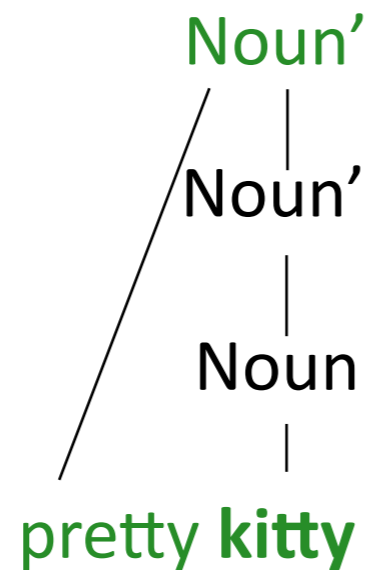
“Look – a pretty kitty! Oh, look – another one.”

Antecedent = “pretty kitty”

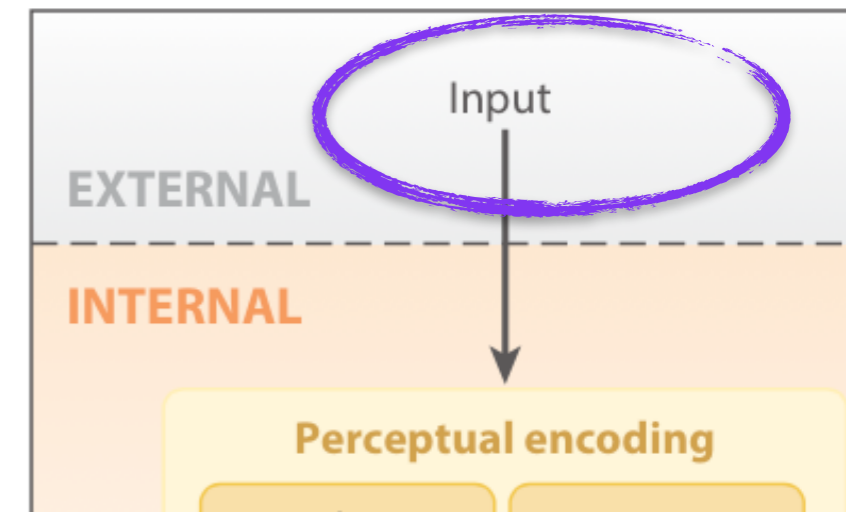
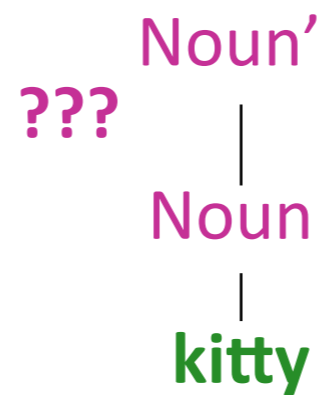
???

Antecedent = “kitty”

Referent



Syntactic category?



# Pronoun interpretation

syntax, semantics

another one



Noun'

pretty kitty



92% SYN ambiguous

8% REF-SYN ambiguous

## English child-directed speech

Problem: Most direct evidence children encounter is ambiguous.

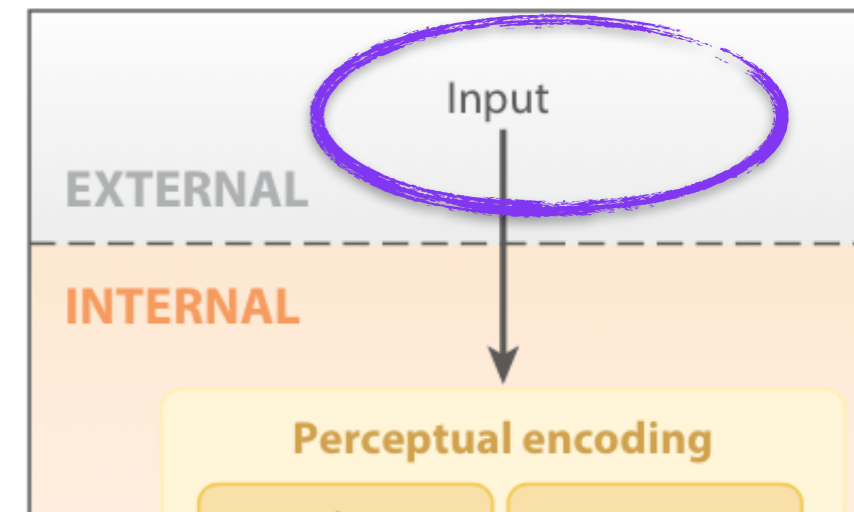
Unambiguous (UNAMB) data

What we wish were there but isn't

(0% according to corpus study by Pearl & Mis 2011, 2016)

“Look – a pretty kitty!

Hmmm - there doesn't seem to be another one here, though.”





# Pronoun interpretation

syntax, semantics

another one



Noun'

pretty kitty



## English child-directed speech

Problem: Most direct evidence children encounter is ambiguous.

Unambiguous (UNAMB) data

What we wish were there but isn't

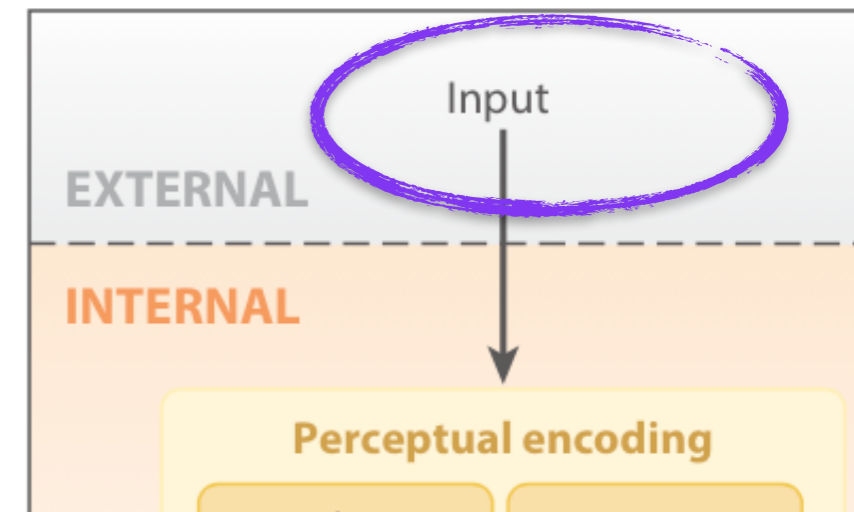
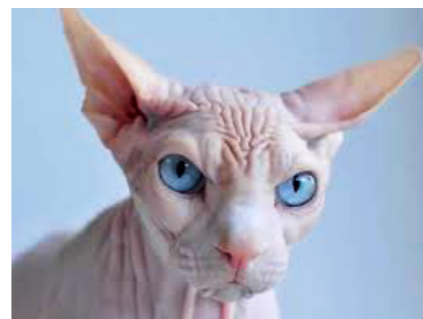
(0% according to corpus study by Pearl & Mis 2011, 2016)

“Look – a pretty **kitty**!

Hmmm - there doesn't seem to be another **one** here, though.”

~~kitty~~

Can't have “**kitty**” as its antecedent, because there *is* another kitty here. This would be a false thing to say.



# Pronoun interpretation

syntax, semantics

another one



Noun'

pretty kitty



Referent

92% SYN ambiguous

8% REF-SYN ambiguous

## English child-directed speech

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Unambiguous (UNAMB) data

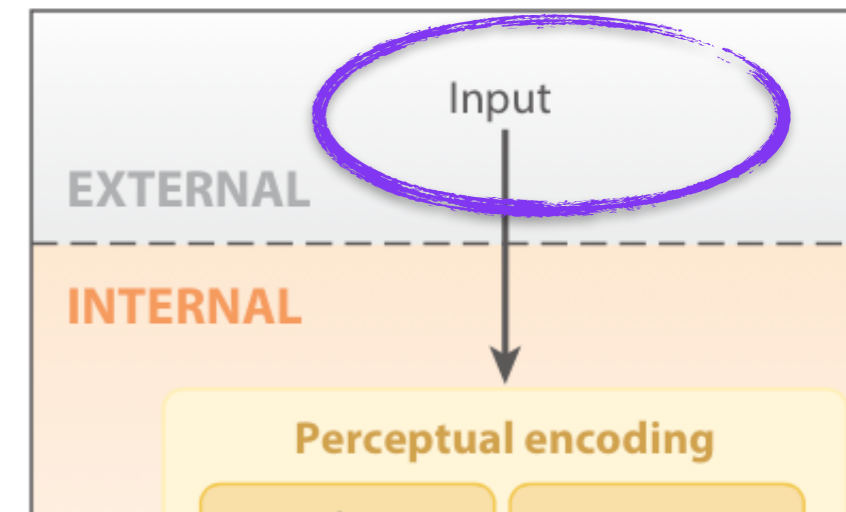
What we wish were there but isn't

(0% according to corpus study by Pearl & Mis 2011, 2016)

“Look – a **pretty kitty!**

Must have “pretty kitty” as its antecedent.

Hmmm - there doesn't seem to be another **one** here, though.”



# Pronoun interpretation

syntax, semantics

another one



Noun'

pretty kitty



Referent

92% SYN ambiguous

8% REF-SYN ambiguous

## English child-directed speech

Problem: Most direct evidence children encounter is ambiguous.

Unambiguous (UNAMB) data

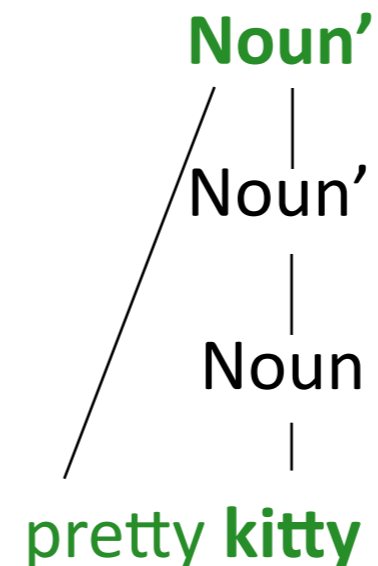
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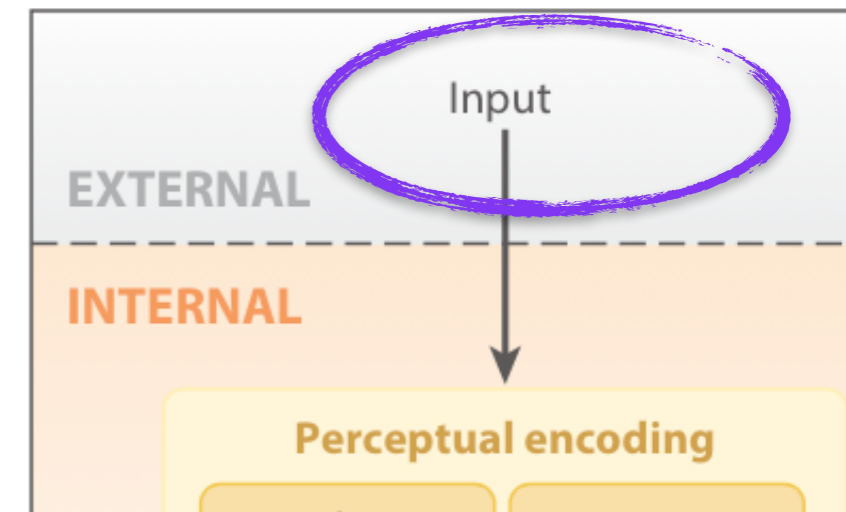
“Look – a **pretty kitty!**

Must have “pretty kitty” as its antecedent.

Hmmm - there doesn't seem to be another **one** here, though.”



and be a Noun' category.



# Pronoun interpretation

syntax, semantics

another *one*



English child-directed speech

Problem: Most direct evidence  
children encounter is ambiguous.

92% SYN ambiguous

8% REF-SYN ambiguous

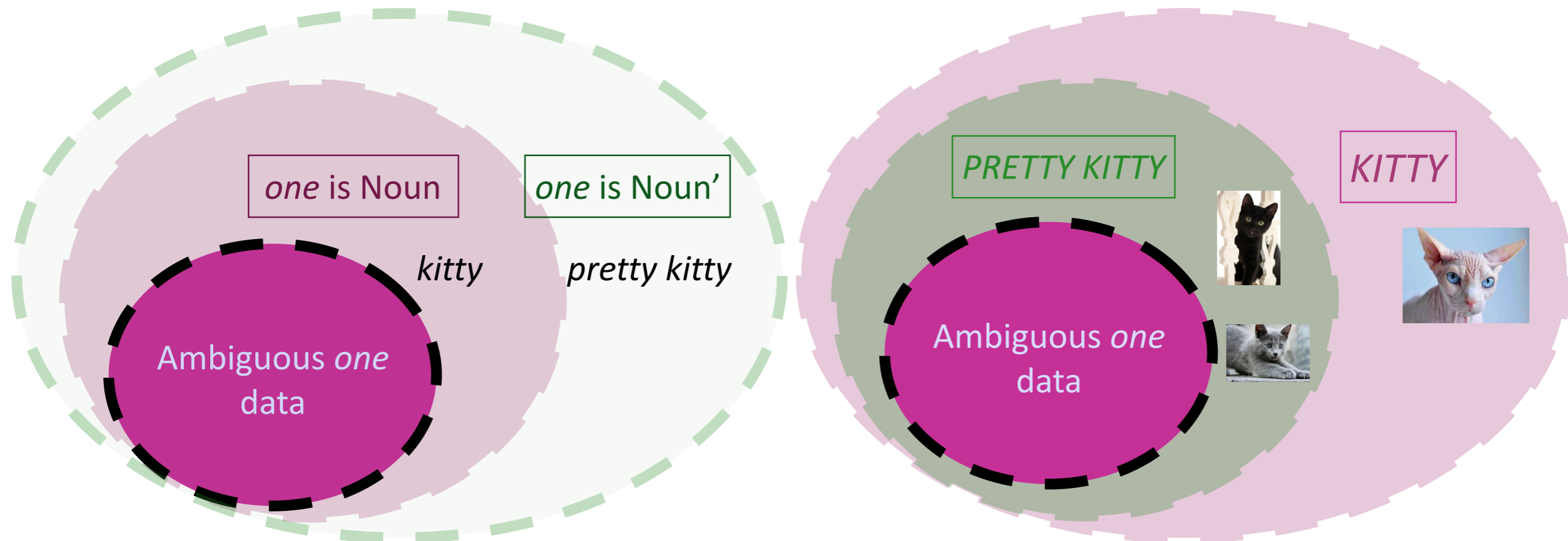
Noun'

pretty kitty

How do children learn the right generalizations for interpreting *one*?

syntactic category

referent in context



# Pronoun interpretation

syntax, semantics

another *one*

English child-directed speech

Problem: Most direct evidence  
children encounter is ambiguous.

92% SYN ambiguous

8% REF-SYN ambiguous



Noun'  
pretty kitty



How do children learn the right generalizations for interpreting *one*?

Regier & Gahl (2004), Pearl & Lidz (2009):  
**Filtering the direct evidence** (being more selective about what you learn from) & learning from it in more sophisticated ways

Pearl & Mis (2016): **Leveraging a broader set of data** to learn from & learning from it more sophisticated ways



# Pronoun interpretation

syntax, semantics

another *one*

English child-directed speech

Problem: Most direct evidence  
children encounter is ambiguous.

92% SYN ambiguous

8% REF-SYN ambiguous



Noun'  
pretty kitty



How do children learn the right generalizations for interpreting *one*?

Regier & Gahl (2004), Pearl & Lidz (2009):

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Pearl & Mis (2016):

**Leveraging a broader set of data**

**Learning from it in more sophisticated ways**

# Pronoun interpretation

syntax, semantics

another one

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Noun'  
pretty kitty



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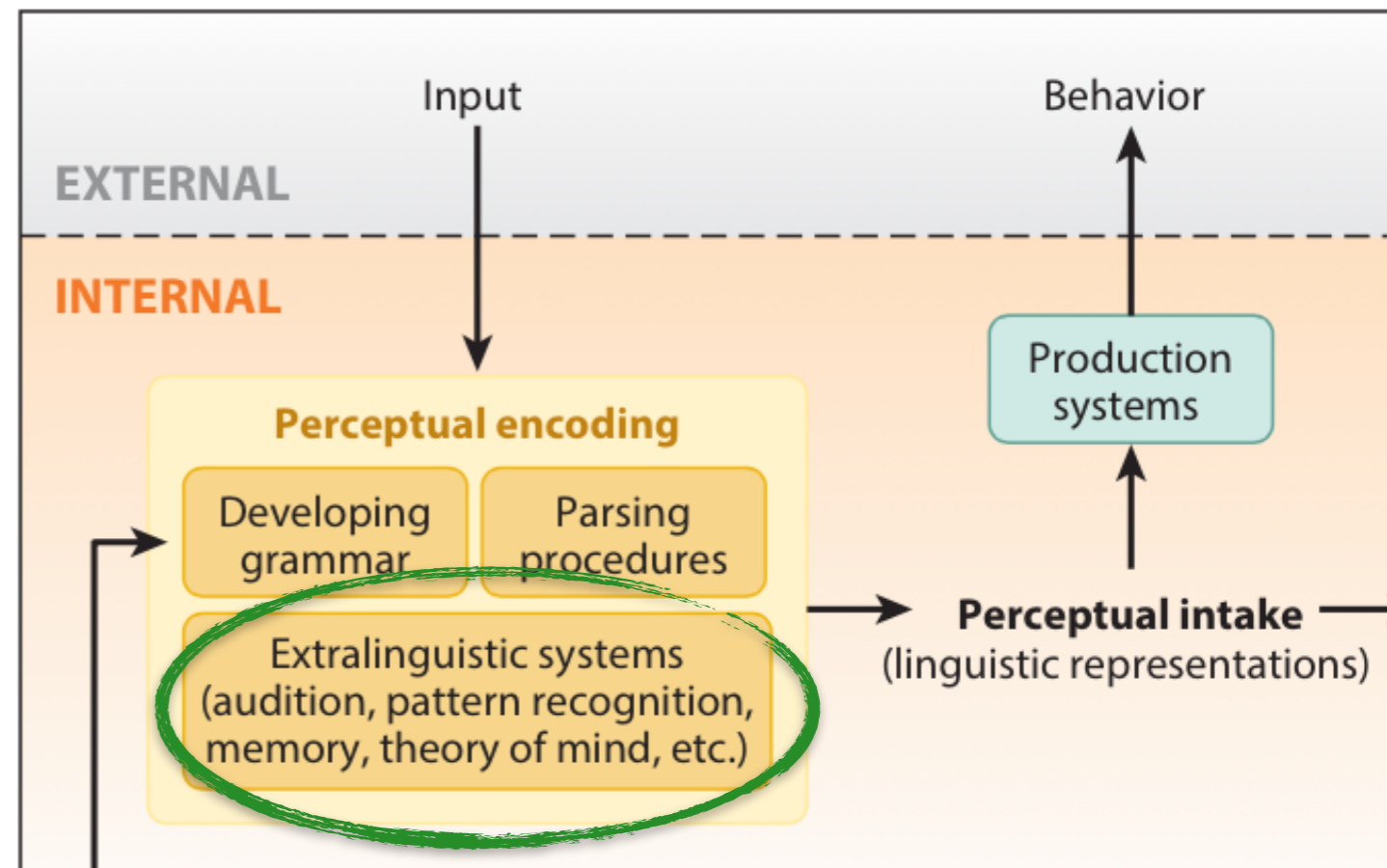
Filtering the direct evidence

Pearl & Mis (2016):

Leveraging a broader set of data

Learning from it in more sophisticated ways

Probabilistic reasoning about input:  
Bayesian inference



# Pronoun interpretation

syntax, semantics

another one

English child-directed speech

Problem: Most direct evidence children encounter is ambiguous.

92% SYN ambiguous

8% REF-SYN ambiguous



Noun'  
pretty kitty



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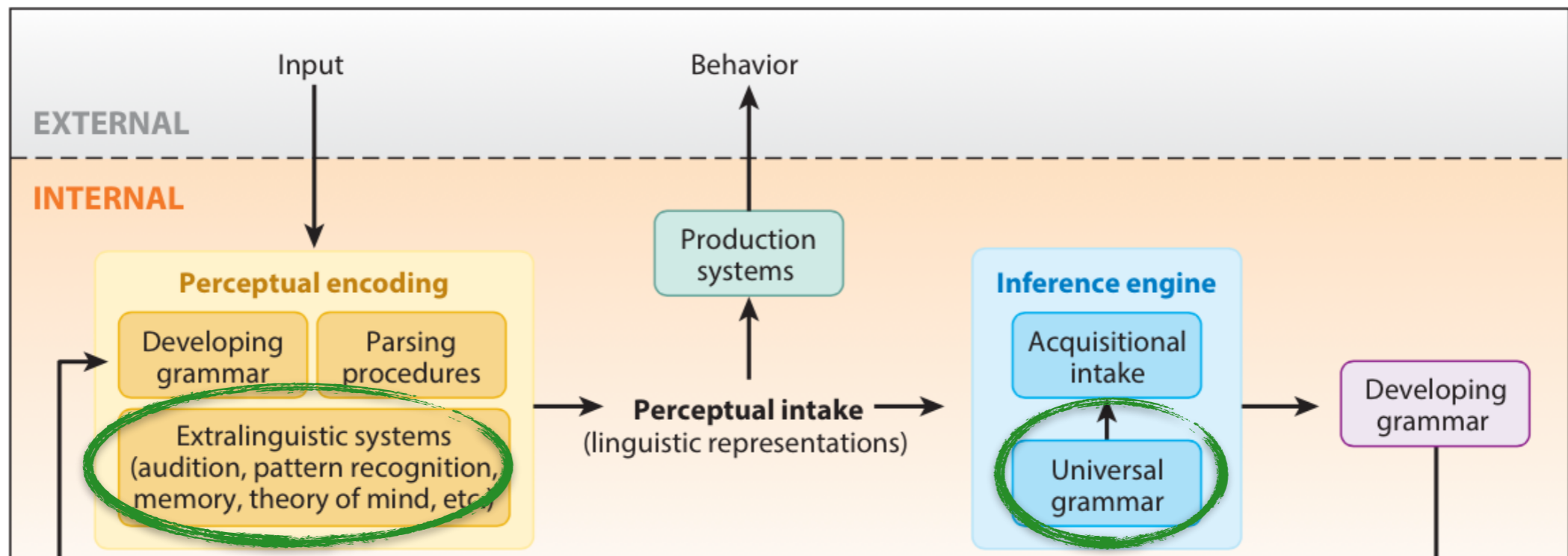
Pearl & Mis (2016):

Leveraging a broader set of data

Learning from it in more sophisticated ways

Regier & Gahl (2004), Pearl & Lidz (2009):

Filtering the direct evidence





# Pronoun interpretation

syntax, semantics

another *one*



English child-directed speech

Problem: Most direct evidence  
children encounter is ambiguous.

8% REF-SYN ambiguous

Noun'  
pretty kitty

How do children learn the right generalizations for interpreting *one*?

Pearl & Mis (2016):

**Leveraging a broader set of data**

**Learning from it in more sophisticated ways**

Regier & Gahl (2004), Pearl & Lidz (2009):

**Filtering the direct evidence**

**Ignore these data** 92% SYN ambiguous

“Look – a **kitty!**

Oh, look – another **one.**”



# Pronoun interpretation

syntax, semantics

another one



English child-directed speech

Problem: Most direct evidence  
children encounter is ambiguous.

Noun'  
pretty kitty

How do children learn the right generalizations for interpreting *one*?

Pearl & Mis (2016):

Leveraging a broader set of data

Learning from it in more sophisticated ways

Regier & Gahl (2004), Pearl & Lidz (2009):

Filtering the direct evidence

Ignore these data 92% SYN ambiguous

“Look – a pretty kitty!  
Oh, look – another one.”

and learn from these data  
using Bayesian inference

8% REF-SYN ambiguous



# Pronoun interpretation

syntax, semantics

another one

English child-directed speech

Problem: Most direct evidence children encounter is ambiguous.

92% SYN ambiguous  
8% REF-SYN ambiguous



Noun'  
pretty kitty



How do children learn the right generalizations for interpreting *one*?

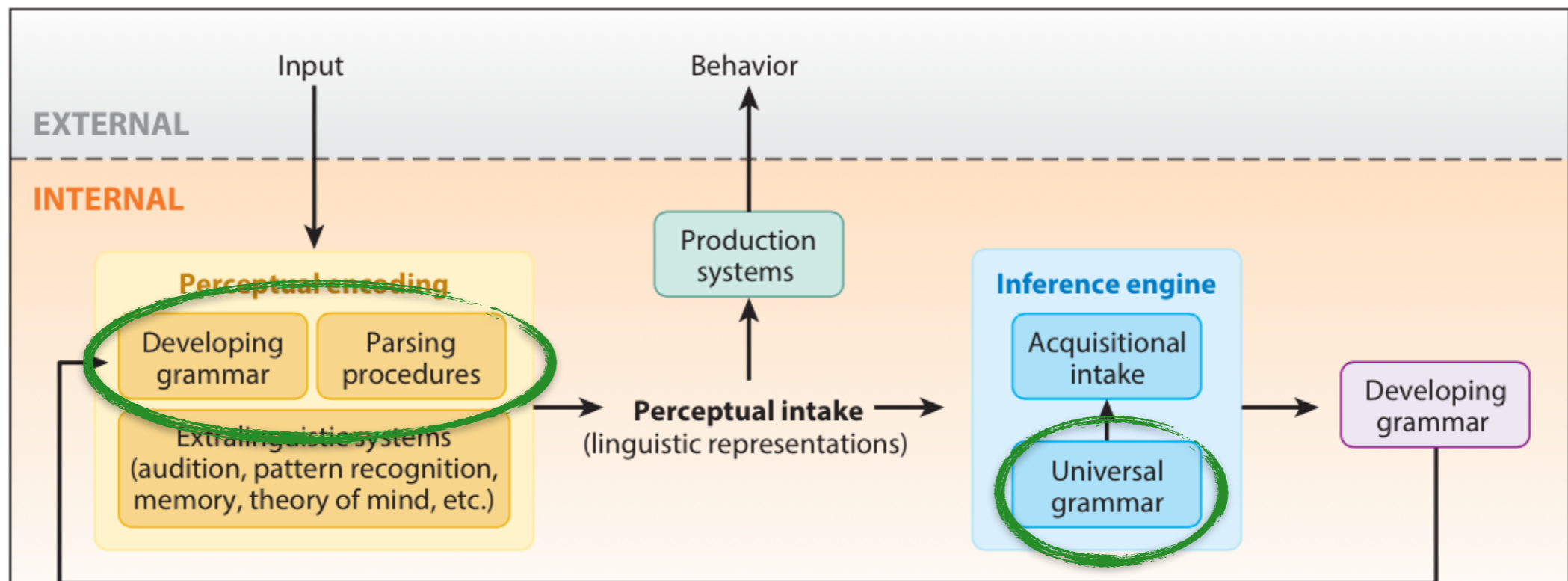
Regier & Gahl (2004), Pearl & Lidz (2009):

Filtering the direct evidence

Learning from it in more sophisticated ways

Pearl & Mis (2016):

Leveraging a broader set of data



# Pronoun interpretation

syntax, semantics

another *one*



English child-directed speech

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92% SYN ambiguous

8% REF-SYN ambiguous

Noun'

pretty kitty



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Regier & Gahl (2004), Pearl & Lidz (2009):

**Filtering the direct evidence**

**Learning from it in more sophisticated ways**

Pearl & Mis (2016):

**Leveraging a broader set of data**

**Learn from data like these  
that involve other pronouns**

“Look – a **pretty kitty!**

I want to pet **it.**”



# Pronoun interpretation

syntax, semantics

another one



## English child-directed speech

Problem: Most direct evidence  
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92% SYN ambiguous

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Noun'

pretty kitty



How do children learn the right generalizations for interpreting *one*?

Regier & Gahl (2004), Pearl & Lidz (2009):

**Filtering the direct evidence**

**Learning from it in more sophisticated ways**

Pearl & Mis (2016):

**Leveraging a broader set of data**

**Learn from data like these  
that involve other pronouns**

“Look – a **pretty kitty!**

I want to pet **it.**”



Key: modifier is included in antecedent.

Implication: May want to include the  
modifier whenever it's an option.

**one  
pretty kitty**

# Pronoun interpretation

syntax, semantics

another one



Regier & Gahl (2004), Pearl & Lidz (2009):

Filtering the direct evidence

Learning from it in more sophisticated ways



Noun'

pretty kitty



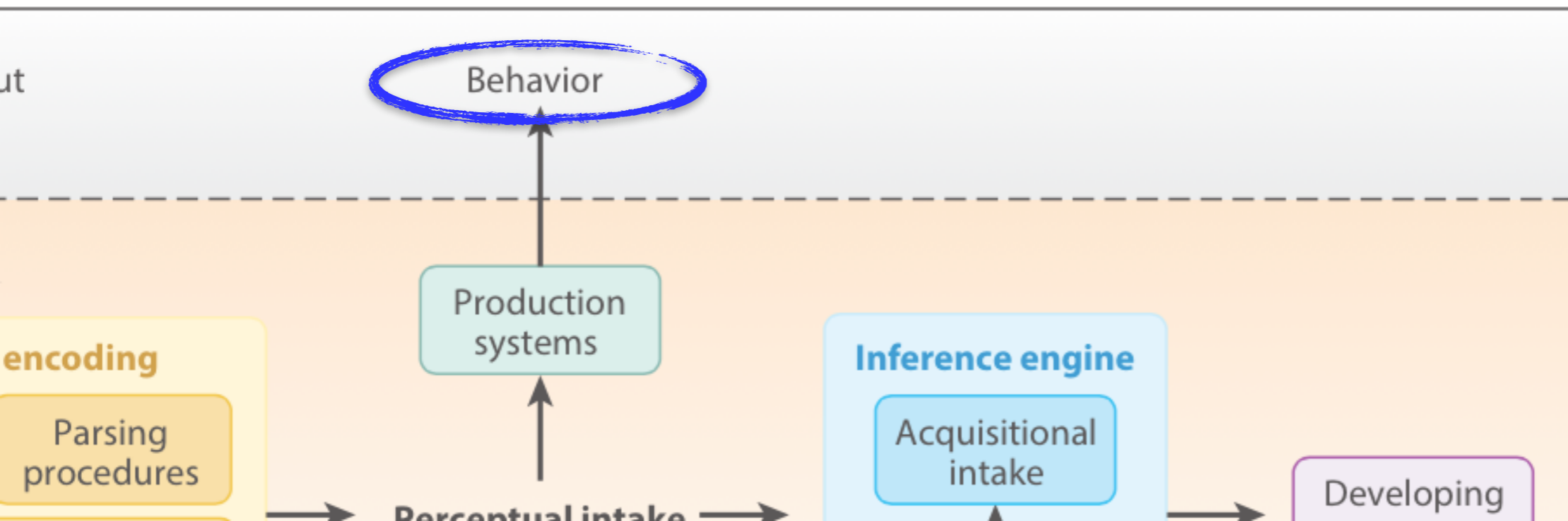
Pearl & Mis (2016):

Leveraging a broader set of data

Algorithmic-level implementation of these strategies

Evaluated on whether they matched

18-month-old looking preferences.



# Pronoun interpretation

syntax, semantics

another one



Regier & Gahl (2004), Pearl & Lidz (2009):

Filtering the direct evidence

Learning from it in more sophisticated ways



Noun'

pretty kitty

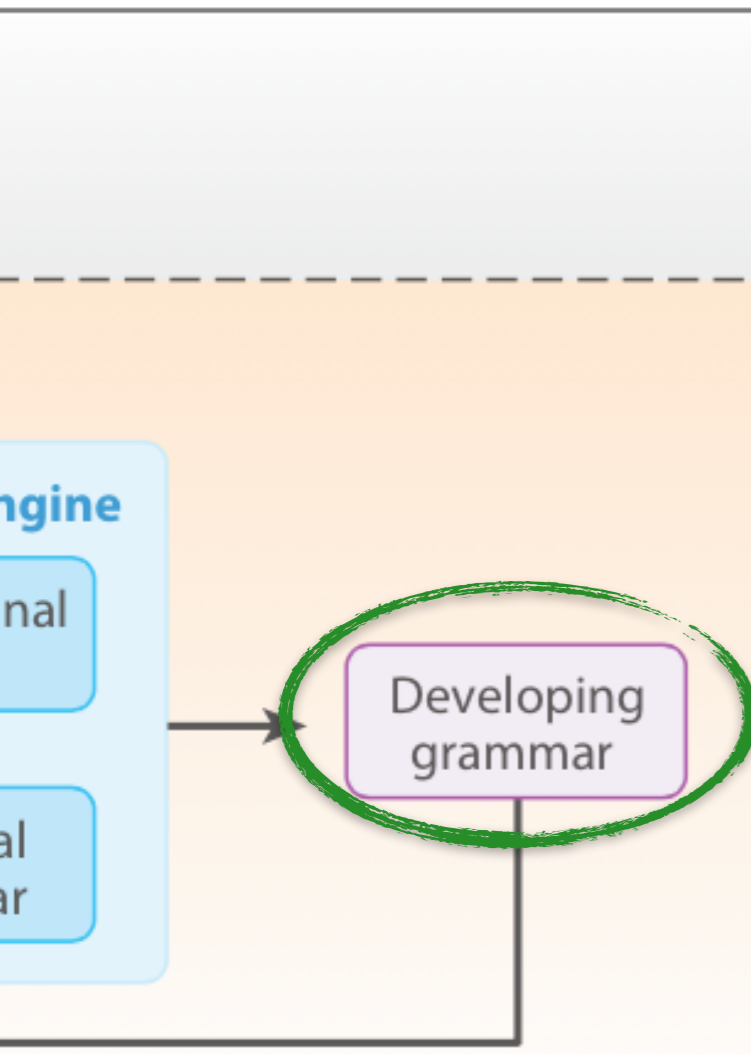


Pearl & Mis (2016):

Leveraging a broader set of data

## Algorithmic-level

Both were successful at generating the 18-month-old behavior. We can then look inside the modeled learners and see what the underlying representations were.



# Pronoun interpretation

syntax, semantics

another one



Noun'

pretty kitty



Learning from it in more sophisticated ways

Pearl & Mis (2016):  
Leveraging a broader set of data



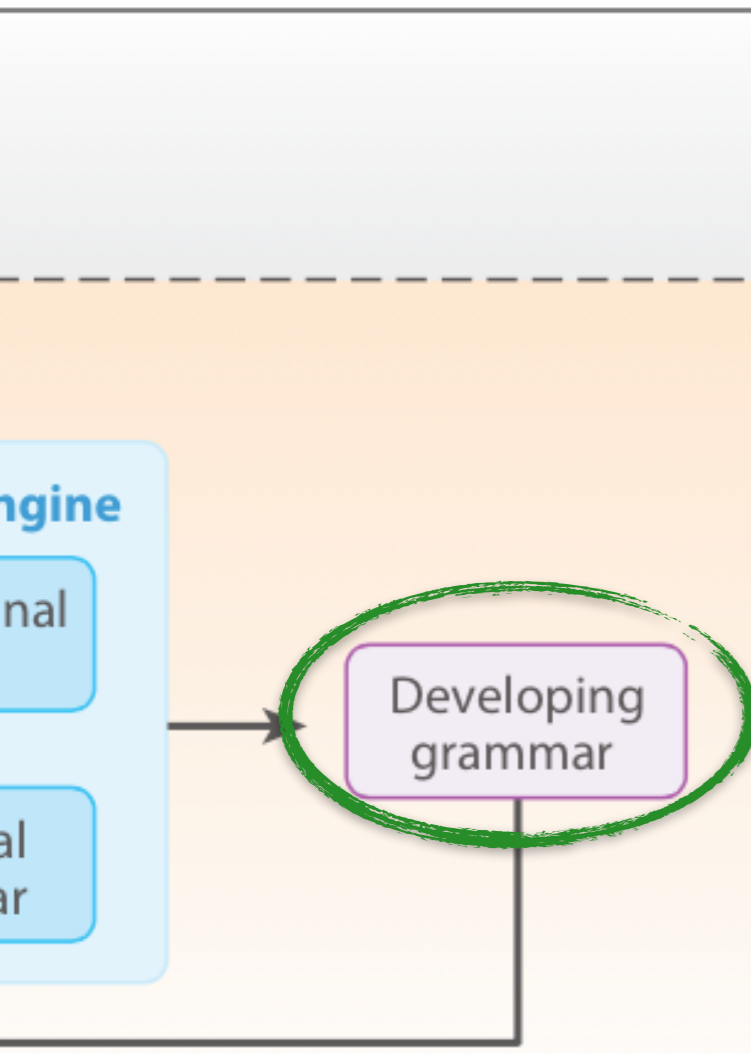
## Algorithmic-level

Regier & Gahl (2004), Pearl & Lidz (2009):  
Filtering the direct evidence

Adult representations

✓ Noun'  
pretty kitty

But...required additional situational context to be present to succeed.





# Pronoun interpretation

syntax, semantics

another one



## Learning from it in more sophisticated ways

Pearl & Mis (2016):  
Leveraging a broader set of data



Noun'  
pretty kitty



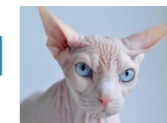
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Filtering the direct evidence

“Look – a pretty kitty!  
Oh, look – another one.”

Adult representations

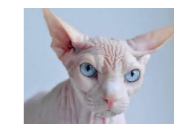
✓ Noun'  
pretty kitty

small

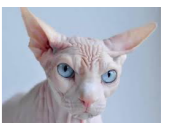


furry

But...required additional situational context to be present to succeed.



light-eyed

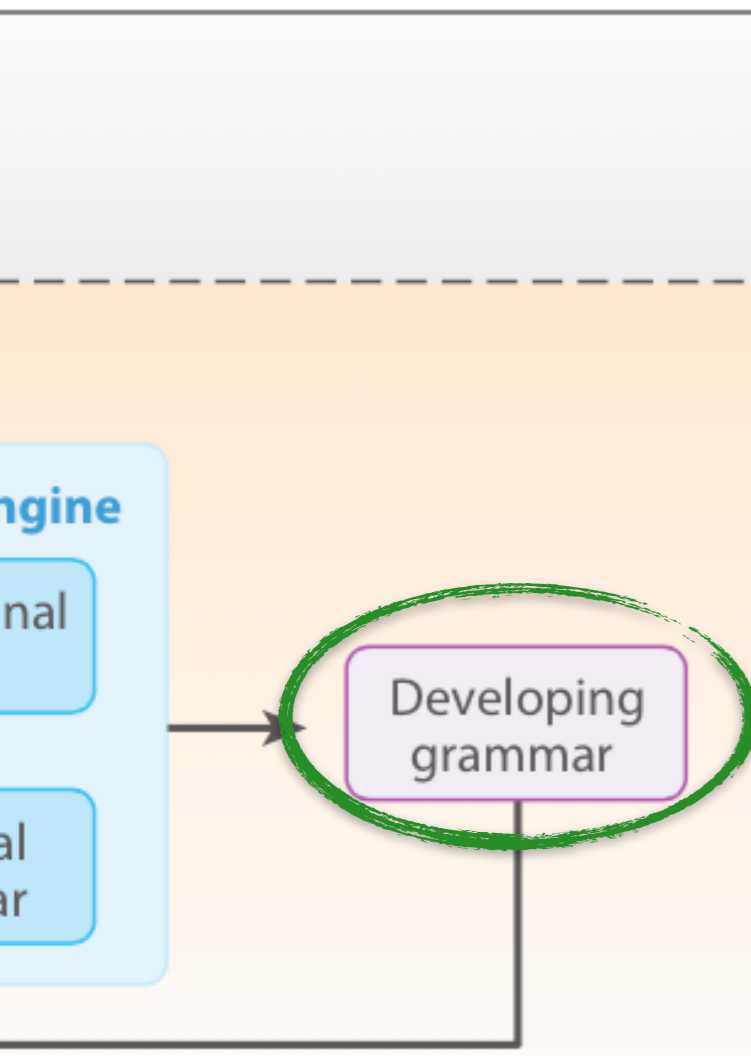


big-eared

Less robust

Needed to have a lot of alternative options so it's a suspicious coincidence that the referent is pretty if “pretty” wasn't actually included in the antecedent.

## Algorithmic-level



# Pronoun interpretation

syntax, semantics

another one



Regier & Gahl (2004), Pearl & Lidz (2009):

Filtering the direct evidence ✓ Less robust

Learning from it in more sophisticated ways



Noun'  
pretty kitty

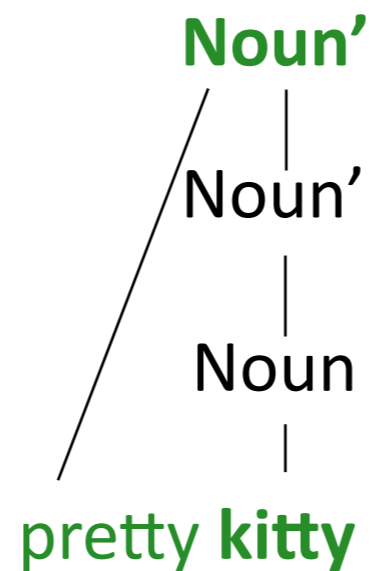
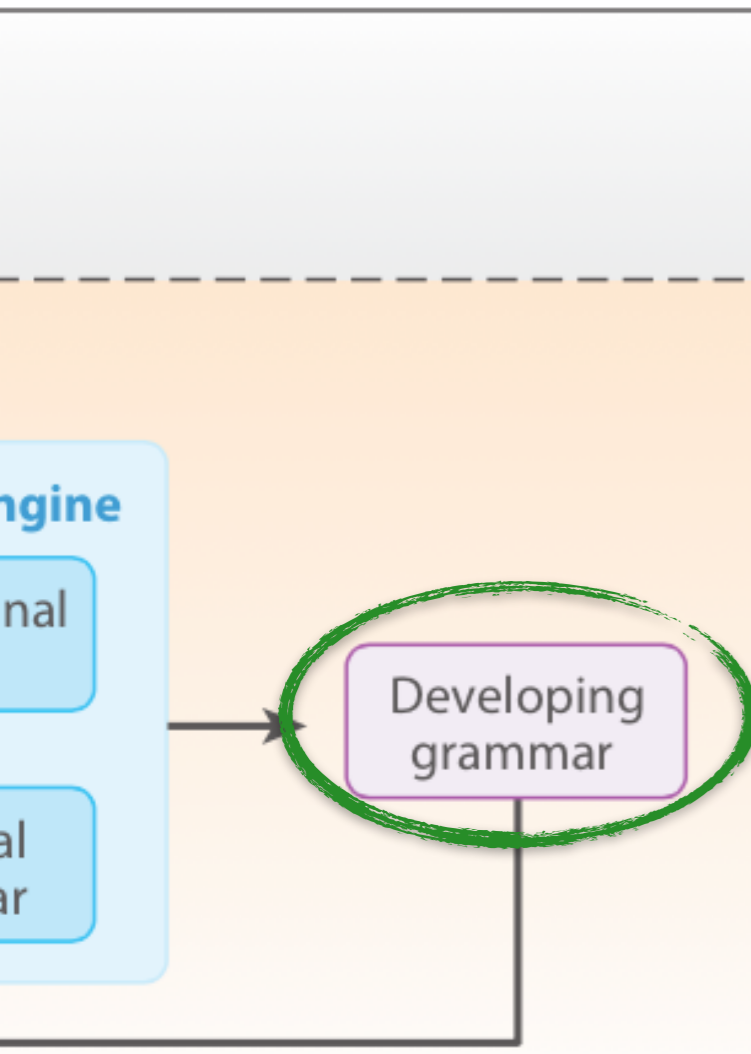
Pearl & Mis (2016):

Leveraging a broader set of data

Algorithmic-level

Immature representations

✓ Noun' only in certain linguistic contexts  
pretty kitty



“Look – a pretty kitty!  
Oh, look – another one.”

Noun'



# Pronoun interpretation

syntax, semantics

another one



Regier & Gahl (2004), Pearl & Lidz (2009):

Filtering the direct evidence ✓ Less robust

Learning from it in more sophisticated ways



Noun'  
pretty kitty

Pearl & Mis (2016):

Leveraging a broader set of data

Noun  
|  
kitty

Algorithmic-level

Immature representations

✓ Noun' only in certain linguistic contexts  
pretty kitty ✗ otherwise Noun



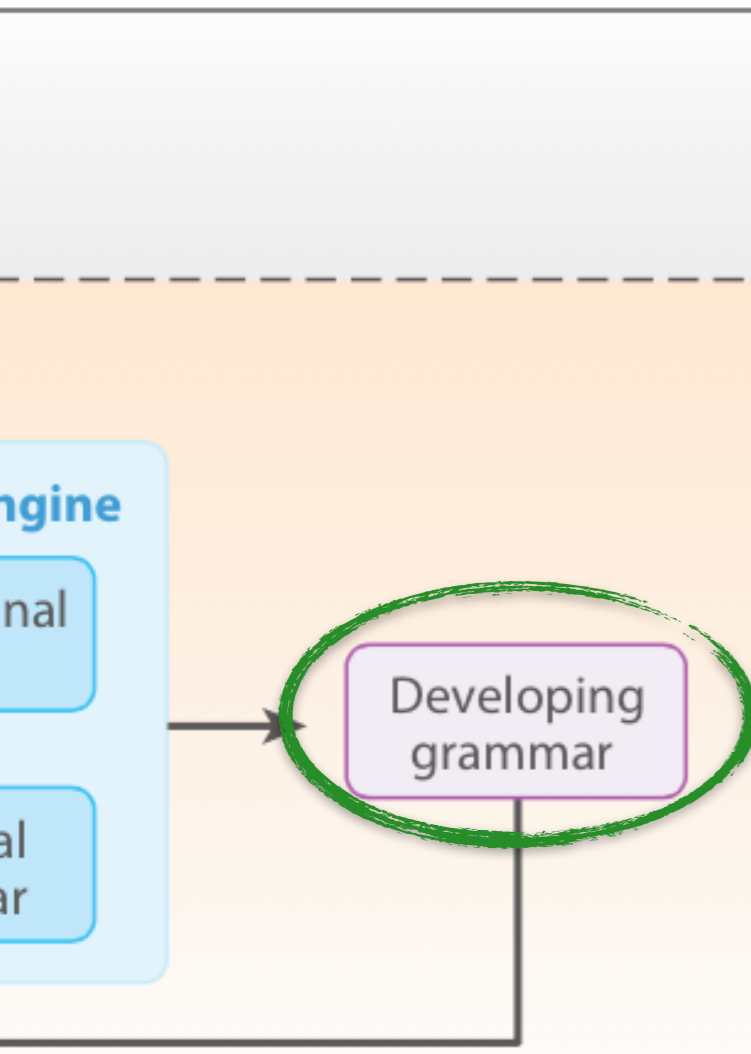
“Look – a **kitty!**”

Oh, look – another **one.**”

Noun

But...does this for pretty much any situational context.

More robust



# Pronoun interpretation

syntax, semantics

another one



Regier & Gahl (2004), Pearl & Lidz (2009):

Filtering the direct evidence ✓ Less robust

Learning from it in more sophisticated ways

Pearl & Mis (2016):

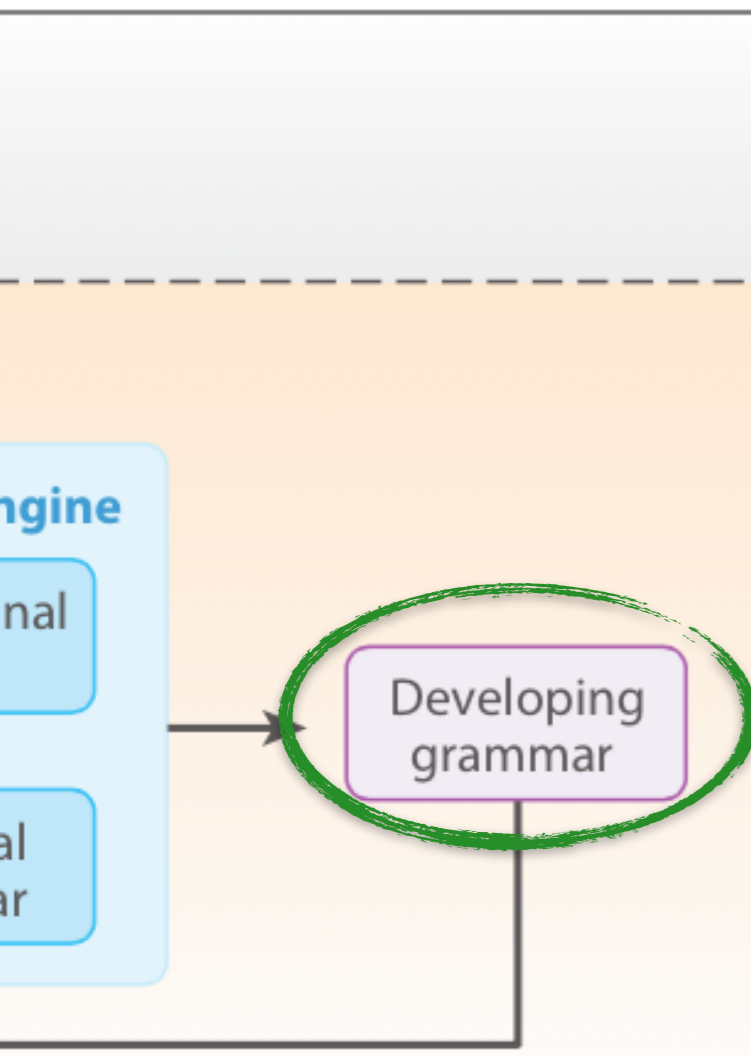
Leveraging a broader set of data ✗ ✓ More robust



Noun'  
pretty kitty



## Algorithmic-level



By modeling, we have two concrete proposals for how children learn the knowledge they do by 18 months.

This also motivates future experimental work to distinguish these two possibilities.



# Pronoun interpretation

syntax, semantics

another one



Noun'

pretty kitty



Regier & Gahl (2004), Pearl & Lidz (2009):

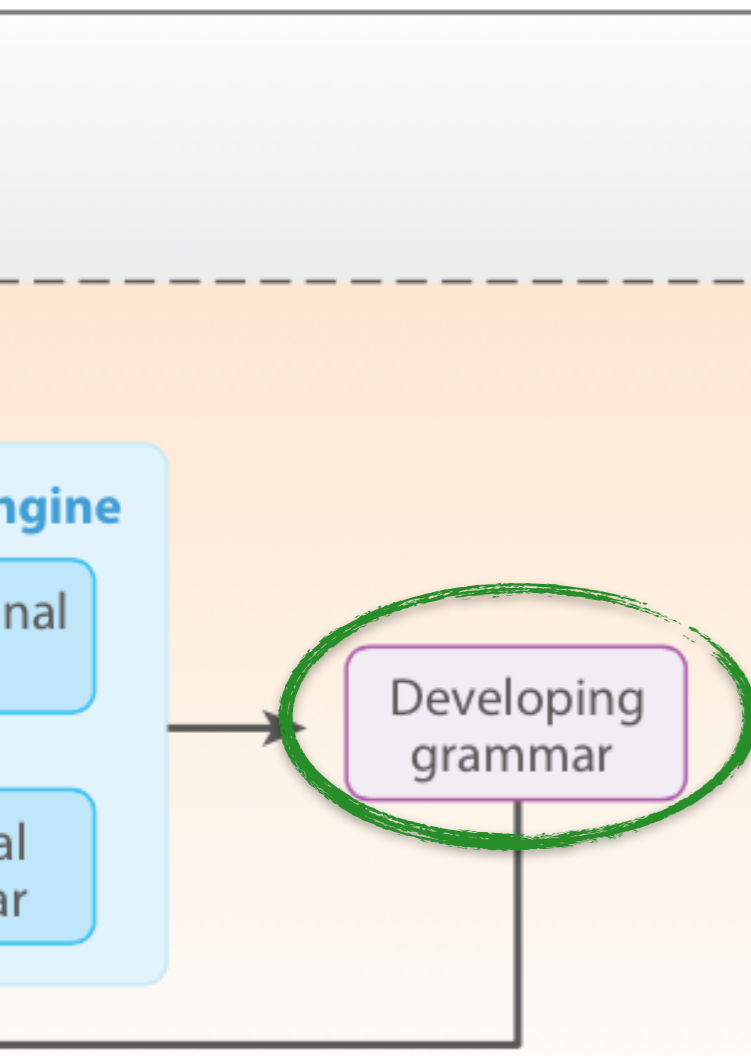
Filtering the direct evidence ✓ Less robust

Learning from it in more sophisticated ways

Pearl & Mis (2016):

Leveraging a broader set of data ✗ ✓ More robust

## Algorithmic-level



This also motivates future experimental work to distinguish these two possibilities.



“This kitty likes the **cup** of milk but not the **one** of water.”



Adults generally don't like this because it forces *one* to be category **Noun**.

# Pronoun interpretation

syntax, semantics

another one

Regier & Gahl (2004), Pearl & Lidz (2009):

Filtering the direct evidence ✓ Less robust

Learning from it in more sophisticated ways

Pearl & Mis (2016):

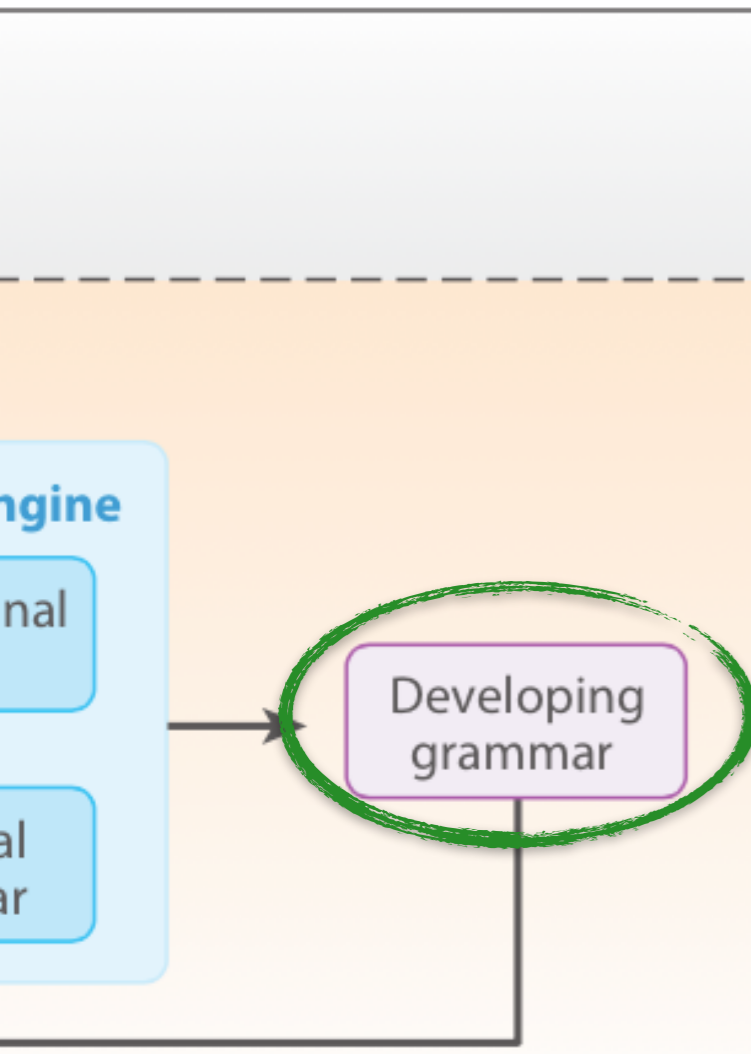
Leveraging a broader set of data ✗ ✓ More robust

Noun'

pretty kitty



## Algorithmic-level



This also motivates future experimental work to distinguish these two possibilities.



“This kitty likes the **cup** of milk but not the **one** of water.”

✗  
Noun

When do children have this same judgment? Is it before 18 months?

# Pronoun interpretation

syntax, semantics

another one

Noun'  
pretty kitty

Learning from it in more sophisticated ways

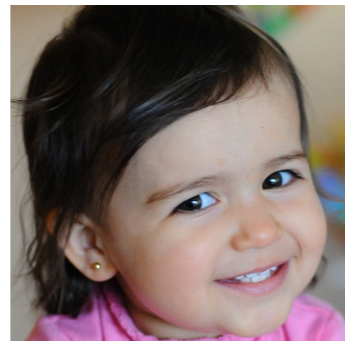
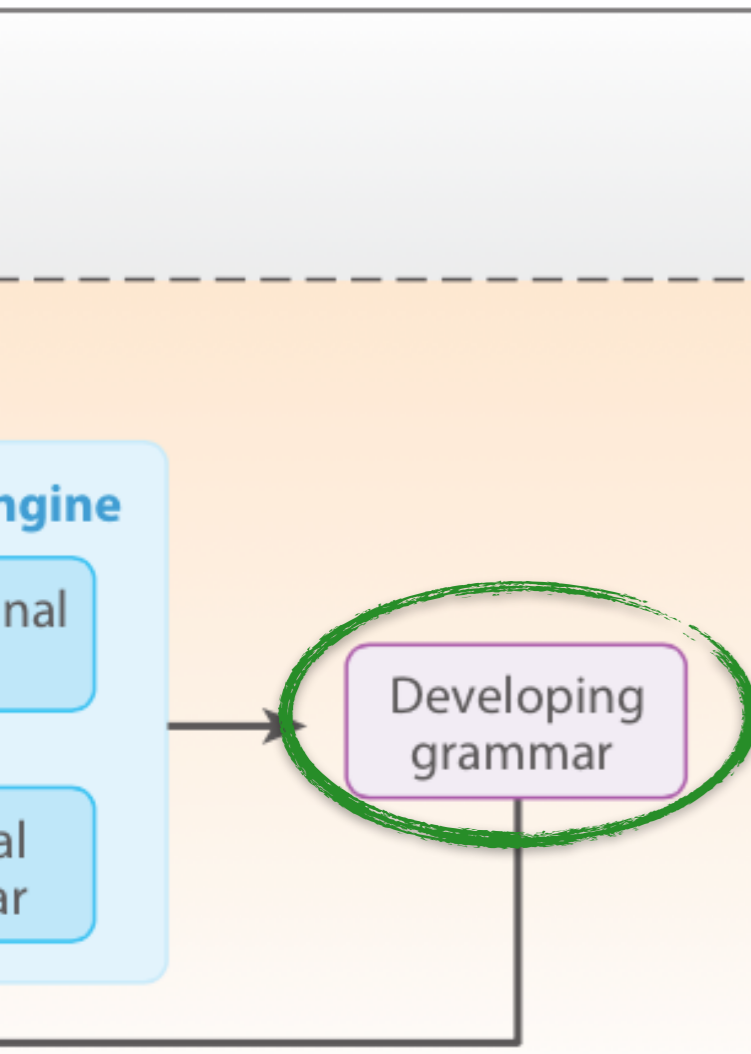
Pearl & Mis (2016):

Leveraging a broader set of data



More robust

## Algorithmic-level



By 18 months

Regier & Gahl (2004),  
Pearl & Lidz (2009):

Filtering the direct evidence



“This kitty likes the **cup** of milk  
but not the **one** of water.”

~~Noun~~

When do children have  
this same judgment? Is it  
before 18 months?

# Pronoun interpretation

syntax, semantics

another one

Noun'  
pretty kitty



**By 18 months**

Regier & Gahl (2004),  
Pearl & Lidz (2009):

**Filtering the direct evidence**



“This kitty likes the **cup** of milk  
but not the **one** of water.”

~~Noun~~

**Not by 18 months**

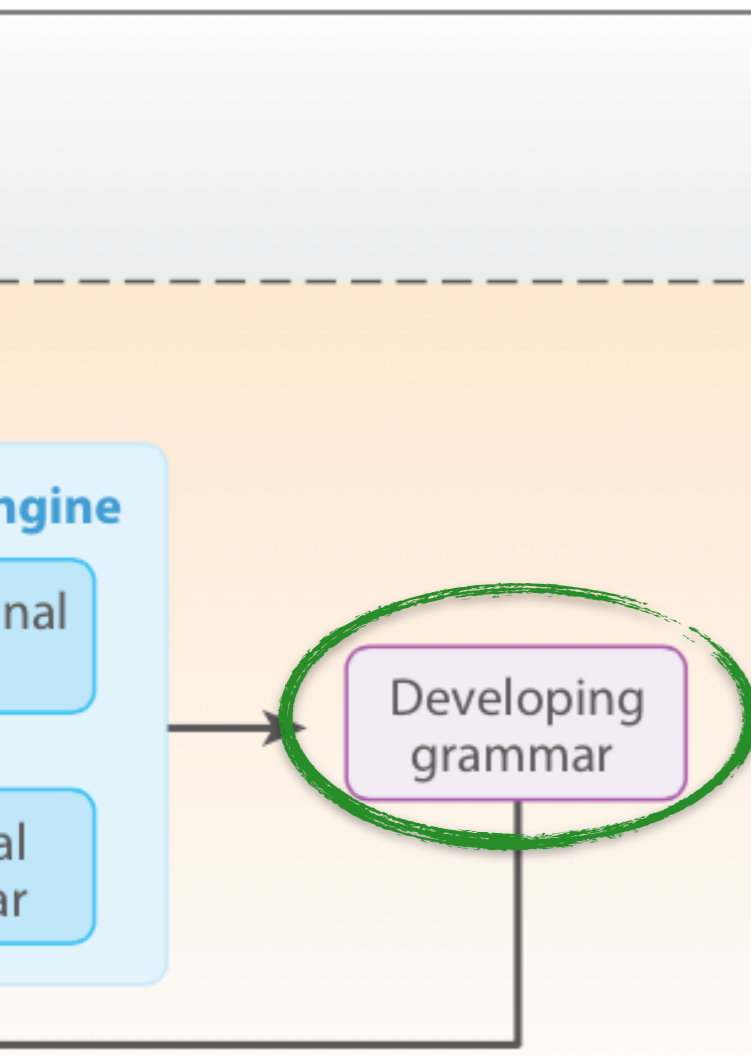
Pearl & Mis (2016):

**Leveraging a broader set of data**



**When do children have  
this same judgment? Is it  
before 18 months?**

**Algorithmic-level**





# Today's Plan:

## Computational models of syntactic acquisition

### I. Some non-parametric examples

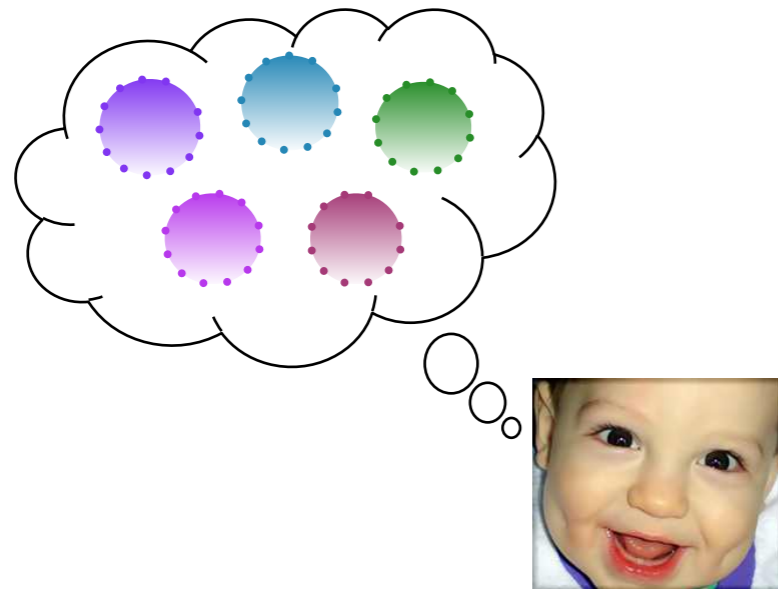
Who does  ...  is pretty?

**syntax** 

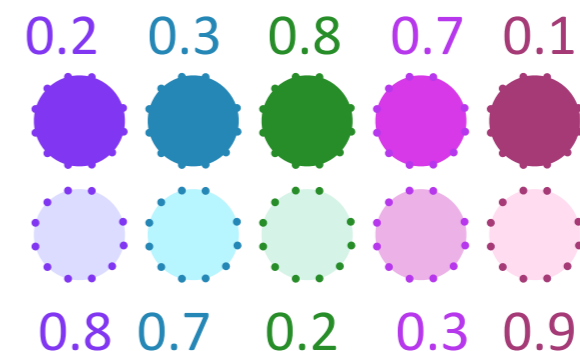
*another one*   

**syntax, semantics**

### II. About linguistic parameters



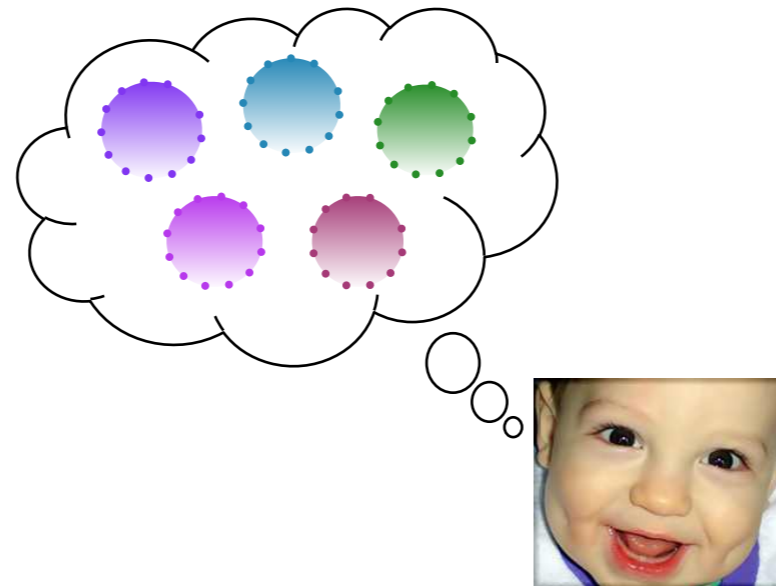
### III. Learning with parameters



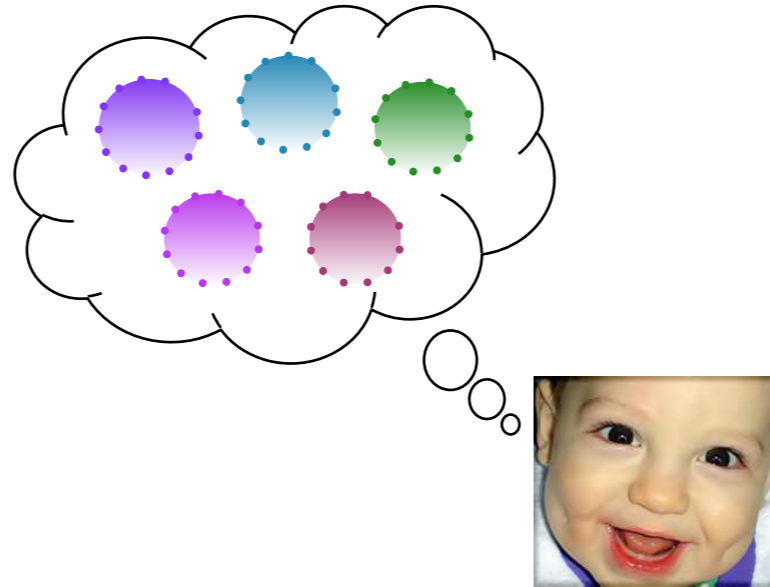
# Today's Plan:

## Computational models of syntactic acquisition

### II. About linguistic parameters



# About linguistic parameters



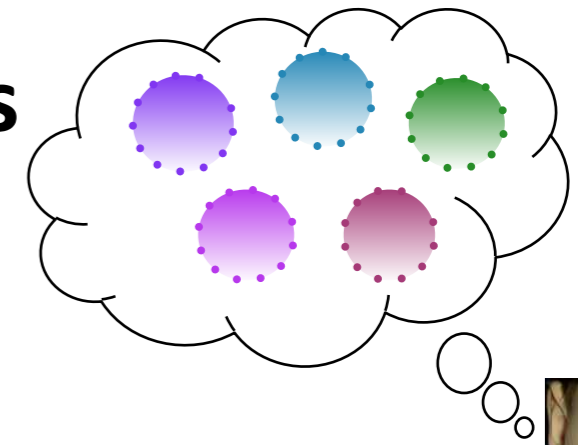
What are linguistic parameters?

How do they work?

What exactly are they supposed to do?



# About linguistic parameters



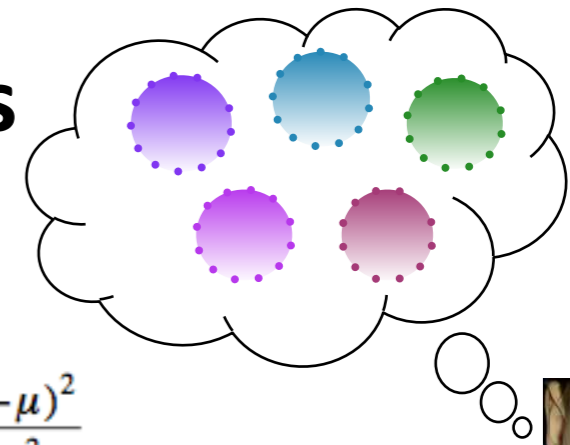
A parameter is meant to be something that can account for multiple observations in some domain.

Parameter for a statistical model: determines what the model predicts will be observed in the world in a variety of situations

Parameter for our mental (and linguistic) model: determines what *we* predict will be observed in the world in a variety of situations



# About linguistic parameters



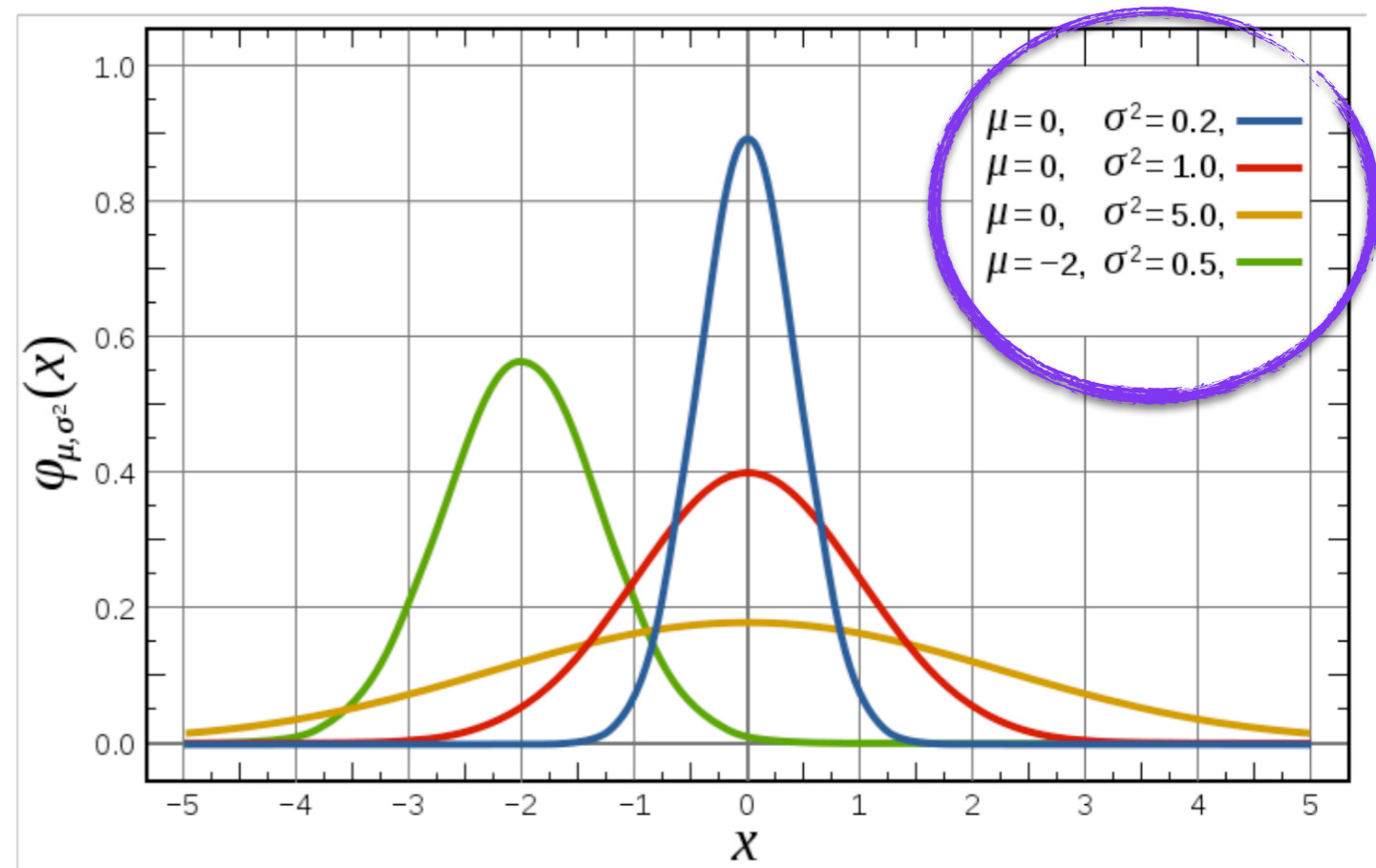
## Statistical parameter

$$\varphi_{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$

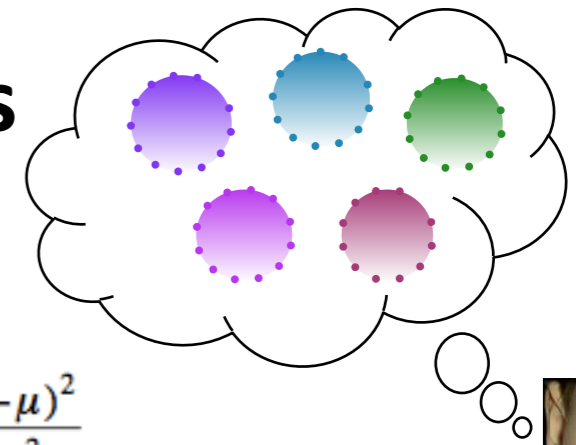
The normal distribution is a statistical model that uses **two parameters**:

- $\mu$  for the mean
- $\sigma$  for the standard deviation

If we know the **values of these parameters**, we can make predictions about the probability of data we rarely or never see.



# About linguistic parameters



Statistical parameter

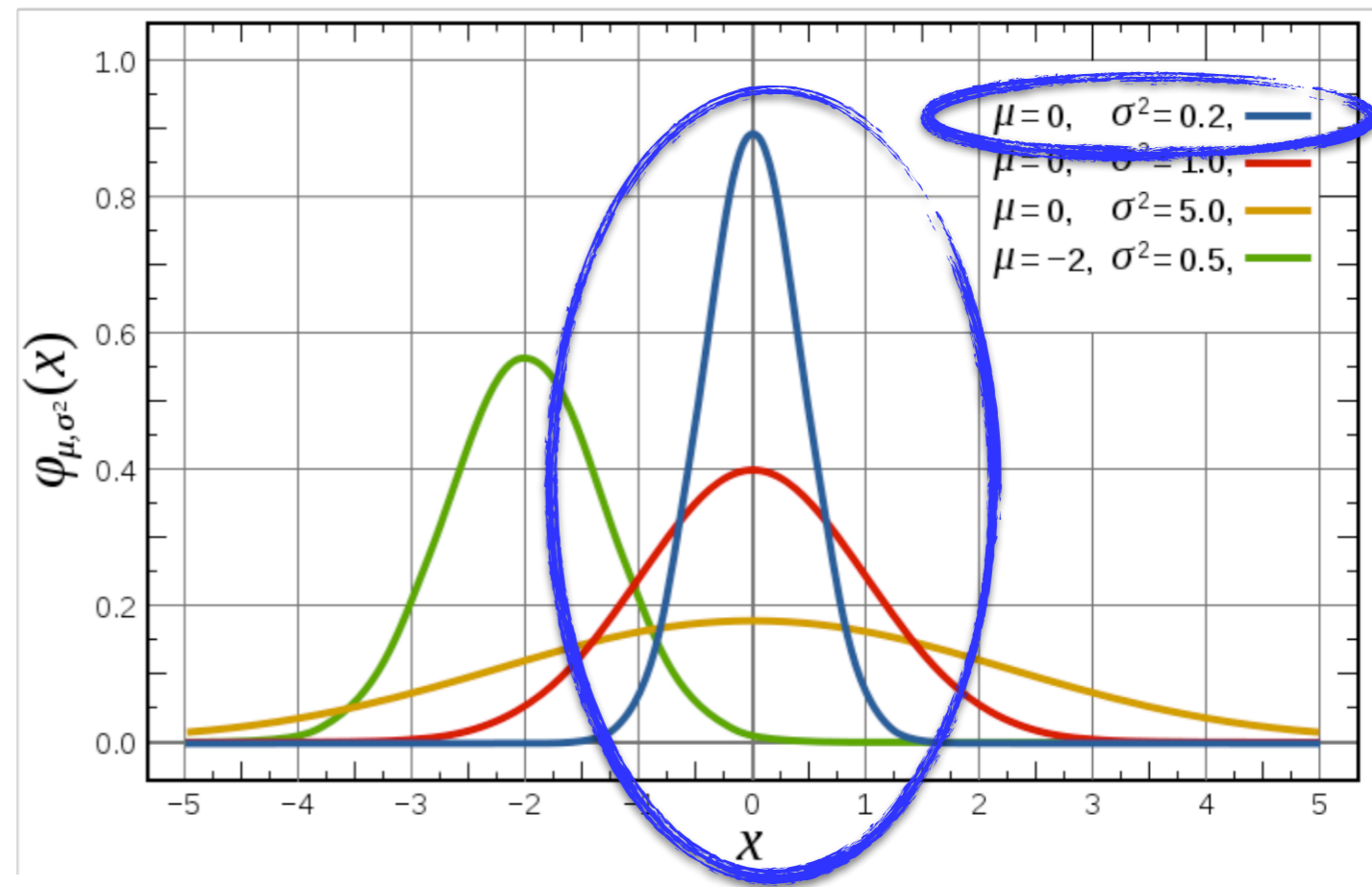
$\mu$  for the mean

$\sigma$  for the standard deviation

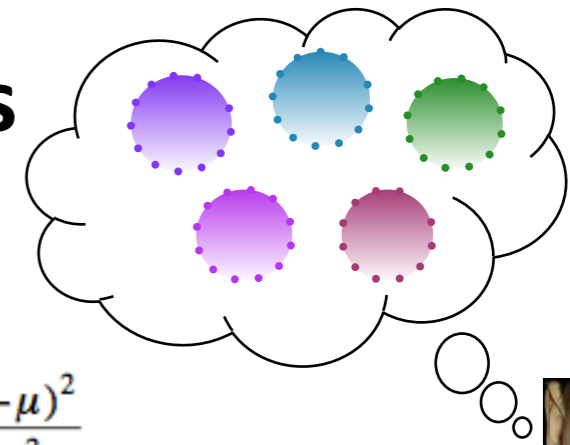
$$\varphi_{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$

Suppose this is a model of  
**how many minutes late I'll be**  
to class.

Let's use the model with  
 **$\mu = 0$  and  $\sigma^2 = 0.2$ .**



# About linguistic parameters



Statistical parameter

$\mu$  for the mean

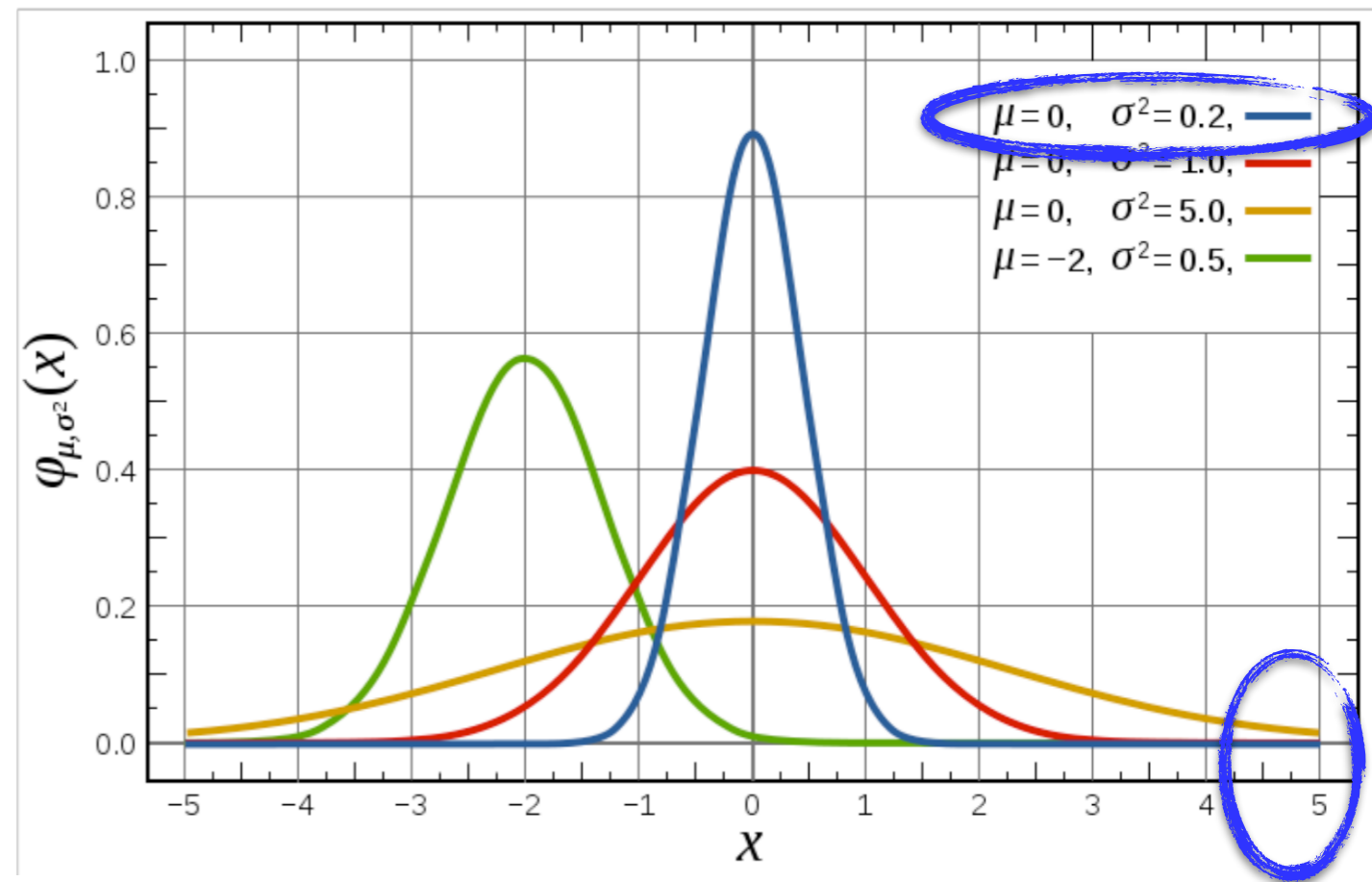
$\sigma$  for the standard deviation

Let's use the model with

$\mu = 0$  and  $\sigma^2 = 0.2$ .

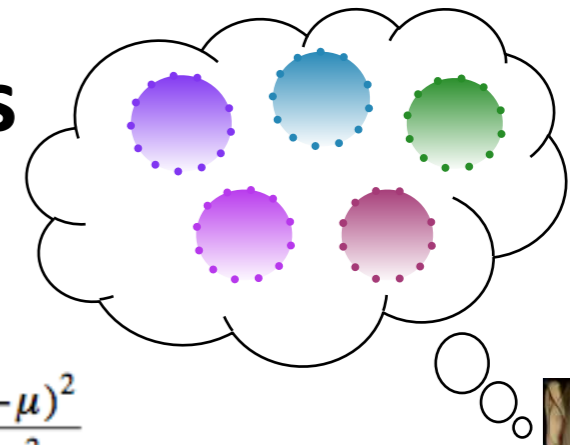
How probable is it that I'll be 5 minutes late, given these parameter values?  $\times$

$$\varphi_{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$



Not very probable!

# About linguistic parameters



Statistical parameter

$\mu$  for the mean

$\sigma$  for the standard deviation

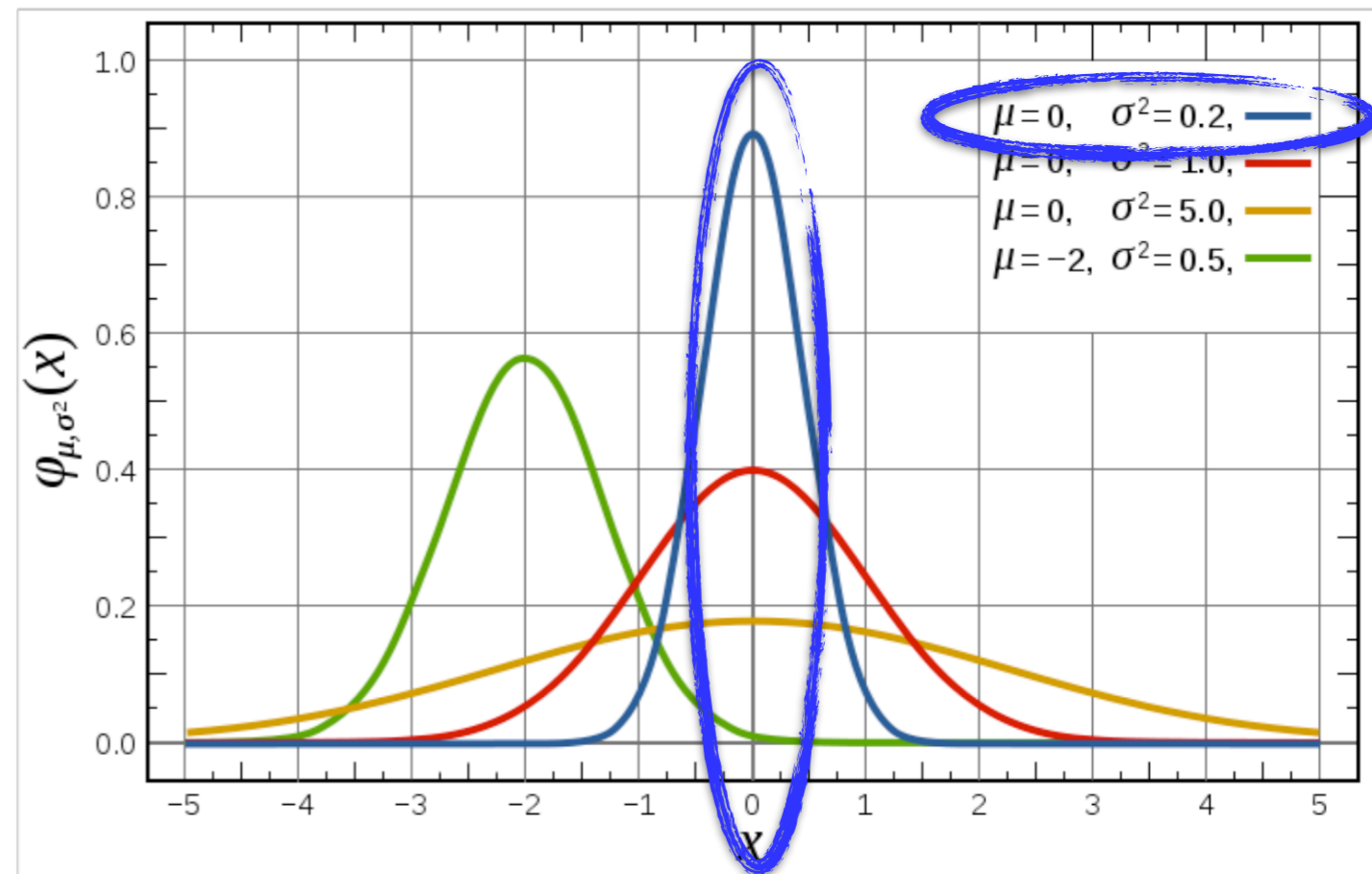
Let's use the model with

$\mu = 0$  and  $\sigma^2 = 0.2$ .

5 minutes late? ✗

What about right on time? ✓

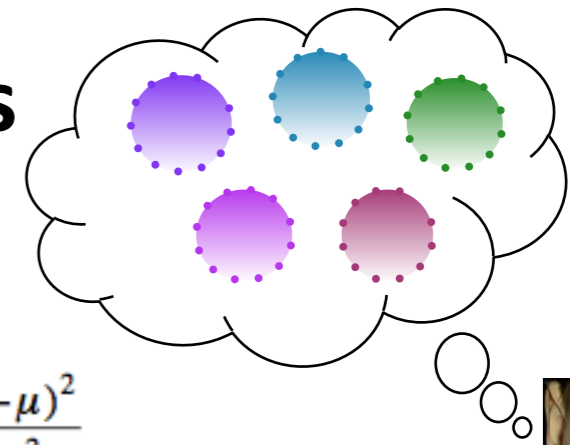
$$\varphi_{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$



Much more probable!



# About linguistic parameters



Statistical parameter

$\mu$  for the mean

$\sigma$  for the standard deviation

Let's use the model with

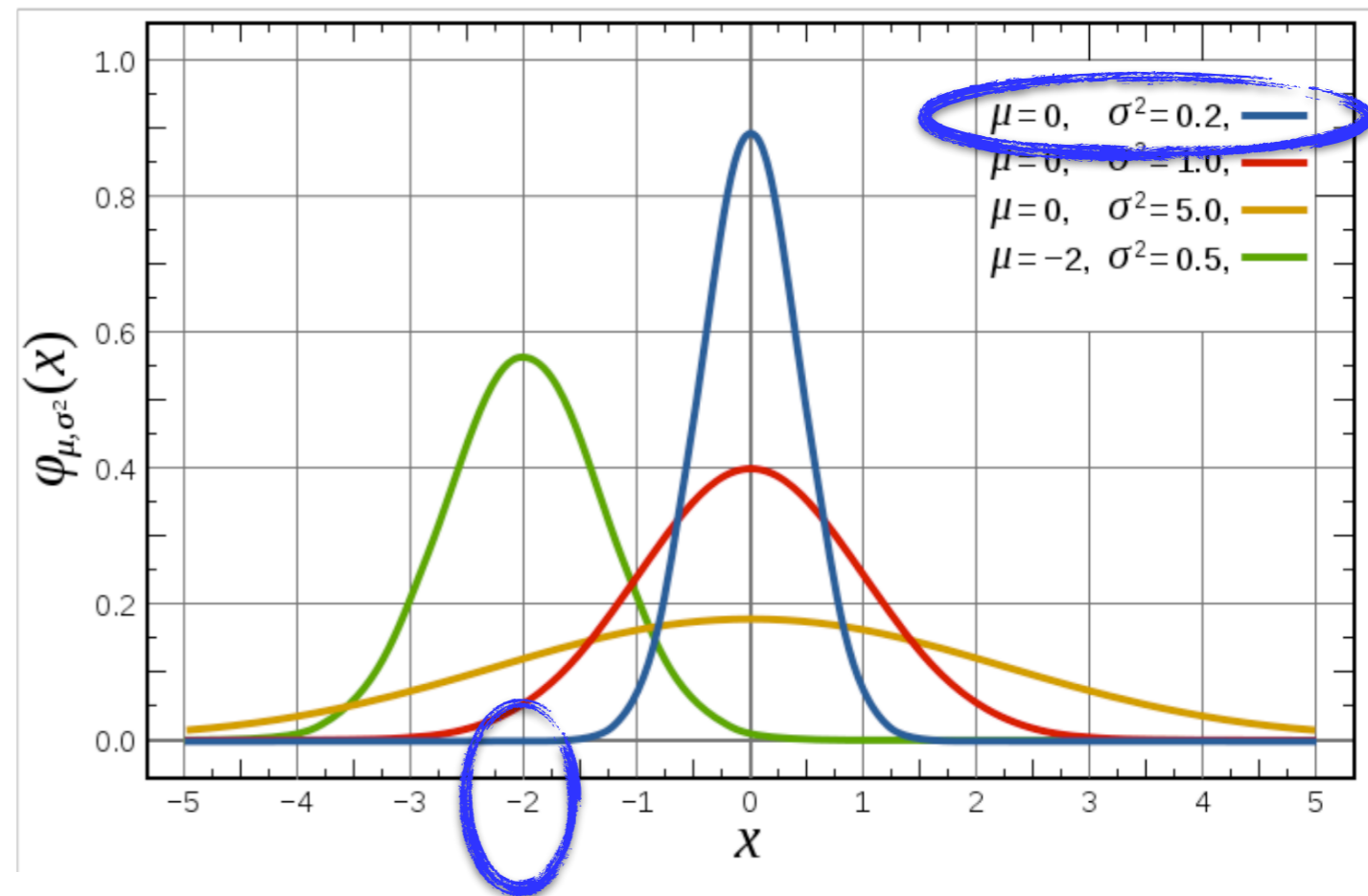
$\mu = 0$  and  $\sigma^2 = 0.2$ .

5 minutes late? ✗

On time? ✓

What about 2 minutes early? ✗

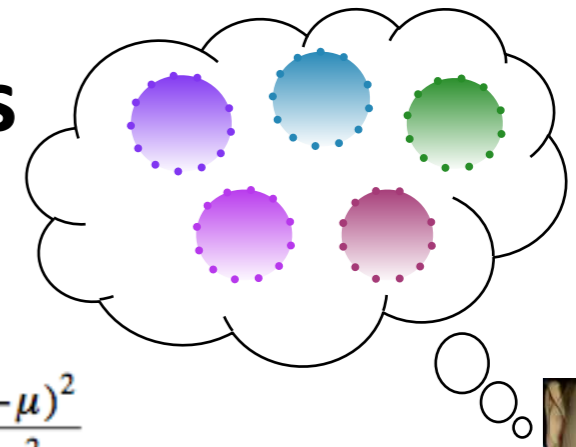
$$\varphi_{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$



We can tell this just by knowing the values of the two statistical parameters. These parameter values allow us to infer the probability of the observable behavior.

**Not very probable!**

# About linguistic parameters



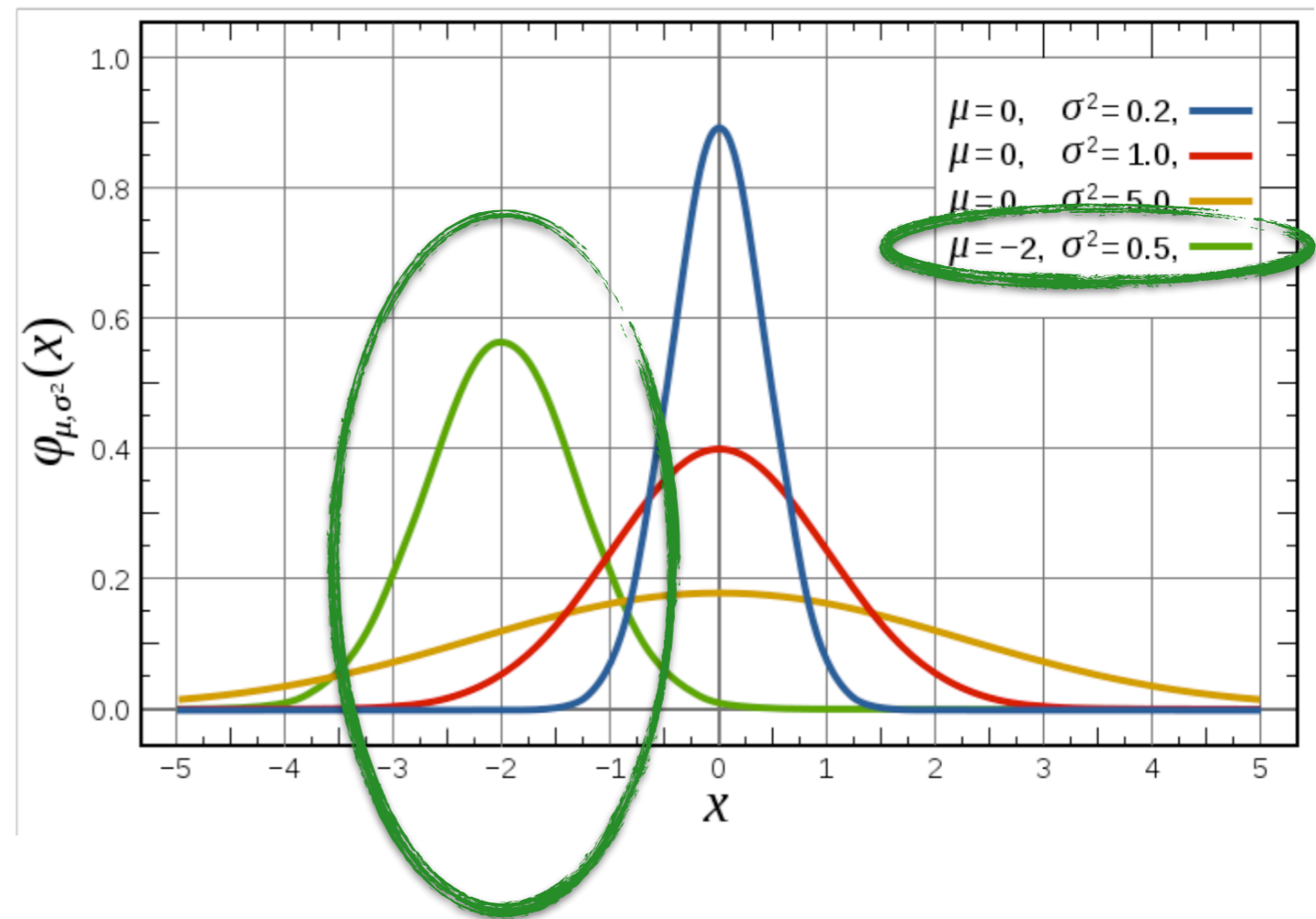
Statistical parameter

$\mu$  for the mean

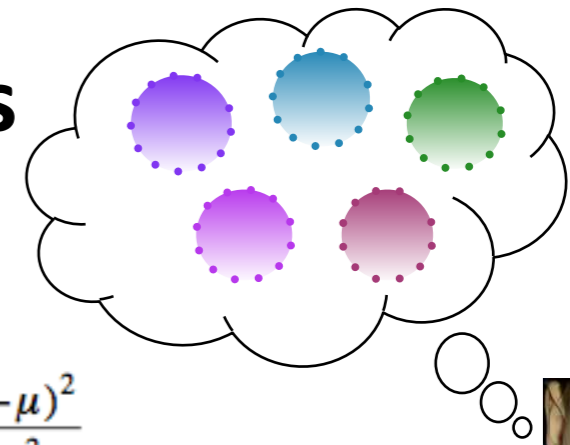
$\sigma$  for the standard deviation

Let's shift to the model  
with  $\mu = -2$  and  $\sigma^2 = 0.5$ .

$$\varphi_{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$



# About linguistic parameters



Statistical parameter

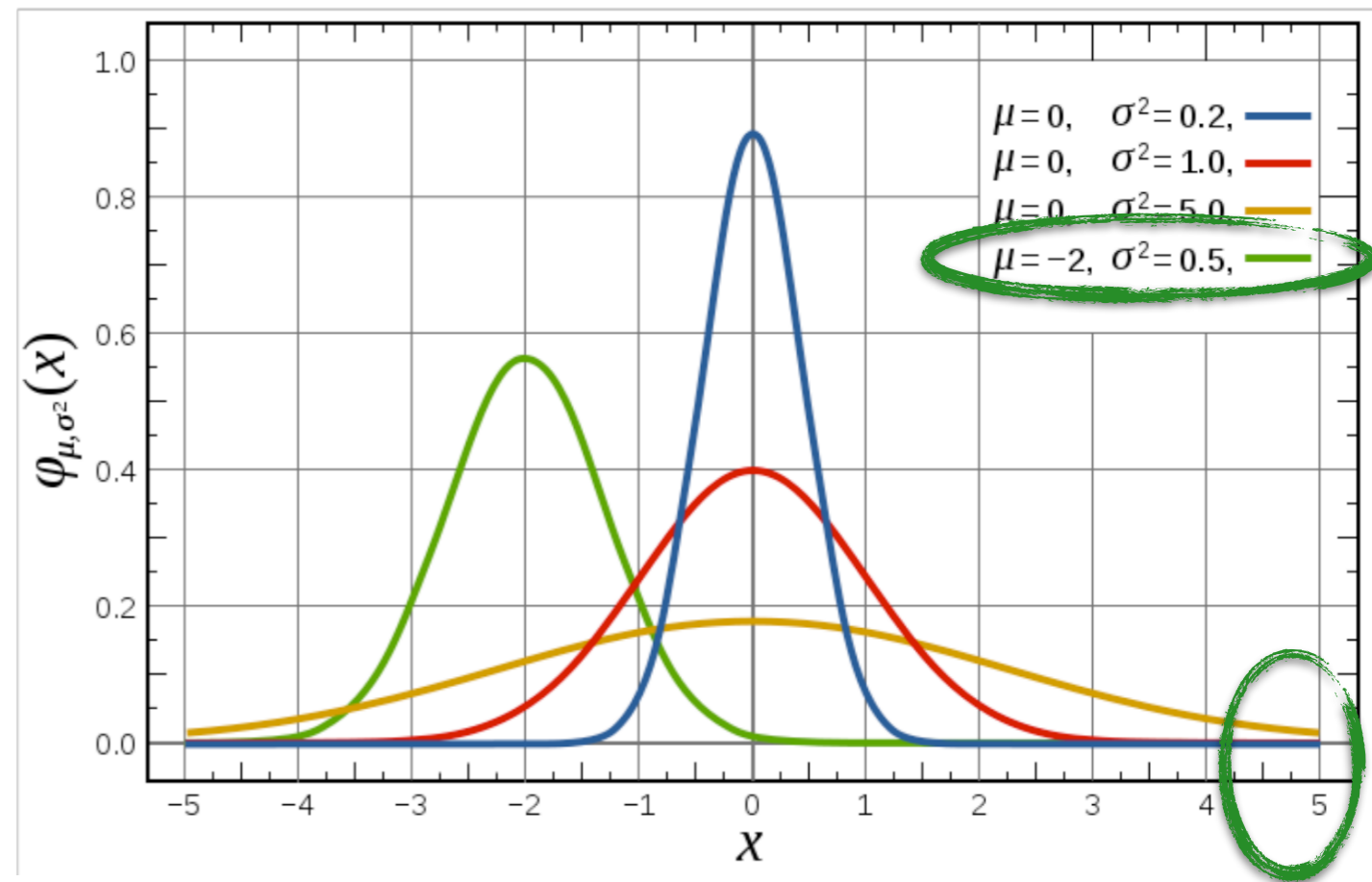
$\mu$  for the mean

$\sigma$  for the standard deviation

Let's shift to the model  
with  $\mu = -2$  and  $\sigma^2 = 0.5$ .

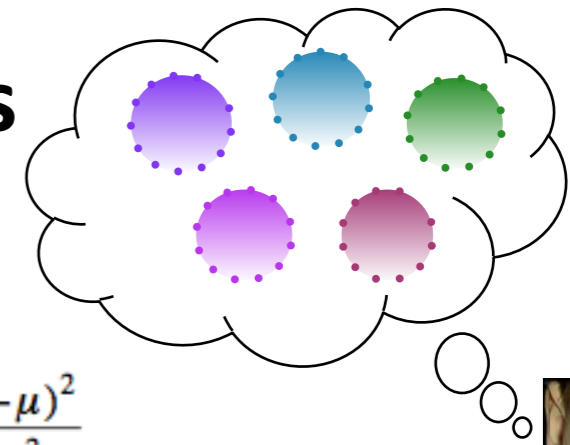
How probable is it that I'll  
be 5 minutes late, given  
these parameter values?  $\times$

$$\varphi_{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$



Not very probable!

# About linguistic parameters



Statistical parameter

$\mu$  for the mean

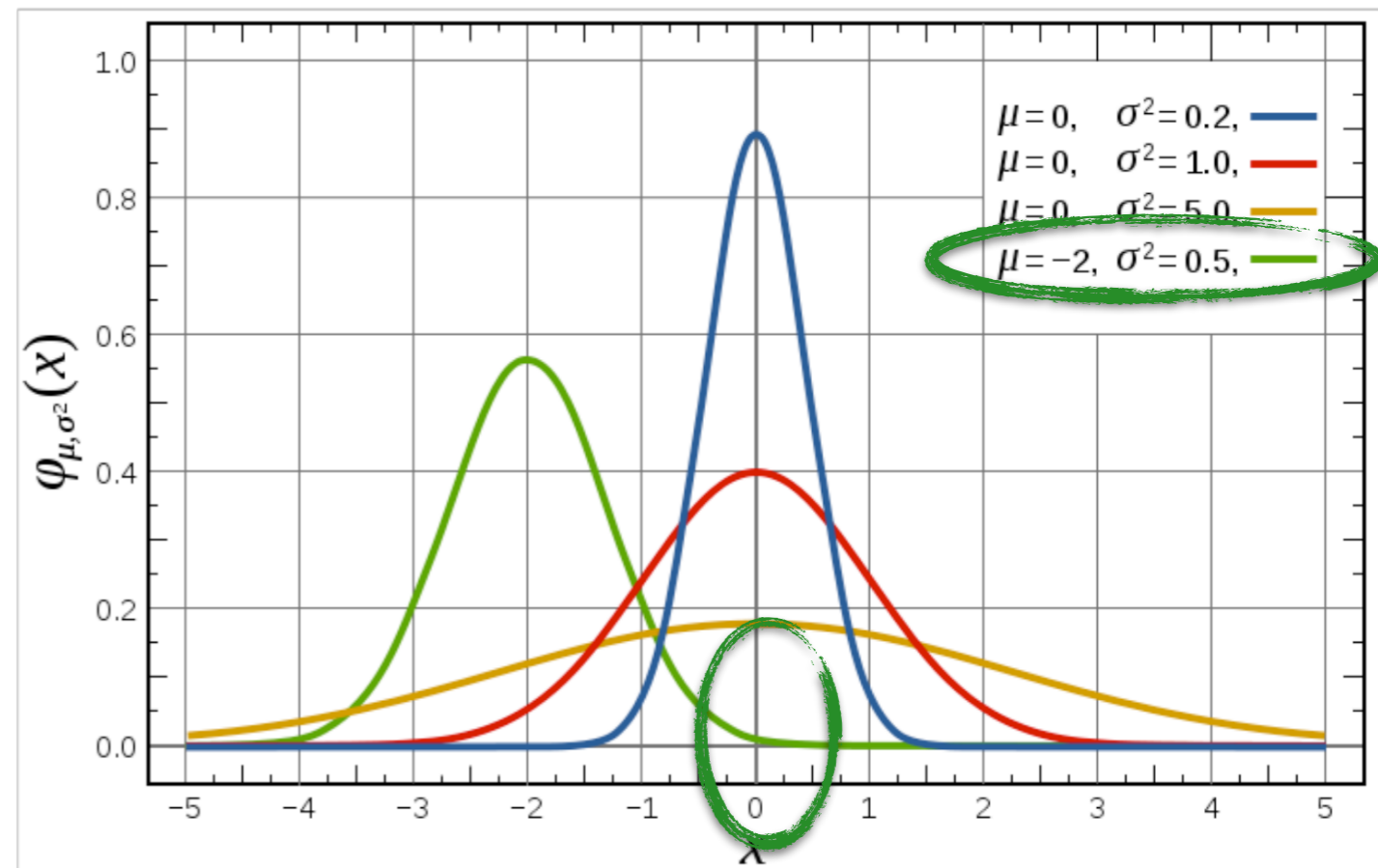
$\sigma$  for the standard deviation

Let's shift to the model  
with  $\mu = -2$  and  $\sigma^2 = 0.5$ .

5 minutes late? ✗

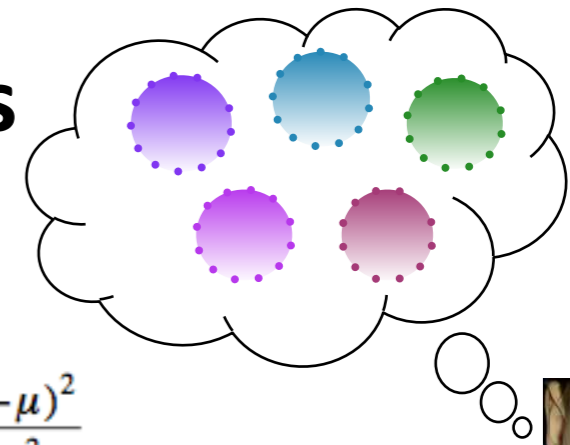
What about right on time? ✗

$$\varphi_{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$



Not very probable!

# About linguistic parameters



Statistical parameter

$\mu$  for the mean

$\sigma$  for the standard deviation

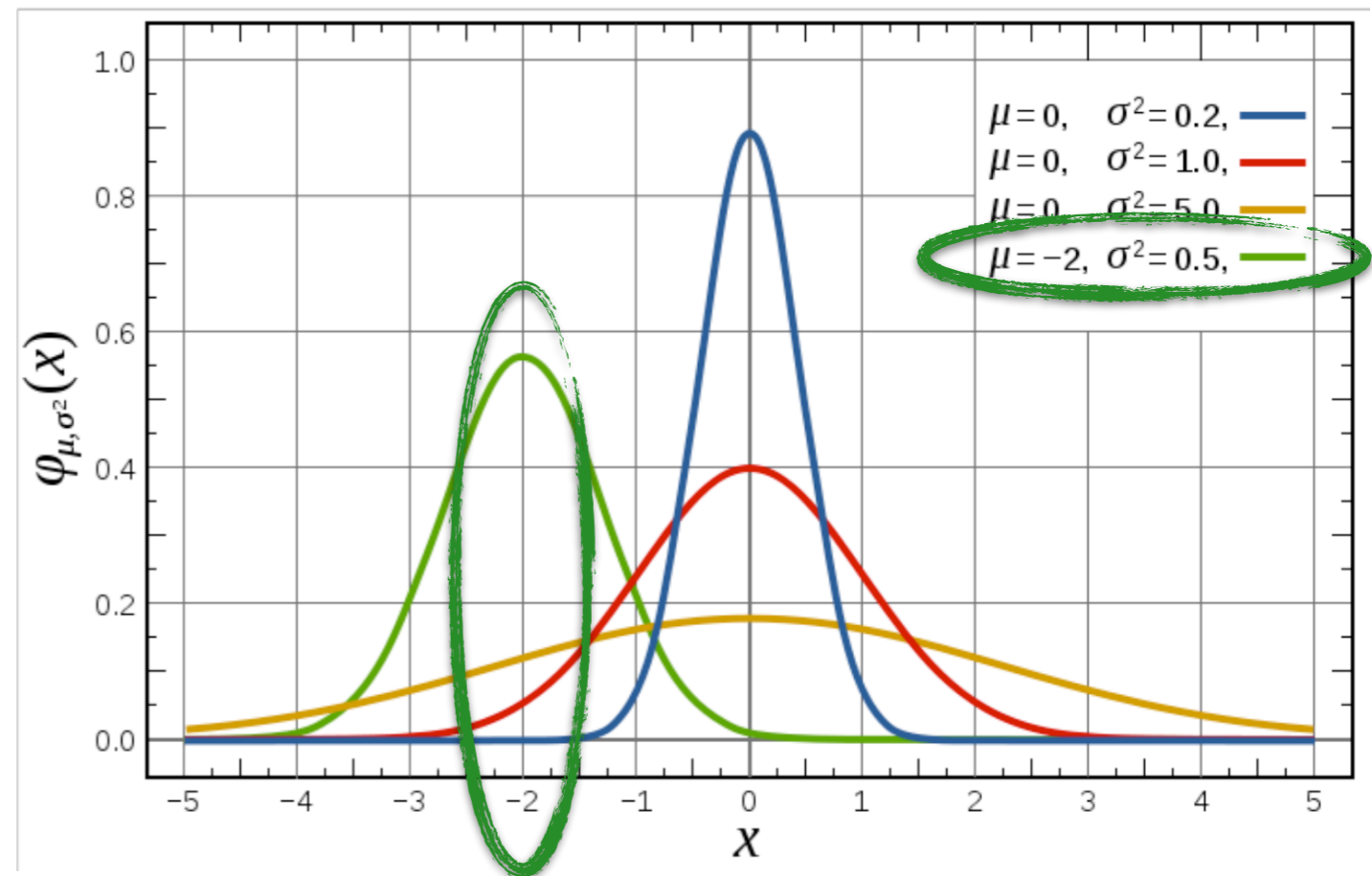
Let's shift to the model  
with  $\mu = -2$  and  $\sigma^2 = 0.5$ .

5 minutes late? ✗

On time? ✗

What about 2 minutes early? ✓

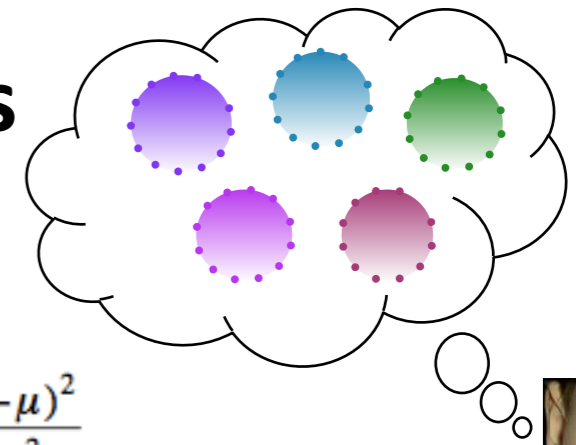
$$\varphi_{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$



**Much more probable!**

Changing the parameter values changes  
the behavior we predict we'll observe.

# About linguistic parameters



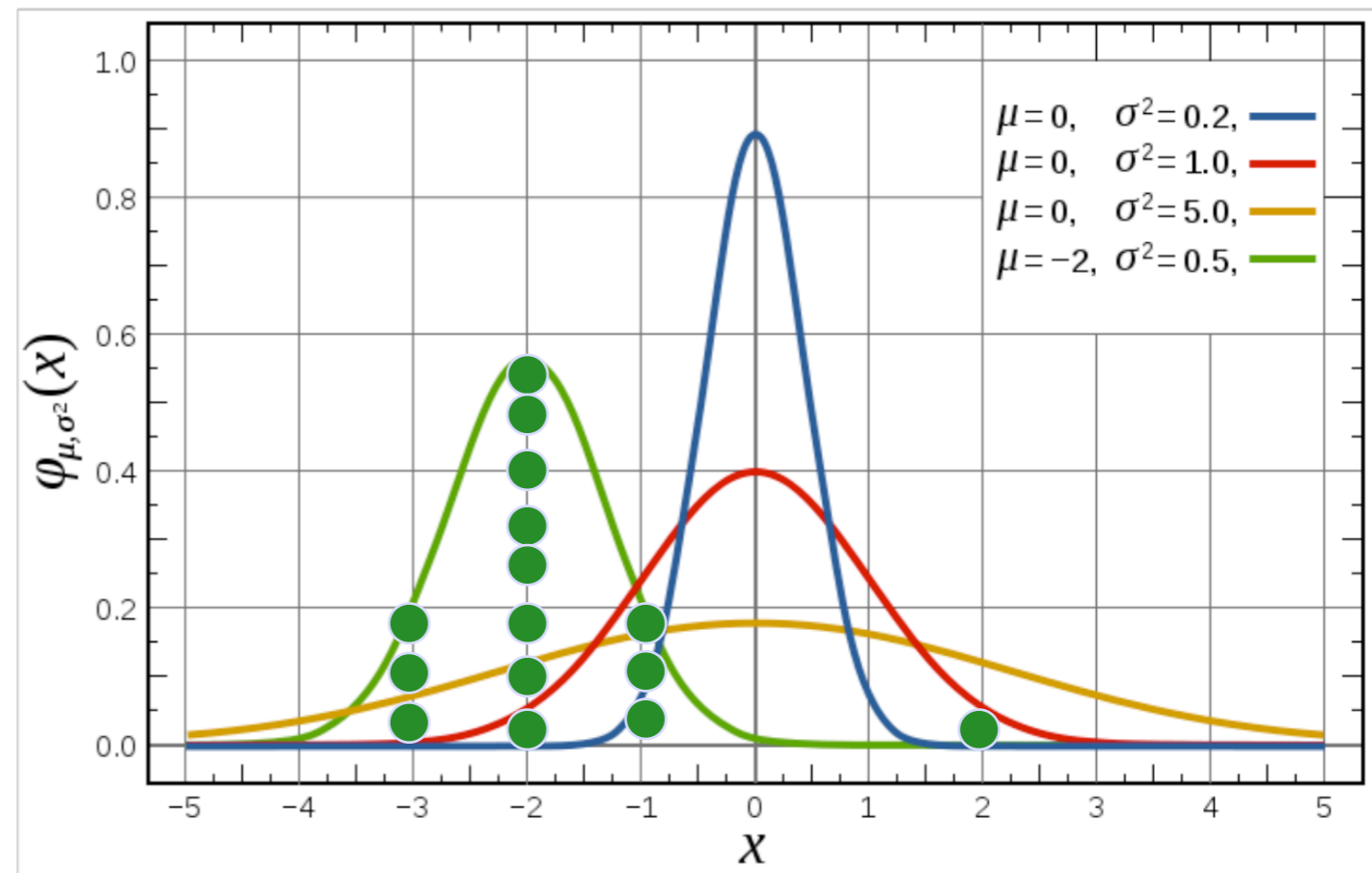
Statistical parameter

$\mu$  for the mean

$\sigma$  for the standard deviation

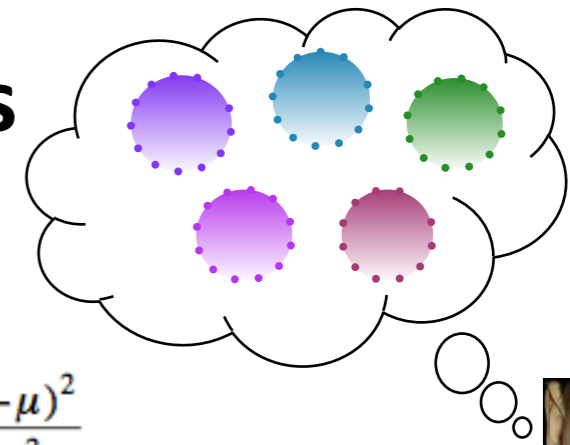
$$\varphi_{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$

Observing different quantities of data with particular values can tell us which values of  $\mu$  and  $\sigma^2$  are most likely, if we know we're trying to determine the values of  $\mu$  and  $\sigma^2$  in function  $\phi(X)$



Observing data points distributed like the green curve tells us that  $\mu$  is likely to be around -2 and  $\sigma^2$  is likely to be around 0.5.

# About linguistic parameters



Statistical parameter

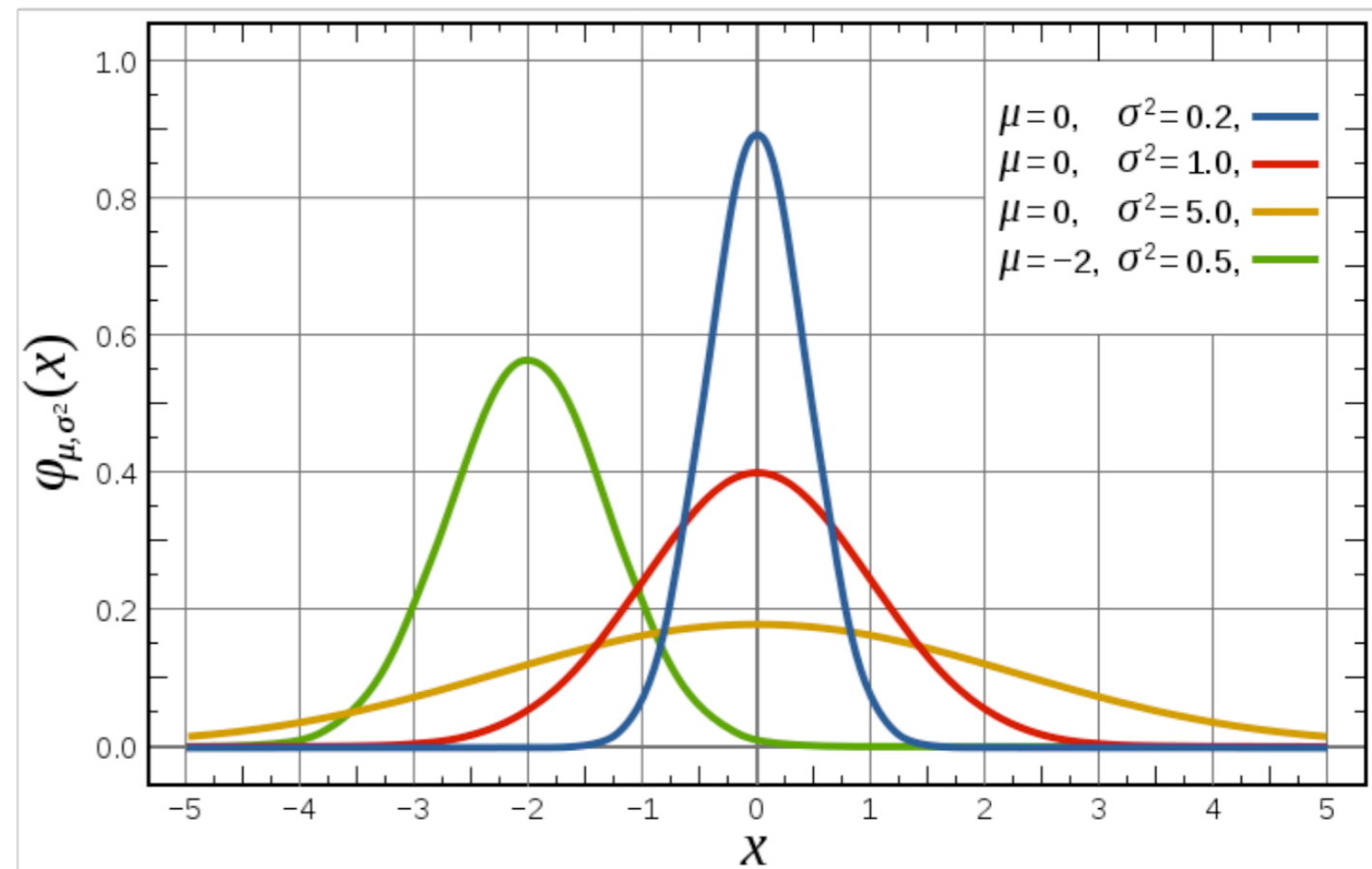
$\mu$  for the mean

$\sigma$  for the standard deviation

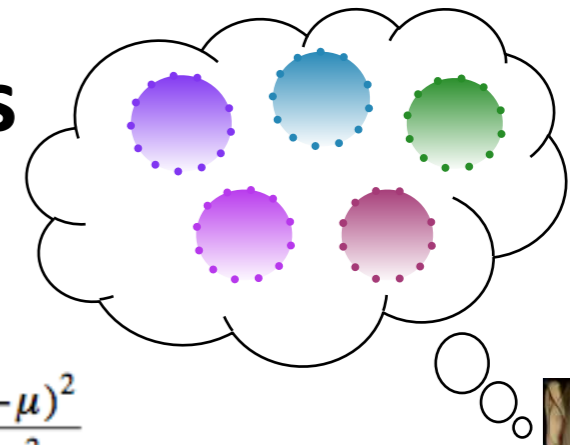
Important similarity to linguistic parameters:

**We don't see the process that generates the data, but only the data themselves.** This means that in order to form our expectations about  $X$ , we are, in effect, reverse engineering the observable data.

$$\varphi_{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$



# About linguistic parameters



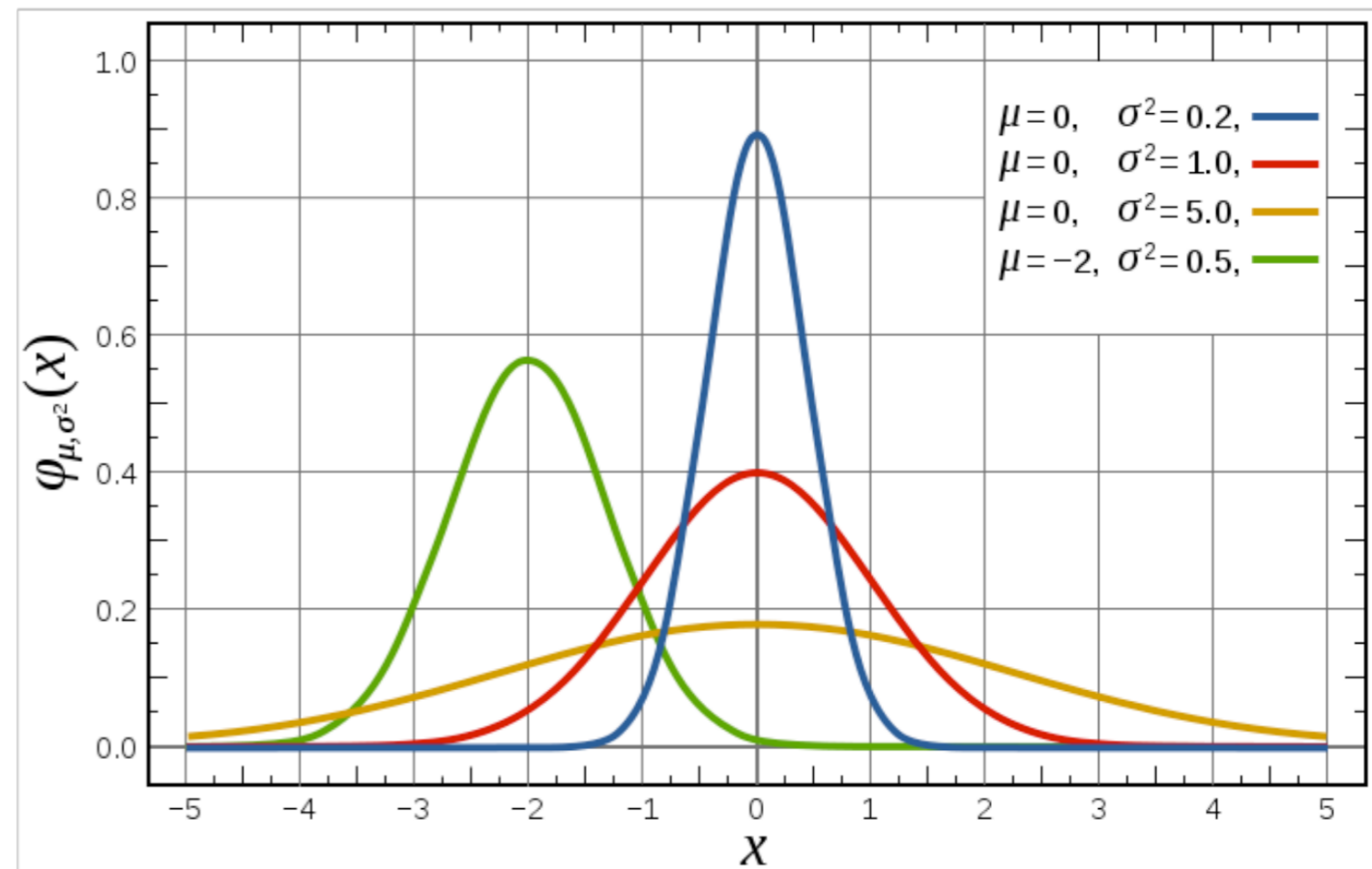
Statistical parameter

$\mu$  for the mean

$\sigma$  for the standard deviation

Our knowledge of the underlying function/principle that generates these data -  $\phi(X)$  - as well as the associated parameters -  $\mu$ , and  $\sigma^2$  - allows us to represent an infinite number of expectations about the behavior of variable  $X$ .

$$\varphi_{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$



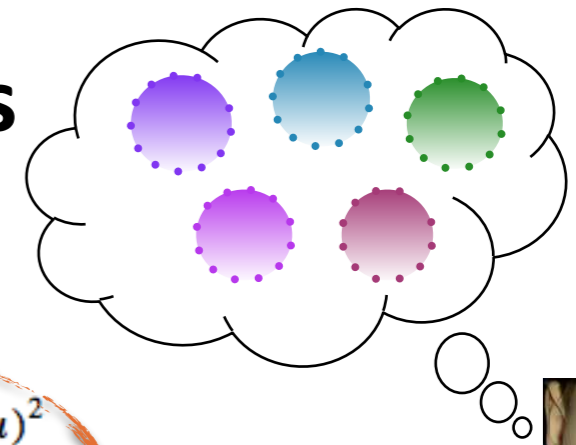


# About linguistic parameters

Comparison: **the equation's form**

– it's the statistical “principle”  
that explains the observed data.

$$\varphi_{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$



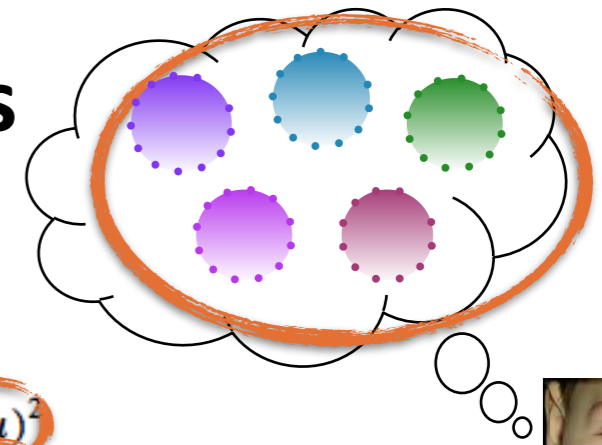
Both linguistic principles and linguistic parameters are often thought of as **innate domain-specific abstractions** that connect to many structural properties about language.

Linguistic **principles** correspond to the properties that are invariant across all human languages.

# About linguistic parameters

Comparison:  $\mu$  and  $\sigma^2$  determine the exact form of the curve that represents the probability of observing certain data. While different values for these parameters can produce many different curves, these curves share their underlying form due to the common invariant function.

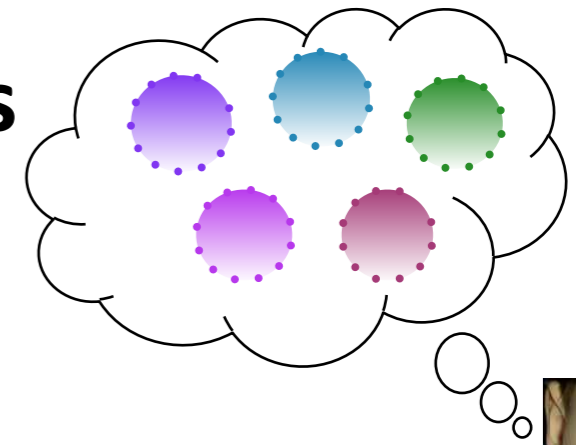
$$q^{\mu, \sigma^2}(X) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(X-\mu)^2}{2\sigma^2}}$$



Both linguistic principles and linguistic parameters are often thought of as **innate domain-specific abstractions** that connect to many structural properties about language.

Linguistic **parameters** correspond to the properties that vary across human languages

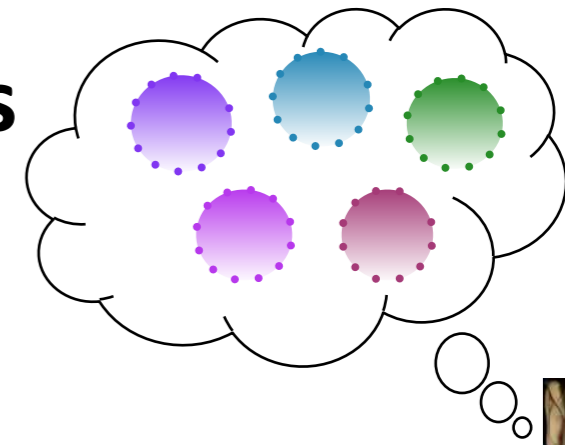
# About linguistic parameters for language acquisition



Parameters connecting to multiple structural properties is a very good thing from the perspective of someone trying to acquire language (like a child). This is because a child can learn about a parameter's value by observing **many different kinds of examples** in the language.



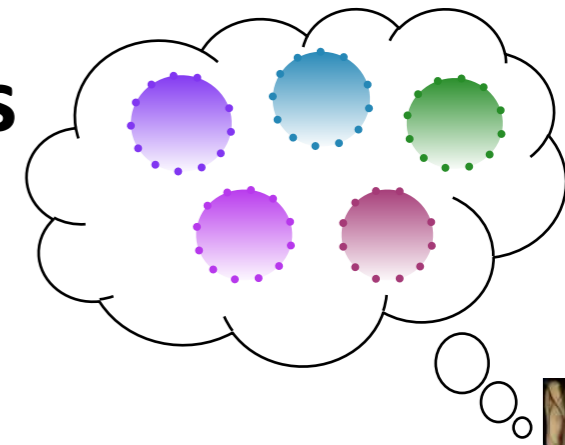
# About linguistic parameters for language acquisition



“The richer the deductive structure associated with a particular parameter, **the greater the range of potential ‘triggering’ data** which will be available to the child for the ‘fixing’ of the particular parameter” – Hyams (1987)



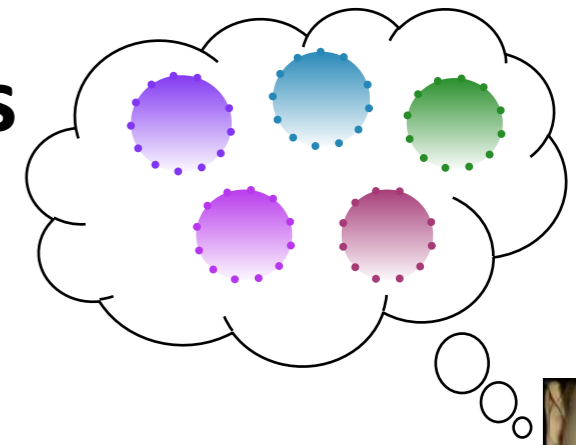
# About linguistic parameters for language acquisition



Parameters can be especially useful when a child is trying to learn the things about language structure that are **otherwise hard to learn**, perhaps because they are very complex properties themselves or because they appear very infrequently in the available data.



# About linguistic parameters for language acquisition



An issue: The observable data are often the result of a **combination of interacting parameters**.

This can make it hard to figure out what parameter values might have produced the observable data - even if the child already knows what the parameters are.

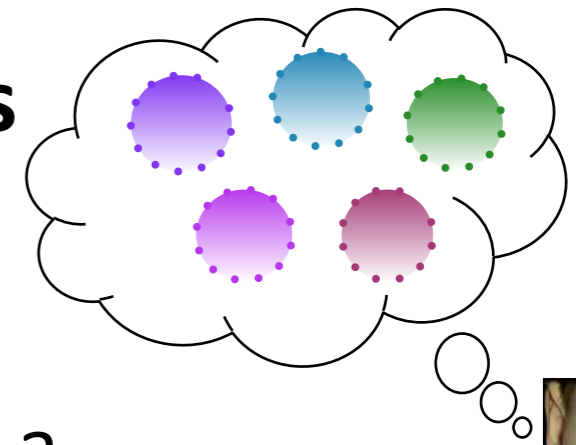
Observable data can be **ambiguous** for which parameter values they signal.

**Observable data**



Subject Verb Object

# About linguistic parameters for language acquisition



An issue: The observable data are often the result of a combination of interacting parameters.

Observable data can be ambiguous for which parameter values they signal.



Subject Verb Object

German

Subject Verb Subject Object Verb

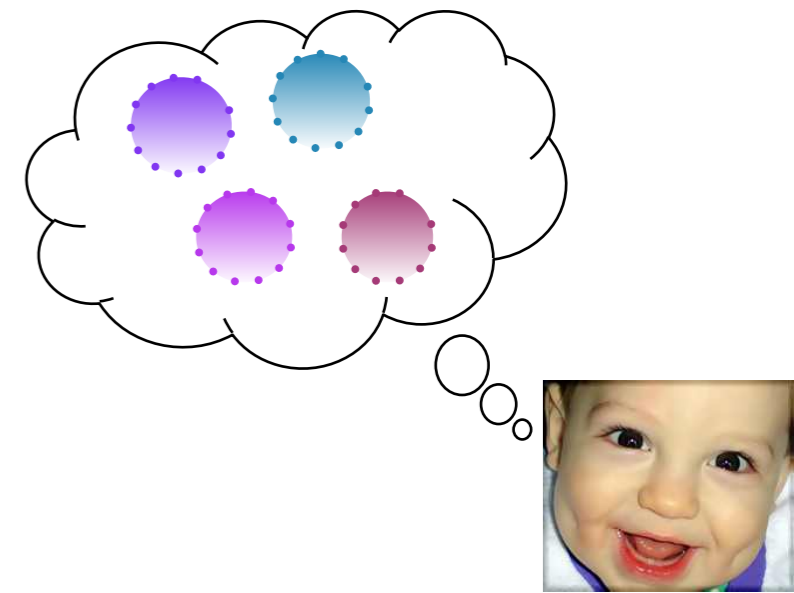
Kannada

Subject Object Verb Object

English

Subject Verb Object

# Interacting parameters

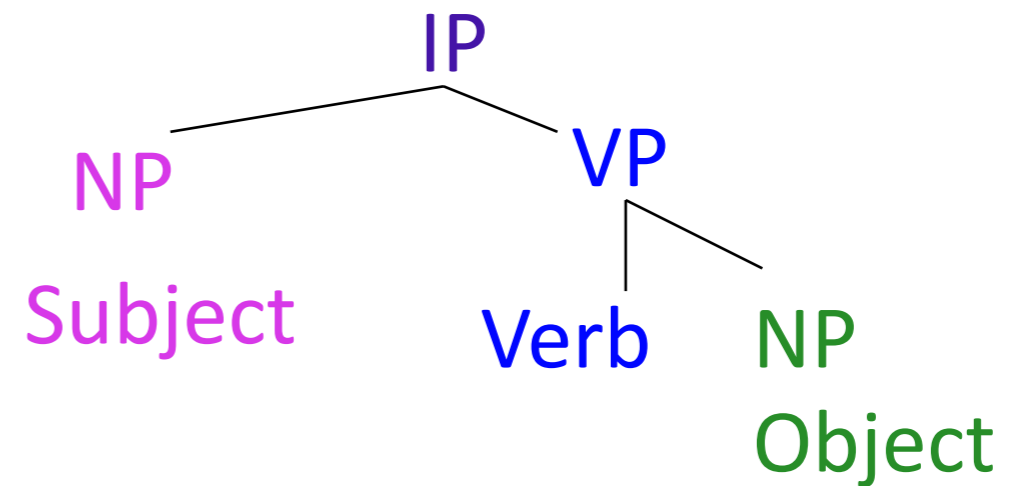


Example Parameter 1: Head-directionality 

Edo/English: Head-first 

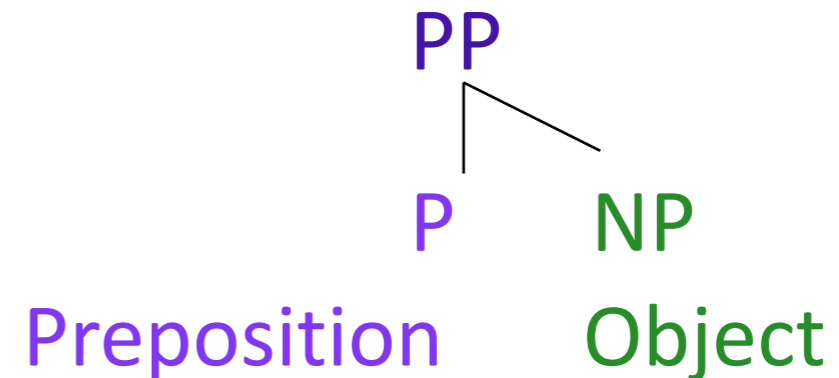
Basic word order:

Subject Verb Object [SVO]



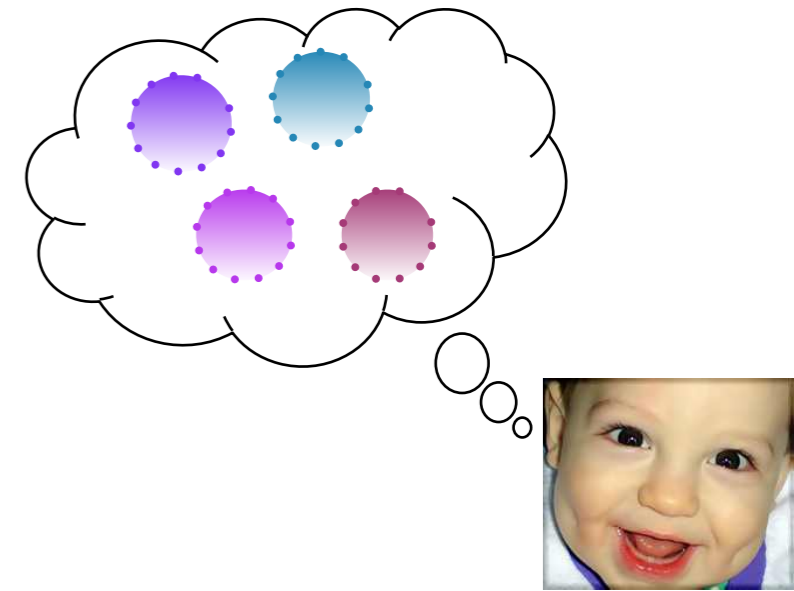
Prepositions:

Preposition Noun Phrase





# Interacting parameters



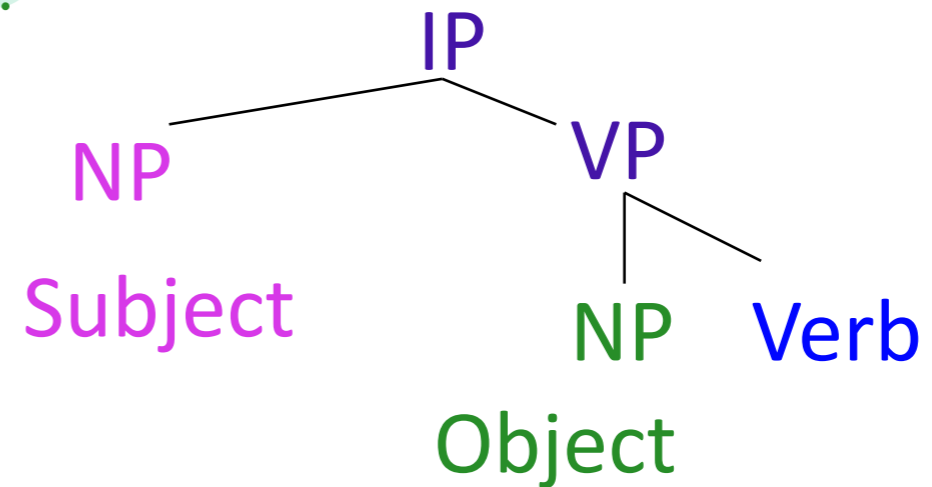
Example Parameter 1: Head-directionality 

Edo/English: Head-first 

Japanese/Navajo: Head-final 

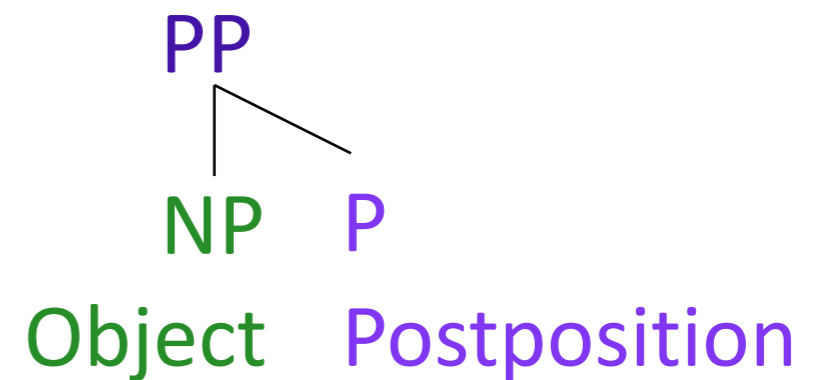
Basic word order:

Subject Object Verb [SOV]



Postpositions:

Noun Phrase Postposition




# Interacting parameters

Example Parameter 1: Head-directionality 

Edo/English: Head-first 

Japanese/Navajo: Head-final 

Example Parameter 2: Verb Second (V2) 

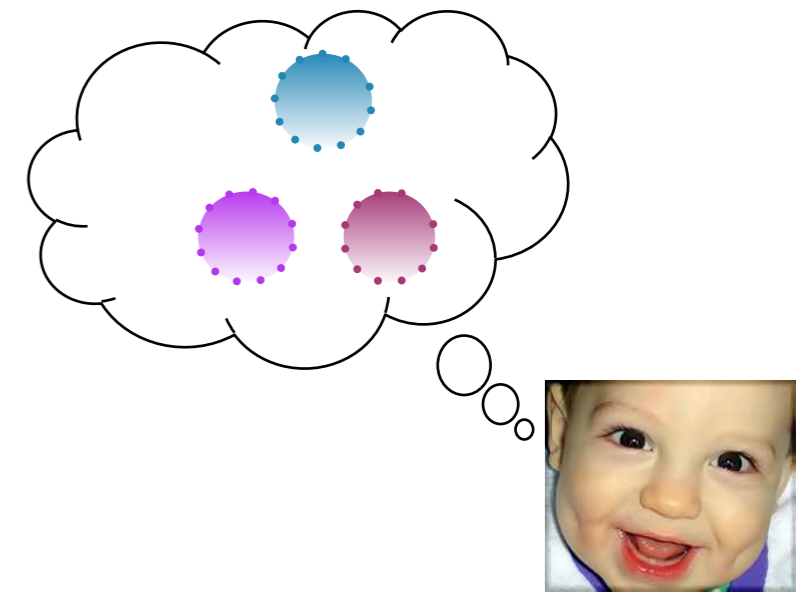
German: +V2 

**Verb** moves to second phrasal position, some other phrase moves to the first position

Sarah das Buch liest


*Sarah the book reads*

*Underlying form of the sentence*




# Interacting parameters

Example Parameter 1: Head-directionality 

Edo/English: Head-first 

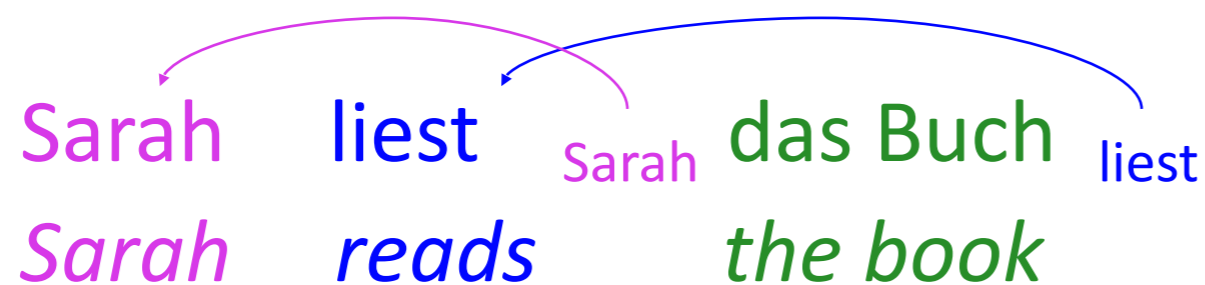
Japanese/Navajo: Head-final 

Example Parameter 2: Verb Second (V2) 

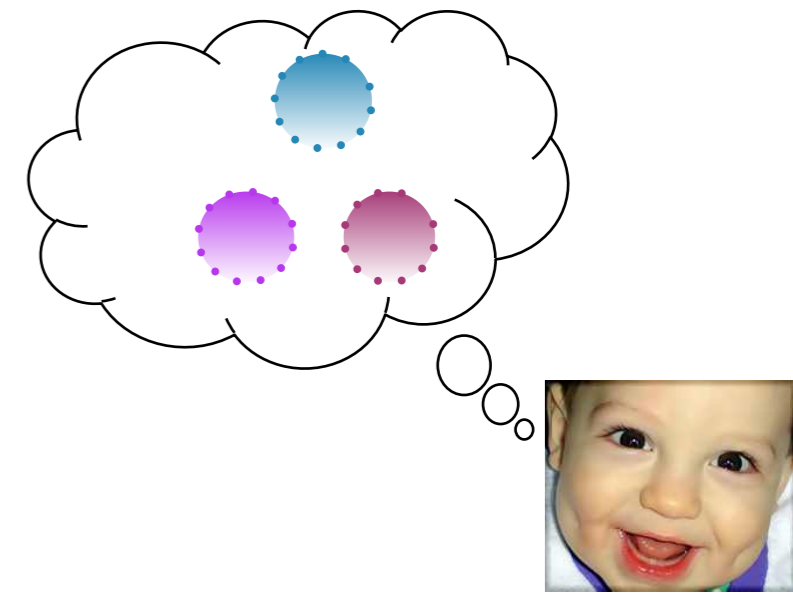
German: +V2 

**Verb** moves to second phrasal position, some other phrase moves to the first position

*Sarah liest Sarah das Buch liest*  
*Sarah reads the book*



*Observable form of the sentence*




# Interacting parameters

Example Parameter 1: Head-directionality 

Edo/English: Head-first 

Japanese/Navajo: Head-final 

Example Parameter 2: Verb Second (V2) 

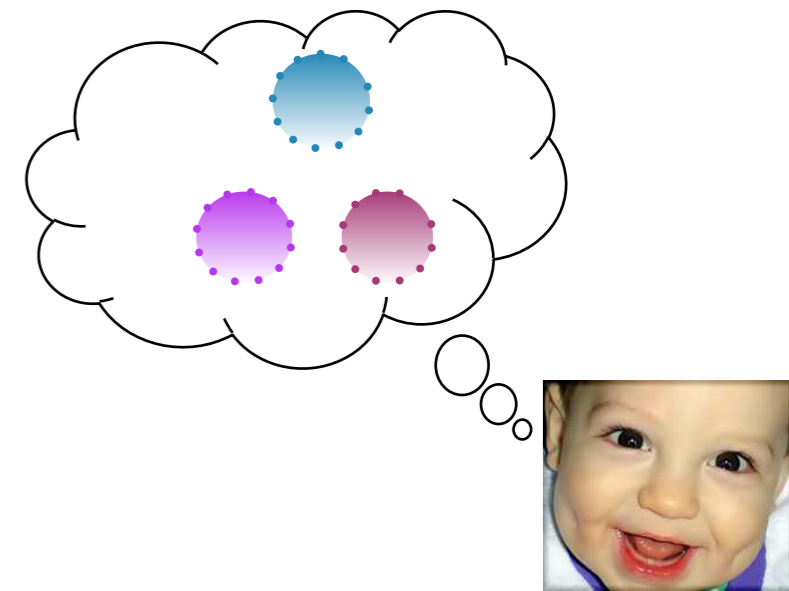
German: +V2 

**Verb** moves to second phrasal position, some other phrase moves to the first position

Sarah das Buch liest


*Sarah the book reads*

*Underlying form of the sentence*




# Interacting parameters

Example Parameter 1: Head-directionality 

Edo/English: Head-first 

Japanese/Navajo: Head-final 

Example Parameter 2: Verb Second (V2) 

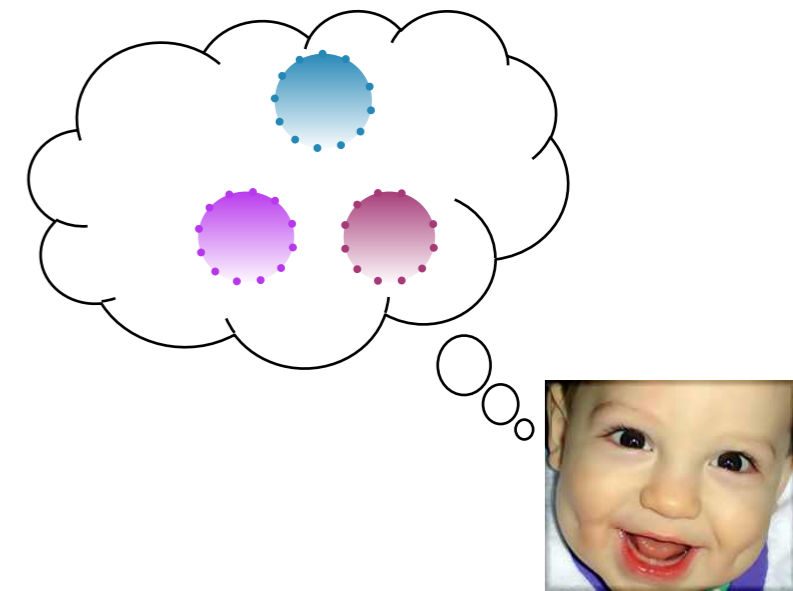
German: +V2 

**Verb** moves to second phrasal position, some other phrase moves to the first position

Das Buch liest Sarah das Buch liest  
*The book reads Sarah*




*Observable form of the sentence*




# Interacting parameters


Example Parameter 1: Head-directionality 

Edo/English: Head-first 

Japanese/Navajo: Head-final 

Example Parameter 2: Verb Second (V2) 

German: +V2 

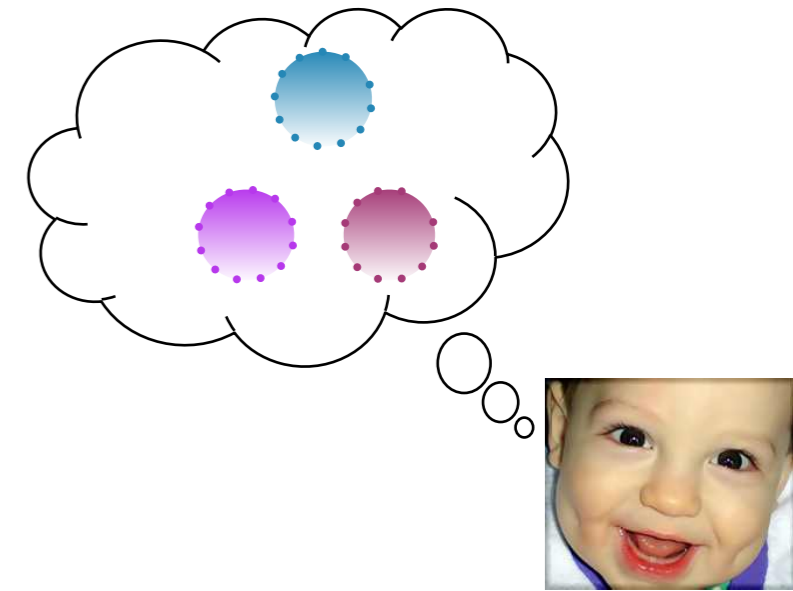
English: -V2 

Verb doesn't move.

Sarah reads the book

*Underlying form of the sentence*

*Observable form of the sentence*

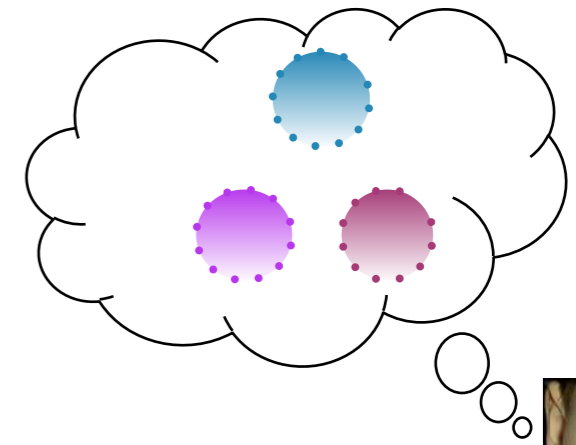


# Interacting parameters

Head-directionality



Verb Second (V2)



## Grammars available

**G1** Head-first +V2

**G2** Head-final +V2

**G3** Head-first -V2

**G4** Head-final -V2

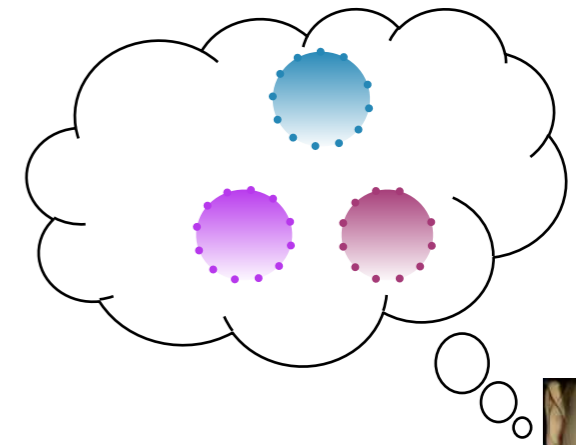


# Interacting parameters

Head-directionality



Verb Second (V2)



Data point

Subject

Verb

Object

**G1** Head-first +V2

**G2** Head-final +V2

**G3** Head-first -V2

**G4** Head-final -V2



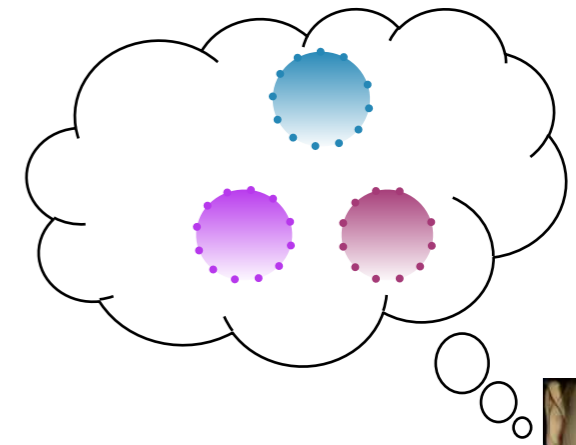


# Interacting parameters

Head-directionality







Verb Second (V2)







Subject    Verb    Object

## Which grammars can analyze this data point?

**G1**    Head-first      
           +V2            

**G2**    Head-final      
           +V2            

**G3**    Head-first      
           -V2            

**G4**    Head-final      
           -V2            

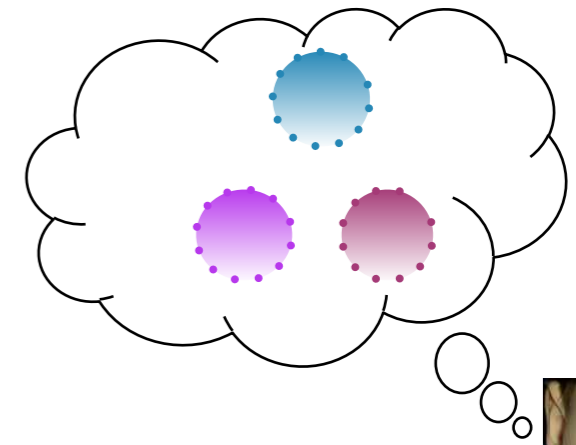


# Interacting parameters

Head-directionality



Verb Second (V2)



Subject

Verb

*Verb*

Object

**G1** Head-first +V2

✓ +head-first predicts SVO

✓ +V2 predicts Verb moved to second position

**G3** Head-first -V2

**G2** Head-final +V2

**G4** Head-final -V2

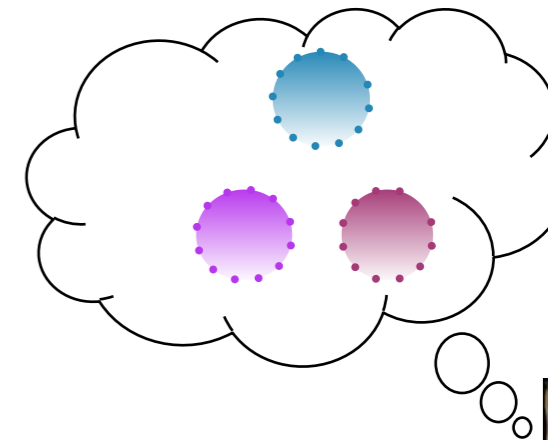


# Interacting parameters

Head-directionality



Verb Second (V2)





Subject

Verb

Subject



Object



Verb



**G2** Head-final   
+V2 

✓ head-final predicts SOV

✓ +V2 predicts Verb moved to second position

✓ **G1** Head-first   
+V2 

**G3** Head-first   
-V2 

**G4** Head-final   
-V2 

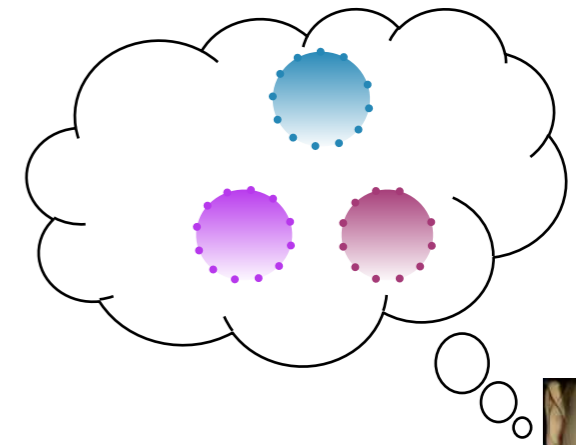


# Interacting parameters

Head-directionality



Verb Second (V2)



"I love kitties."

Subject

Verb

Object

**G3**

Head-first



-V2



✓ head-first predicts SVO

✓ -V2 predicts Verb doesn't move

**G1**

Head-first



+V2



**G2**

Head-final



+V2

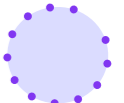


**G4**

Head-final



-V2



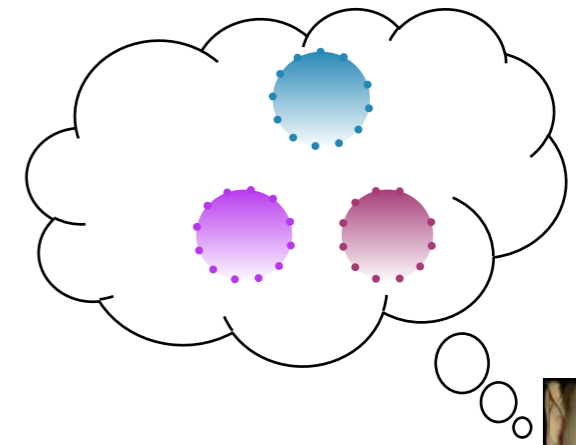


# Interacting parameters

Head-directionality



Verb Second (V2)



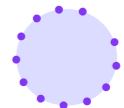
"I love kitties."

Subject

Verb

Object

**G4** Head-final  
-V2



✗ head-final predicts SOV

✓ -V2 predicts Verb doesn't move

**G1**

Head-first  
+V2



**G2**

Head-final  
+V2



**G3**

Head-first  
-V2



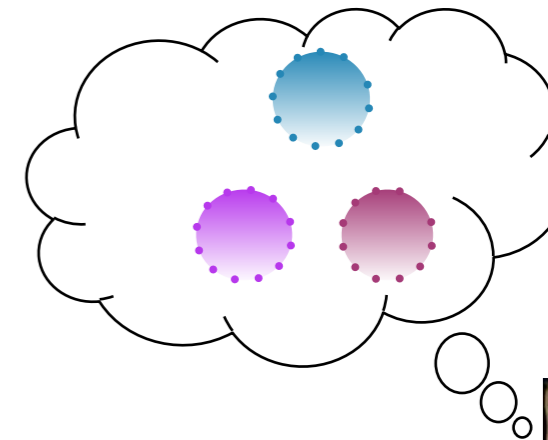


# Interacting parameters

Head-directionality



Verb Second (V2)



"I love kitties."

Subject    Verb    Object

**G1**

Head-first  
+V2



**G2**

Head-final  
+V2



**G3**

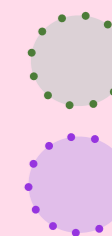
Head-first  
-V2



What do the grammars that can analyze this data point have in common?

~~**G4**~~

Head-final  
-V2

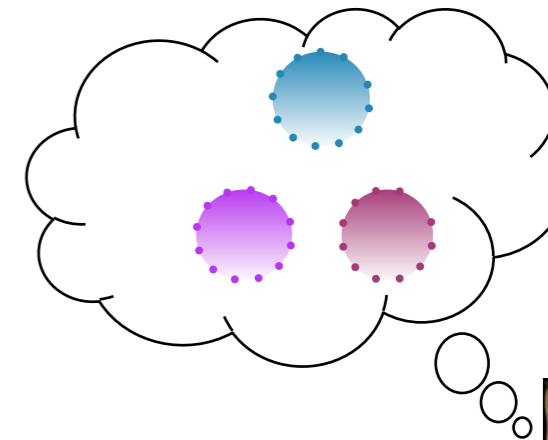




# Interacting parameters

Head-directionality

Verb Second (V2)



"I love kitties."

Subject    Verb    Object

**G1**

Head-first  
+V2



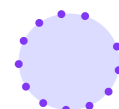
**G2**

Head-final  
+V2



**G3**

Head-first  
-V2

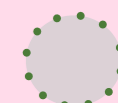


We don't know whether the true grammar is head-first or head-final since there's a grammar of each kind.



**G4**

Head-final  
-V2

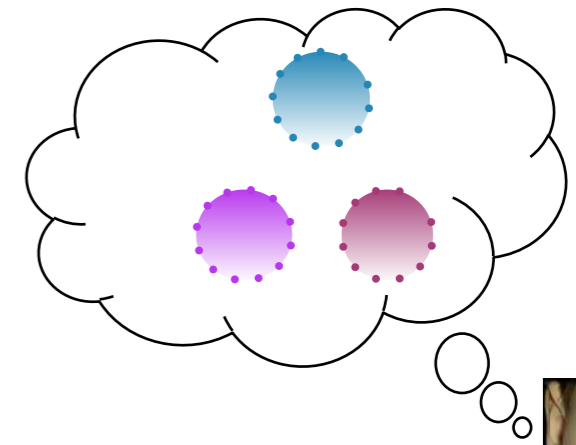




# Interacting parameters

Head-directionality

Verb Second (V2)



"I love kitties."

Subject    Verb    Object

G1

Head-first  
+V2



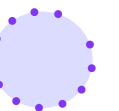
G2

Head-final  
+V2

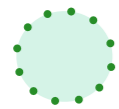


G3

Head-first  
-V2



We don't know whether the true grammar is head-first or head-final since there's a grammar of each kind.

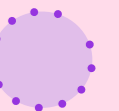
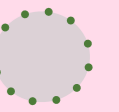


*(though there are more head-first)*



G4

Head-final  
-V2





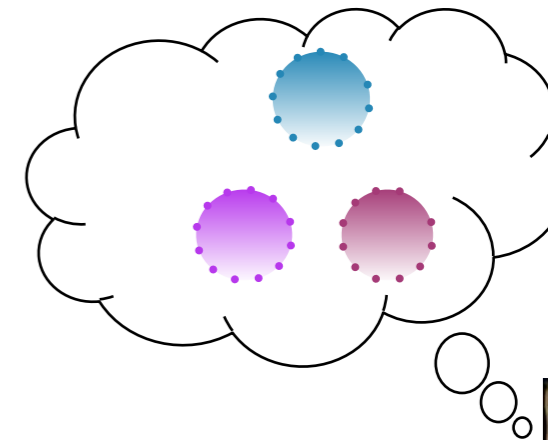


# Interacting parameters

Head-directionality



Verb Second (V2)



"I love kitties."

Subject    Verb    Object

✓  
**G1**    Head-first    ●  
           +V2

✓  
**G2**    Head-final    ●  
           +V2

✓  
**G3**    Head-first    ●  
           -V2

We don't know whether the true grammar is +V2 or -V2 since there's a grammar of each kind.



✗  
**G4**    Head-final    ●  
           -V2

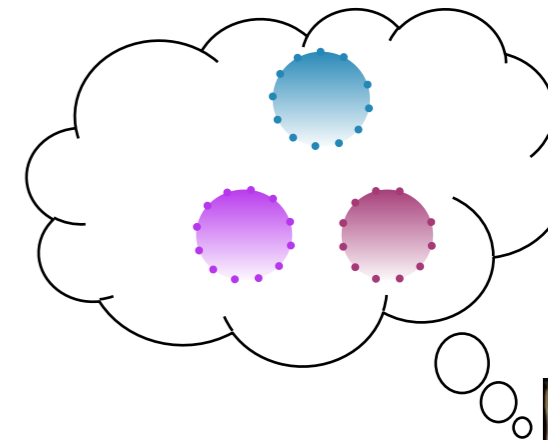


# Interacting parameters

Head-directionality



Verb Second (V2)



Subject    Verb    Object

✓  
**G1**    Head-first    ●  
           +V2

✓  
**G2**    Head-final    ●  
           +V2

✓  
**G3**    Head-first    ●  
           -V2



We don't know whether the true grammar is +V2 or -V2 since there's a grammar of each kind.

*(though there are more +V2)*

✗  
**G4**    Head-final    ●  
           -V2

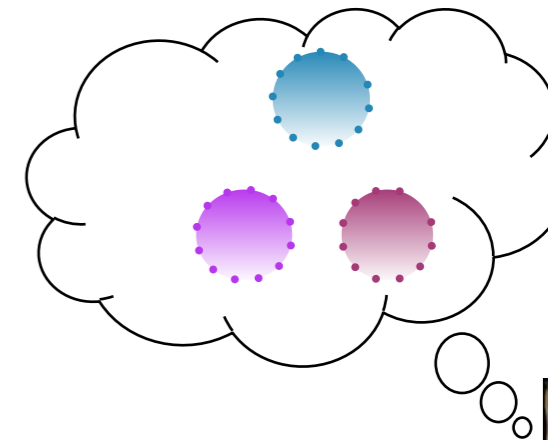


# Interacting parameters

Head-directionality



Verb Second (V2)



"I love kitties."

Subject    Verb    Object

G1

Head-first  
+V2



G2

Head-final  
+V2



G3

Head-first  
-V2



This data point isn't unambiguous for any of the parameters we're interested in because **the parameters interact**...even though we feel like it might be somewhat informative for **head-first** and **+V2** because these occur in more grammars that are compatible.

G4

Head-final  
-V2

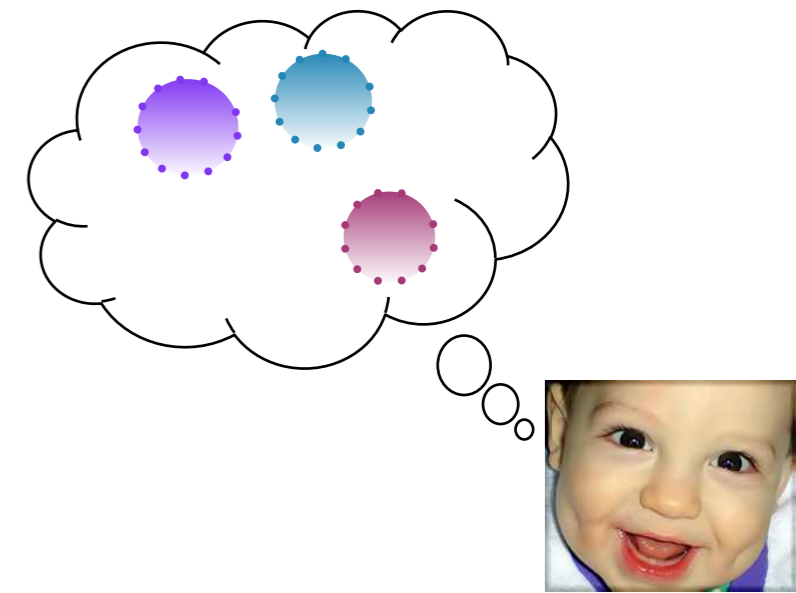


# Interacting parameters

Head-directionality 

Edo/English: Head-first 

Japanese/Navajo: Head-final 



Example Parameter 3: Subject drop 

Spanish: +subj-drop 

Allows **Subject** to be overt or dropped

✓ Ellos beben  
*they drink-3rd-pl*

✓ Beben  
*drink-3rd-pl*

“They drink”

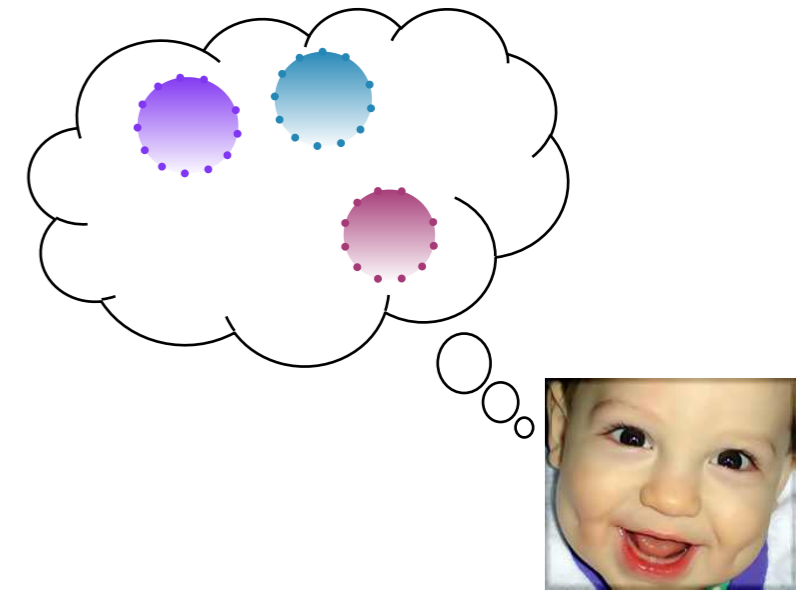


# Interacting parameters

Head-directionality 

Edo/English: Head-first 

Japanese/Navajo: Head-final 



Example Parameter 3: Subject drop 

Spanish: +subj-drop 

English: -subj-drop 

Subject must be overt

✓ They drink

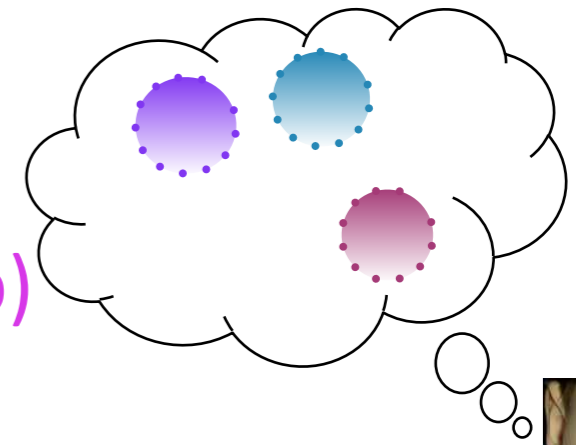
✗ Drink

“They drink”





# Interacting parameters

Head-directionality    Subject drop (subj-drop)





## Grammars available



**G1**

Head-first   
+subj-drop 



**G2**

Head-final   
+subj-drop 

**G3**

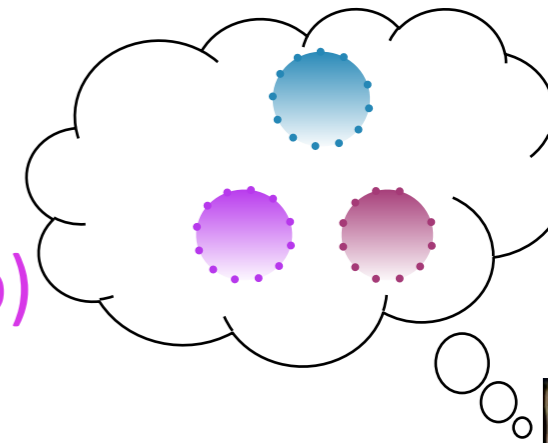
Head-first   
-subj-drop 

**G4**

Head-final   
-subj-drop 



# Interacting parameters



Head-directionality

Subject drop (subj-drop)





“...dass ich  
Kätzchen liebe.”  
...that I Kitties love



Subject



Object



Verb

## Which grammars can analyze this data point?

**G1** Head-first   
+subj-drop 

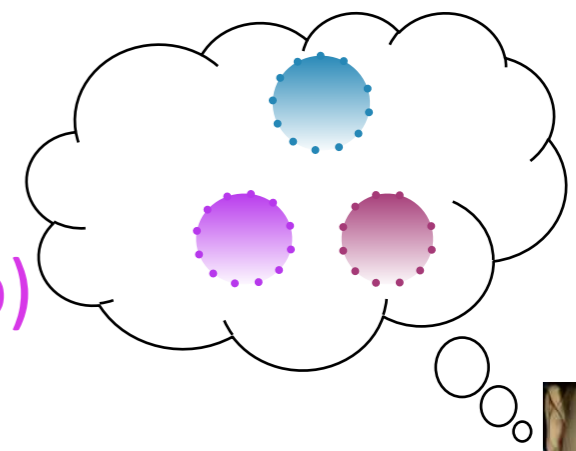
**G2** Head-final   
+subj-drop 

**G3** Head-first   
-subj-drop 

**G4** Head-final   
-subj-drop 



# Interacting parameters



Head-directionality



Subject drop (subj-drop)







“...dass **ich**  
**Kätzchen liebe.**”  
*...that I Kitties love*



**Subject**   **Object**   **Verb**

- ✗ head-first predicts SVO
- ✓ +subj-drop allows subject to be overt

**G1** Head-first   
+subj-drop 

**G2** Head-final   
+subj-drop 

**G3** Head-first   
-subj-drop 

**G4** Head-final   
-subj-drop 

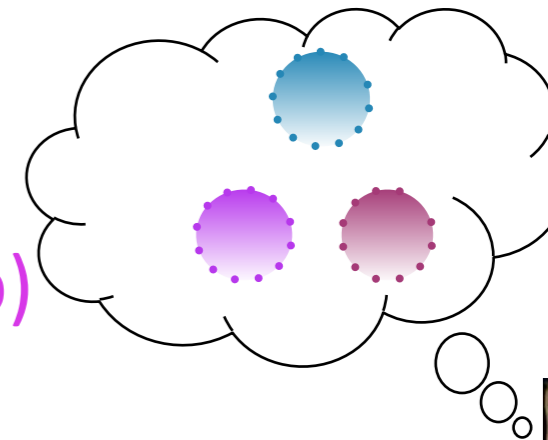




# Interacting parameters

Head-directionality



Subject drop (subj-drop)





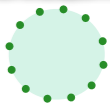
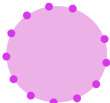
“...dass **ich**  
**Kätzchen liebe.**”  
*...that I Kitties love*



**Subject**   **Object**   **Verb**

- ✓ head-final predicts SOV
- ✓ +subj-drop allows subject to be overt

**G2** Head-final   
+subj-drop 

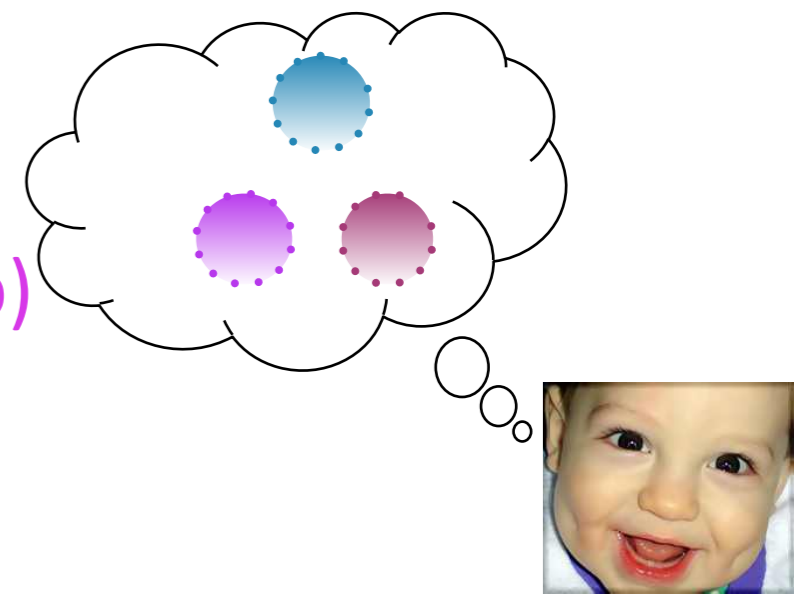
**G3** Head-first   
-subj-drop 

**G4** Head-final   
-subj-drop 

~~**G1**~~ Head-first   
+subj-drop 



# Interacting parameters





Head-directionality



Subject drop (subj-drop)



“...dass ich  
Kätzchen liebe.”  
...that I Kitties love



Subject    Object    Verb

- ✗ head-first predicts SVO
- ✓ -subj-drop requires subject to be overt

**G3** Head-first   
-subj-drop 

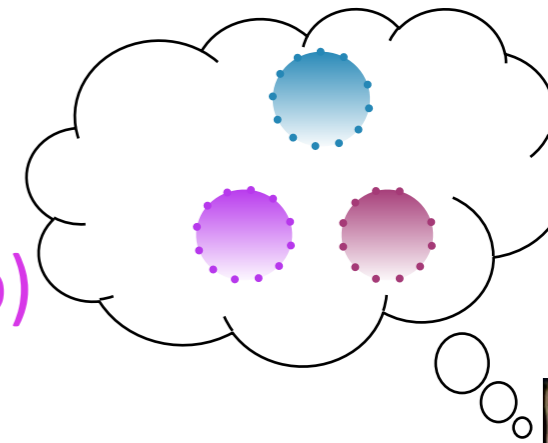
✓ **G2** Head-final   
+subj-drop 

✗ **G1** Head-first   
+subj-drop 

**G4** Head-final   
-subj-drop 



# Interacting parameters



Head-directionality

Subject drop (subj-drop)



“...dass **ich**  
**Kätzchen liebe.**”  
*...that I Kitties love*

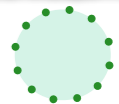
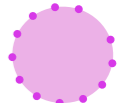
Subject



Object



Verb



✓ head-final predicts SOV

✓ -subj-drop requires subject to be overt

**G4** Head-final   
-subj-drop 

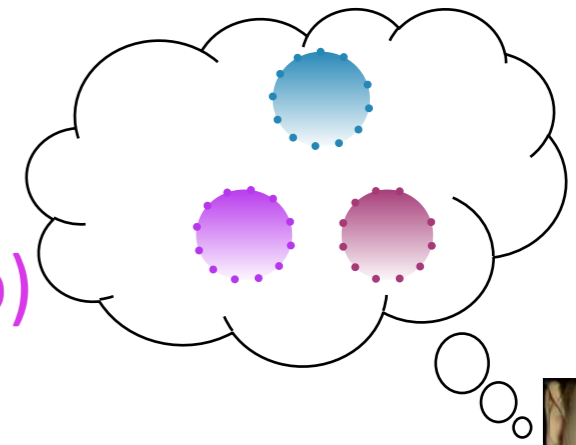
✓ **G2** Head-final   
+subj-drop 

~~**G1**~~ Head-first   
+subj-drop 

~~**G3**~~ Head-first   
-subj-drop 



# Interacting parameters



Head-directionality

Subject drop (subj-drop)



“...dass **ich**  
**Kätzchen liebe.**”  
...that I Kitties love

Subject

Object

Verb

G2

Head-final  
+subj-drop



G4

Head-final  
-subj-drop



There's more than one grammar compatible with this data point...even though we feel like it **should definitely** be informative for **head-final** (since that's the only value in the compatible grammars).



G1

Head-first  
+subj-drop



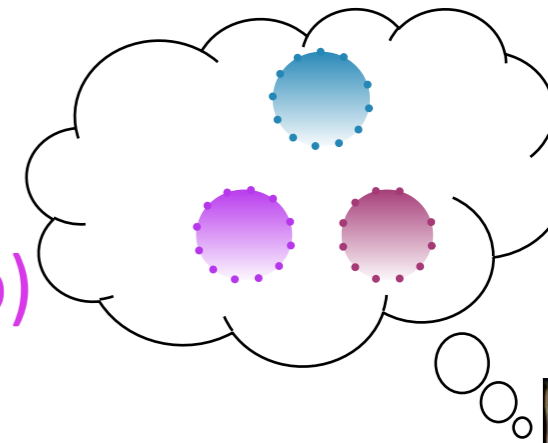
G3

Head-first  
-subj-drop





# Interacting parameters



Head-directionality

Subject drop (subj-drop)



“...dass **ich**  
**Kätzchen liebe.**”  
*...that I Kitties love*

Subject

Object

Verb

**G2**

Head-final  
+subj-drop



**G4**

Head-final  
-subj-drop



But technically, this is still an ambiguous data point because more than one grammar will work....

**G1**

Head-first  
+subj-drop



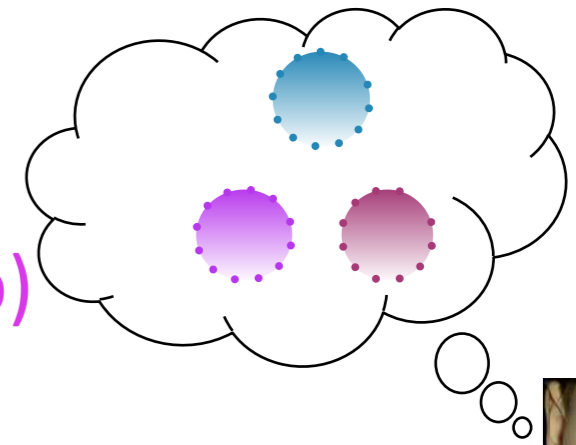
**G3**

Head-first  
-subj-drop





# Interacting parameters



Head-directionality

Subject drop (subj-drop)



“...dass **ich**  
**Kätzchen liebe.**”  
*...that I Kitties love*

Subject

Object

Verb



**G2**

Head-final  
+subj-drop



**G4**

Head-final  
-subj-drop



## So what can we do?



**G1**

Head-first  
+subj-drop



**G3**

Head-first  
-subj-drop



# Today's Plan:

## Computational models of syntactic acquisition

### I. Some non-parametric examples

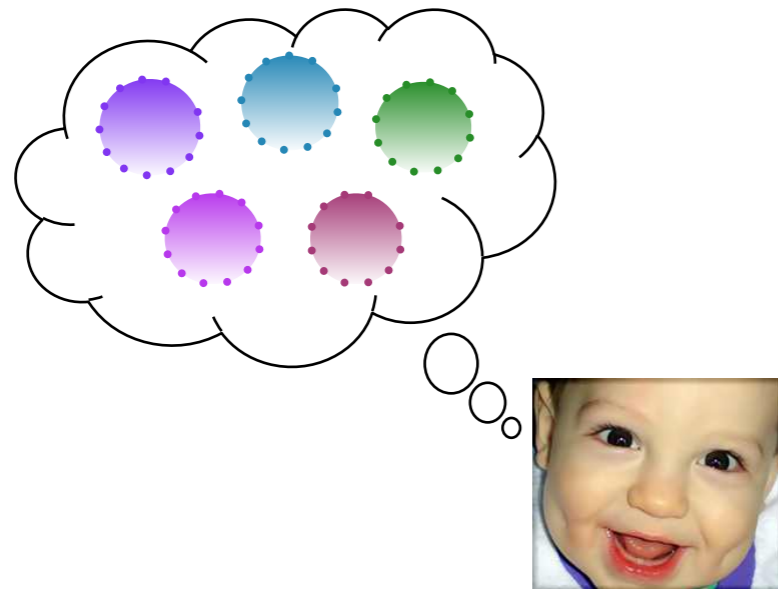
Who does  ...  is pretty?

**syntax** 

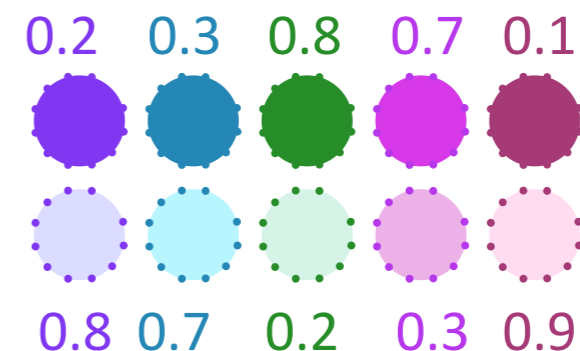
*another one*   

**syntax, semantics**

### II. About linguistic parameters



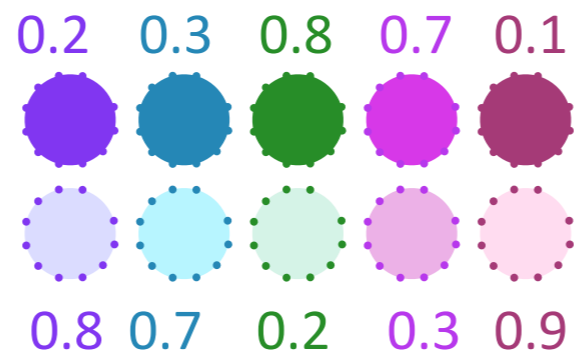
### III. Learning with parameters



# Today's Plan:

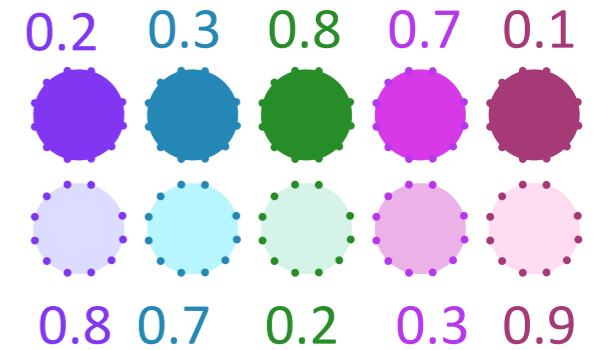
## Computational models of syntactic acquisition

### III. Learning with parameters









# Learning with parameters

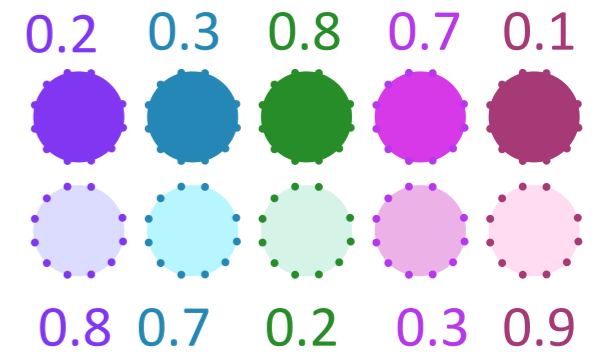


A language's grammar = combination of parameter values

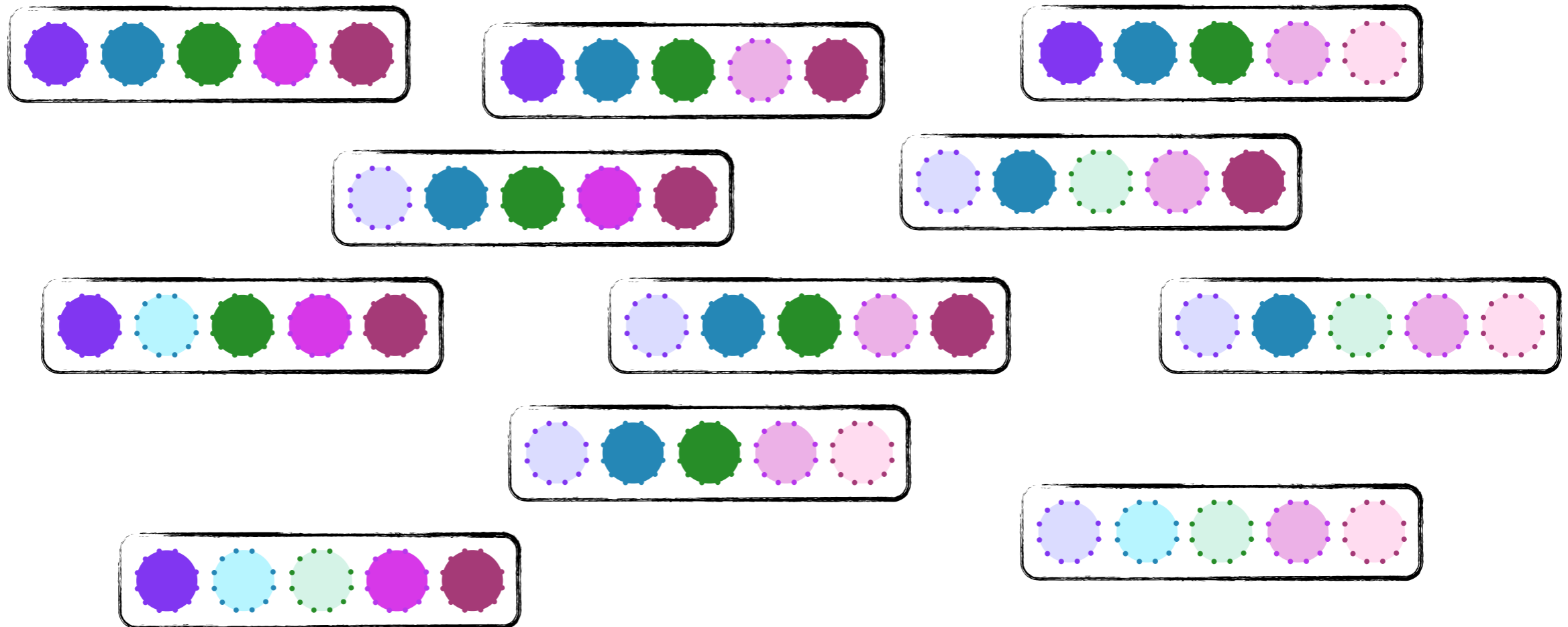
**G2** Head-final   
+subj-drop 

**G4** Head-final   
-subj-drop 

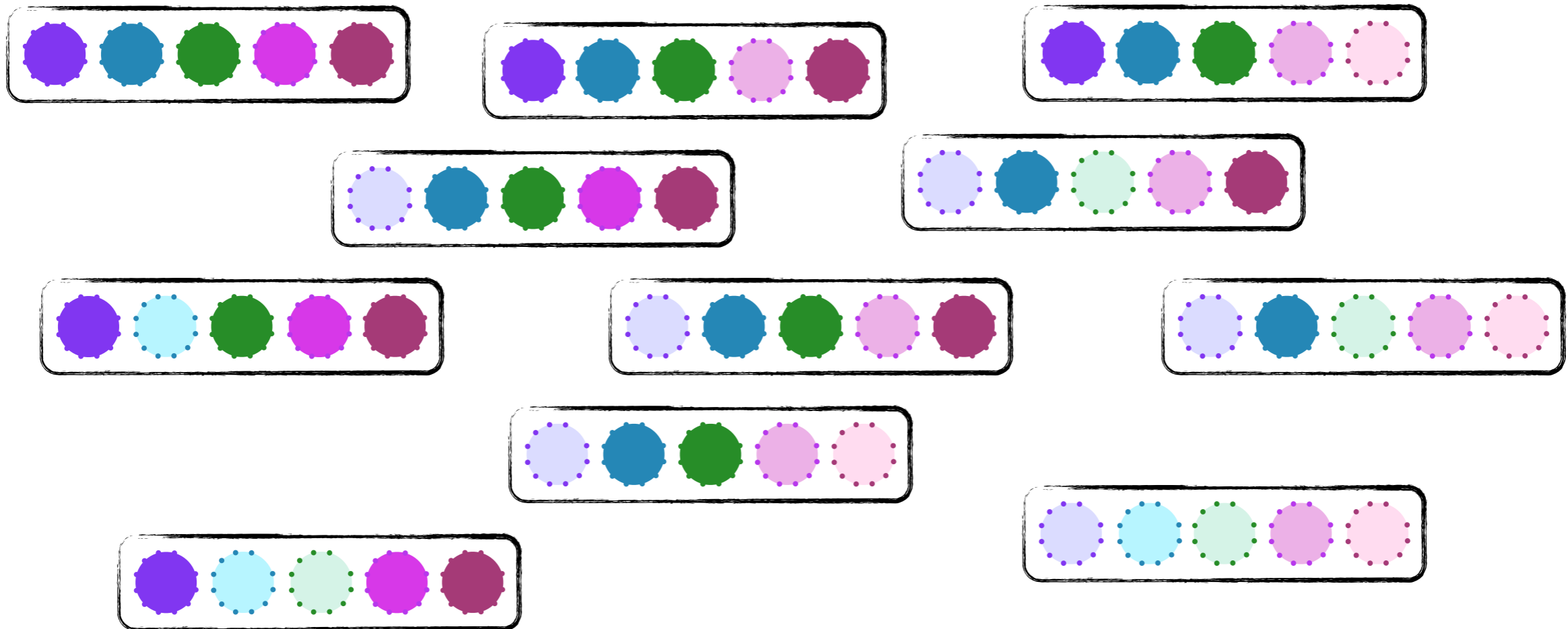
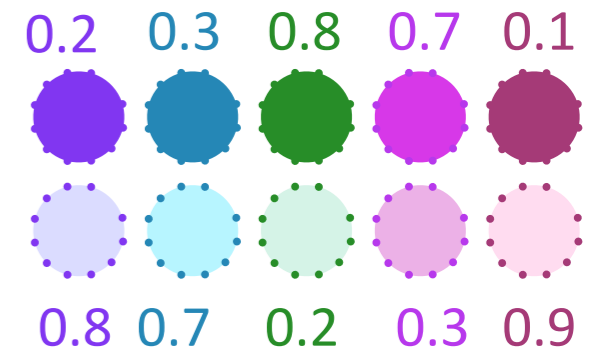
# Learning with parameters



A language's grammar = combination of parameter values



# Learning with parameters

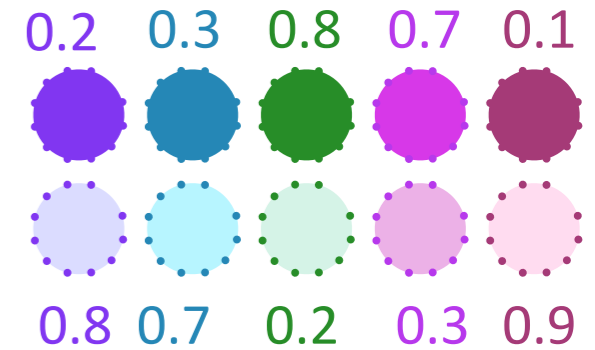


**Variational learning (Yang 2002, 2004, 2012):** use reinforcement learning to learn which value (for each parameter) that the native language uses for its grammar. This is a combination of using linguistic knowledge & statistical learning.



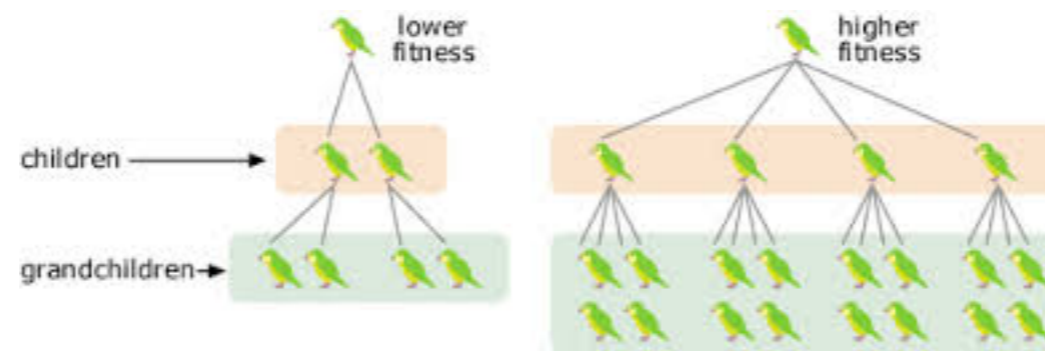
# Learning with parameters

## Variational learning



Idea taken from evolutionary biology:

In a population, individuals compete against each other. The fittest individuals survive while the others die out.

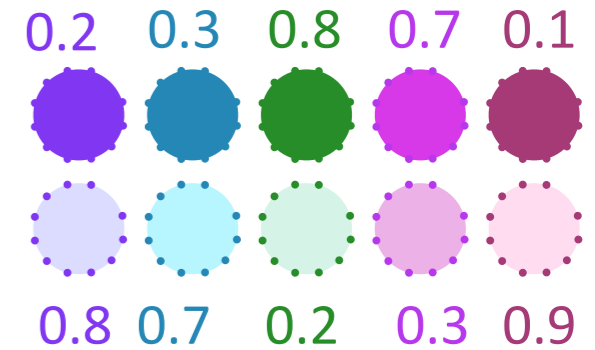


**How do we translate this to learning with parameters?**



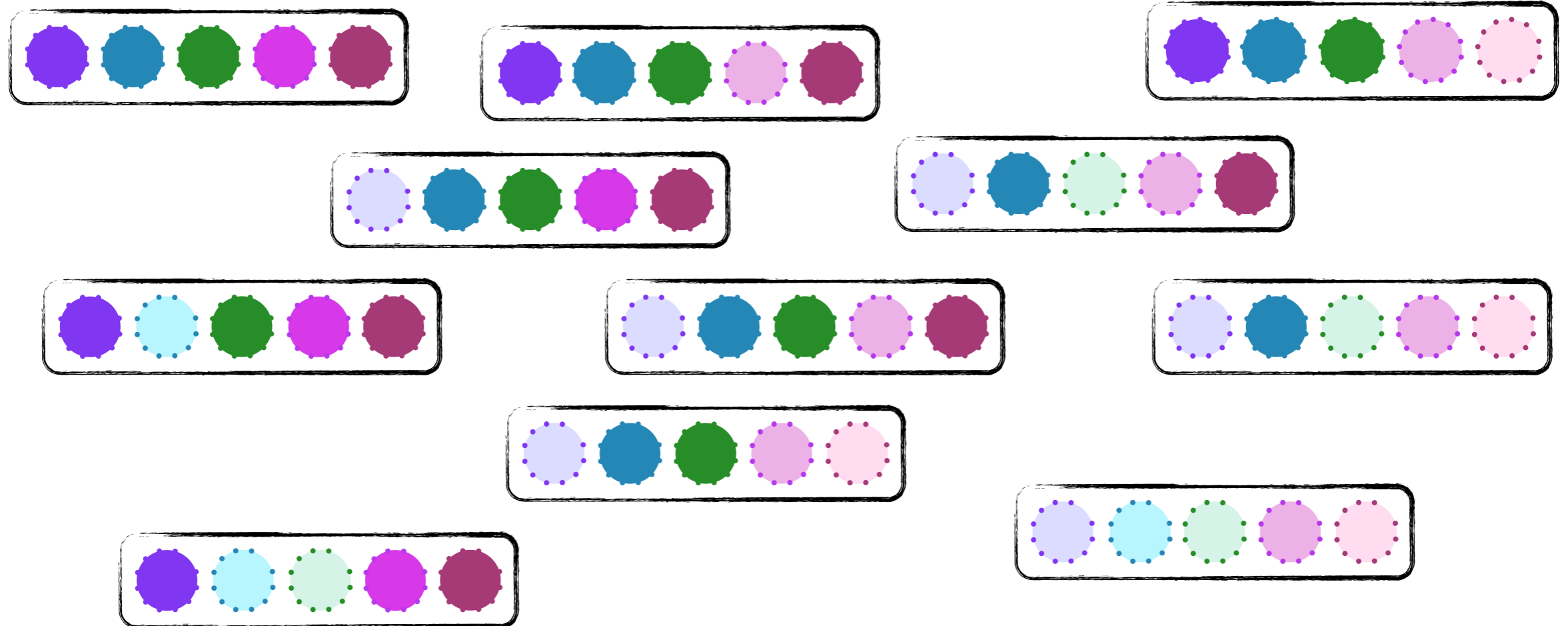
# Learning with parameters

## Variational learning



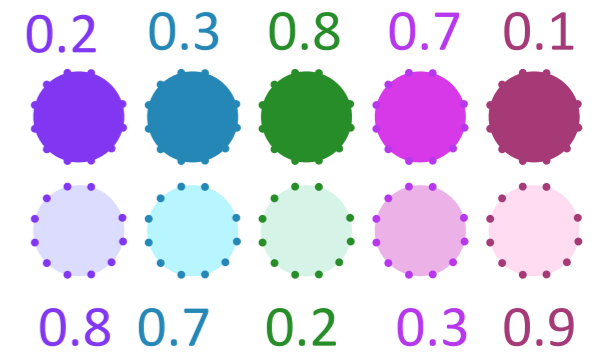
The fittest **individuals** survive while the others die out.

Individual = grammar (combination of parameter values that represents the structural properties of a language)



# Learning with parameters

## Variational learning



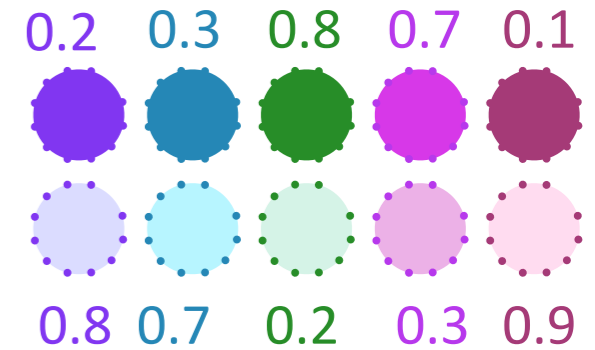
The **fittest** individuals survive while the others die out.

Fitness = how well a grammar can analyze the data the child encounters

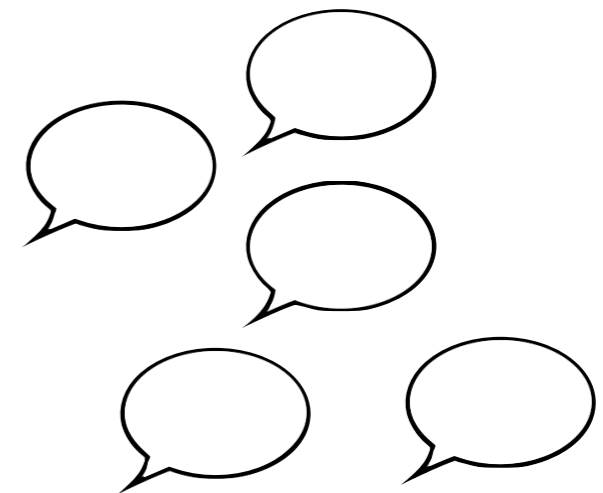
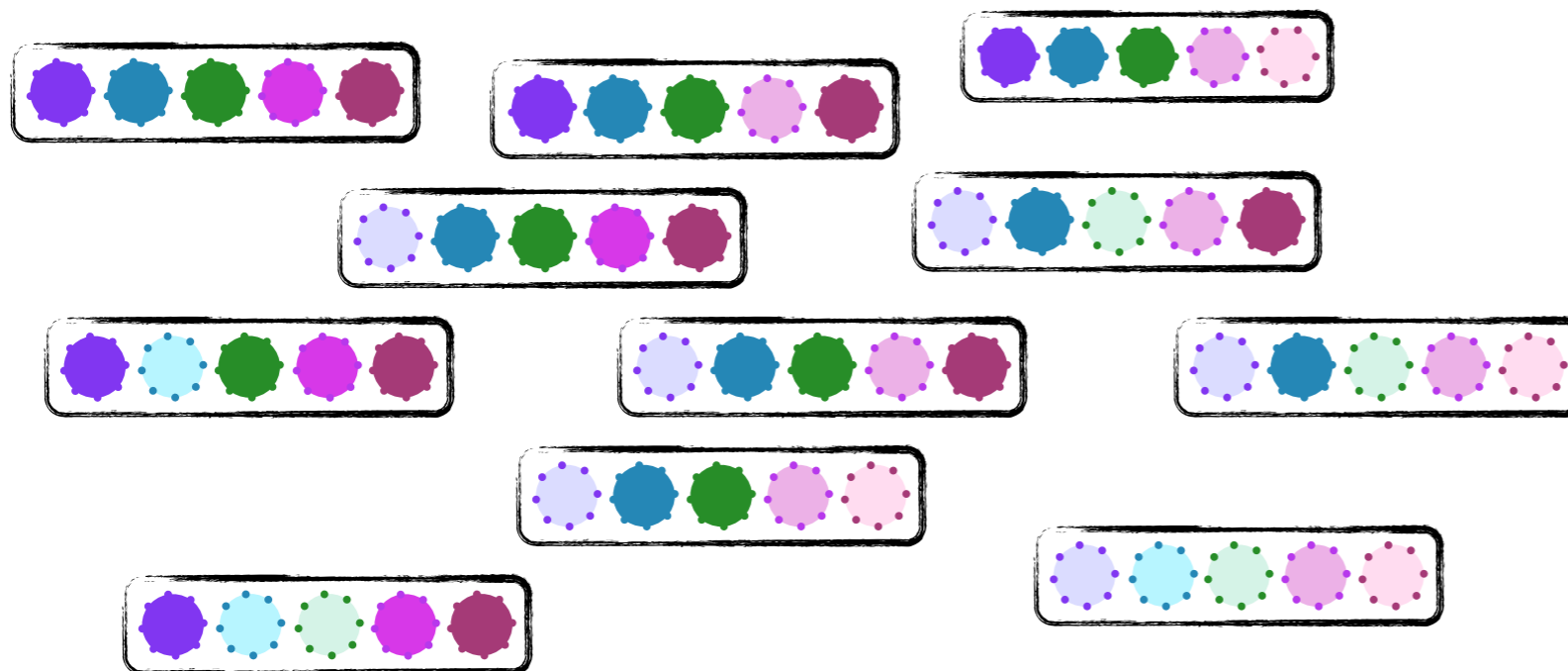


# Learning with parameters

## Variational learning

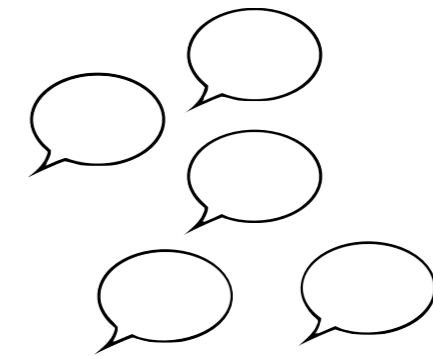
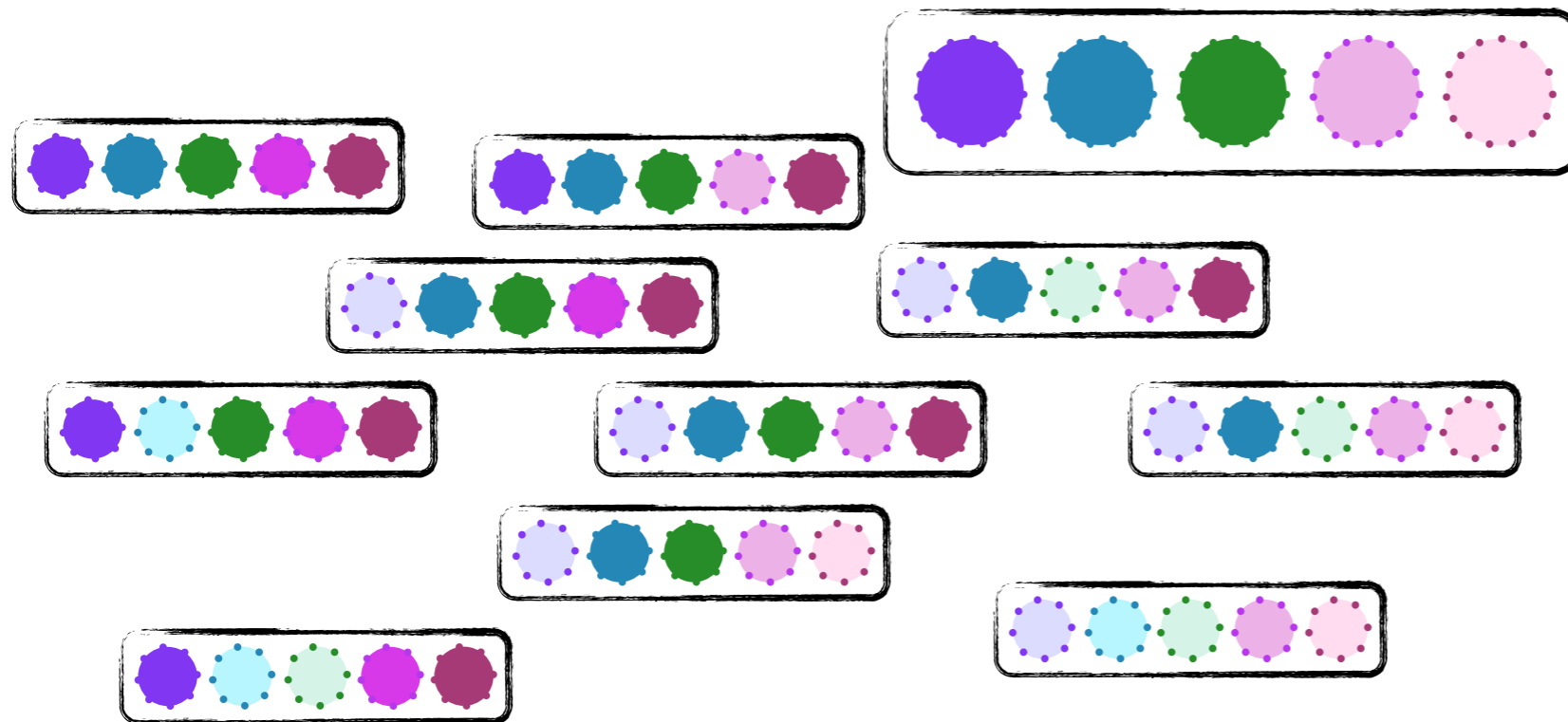
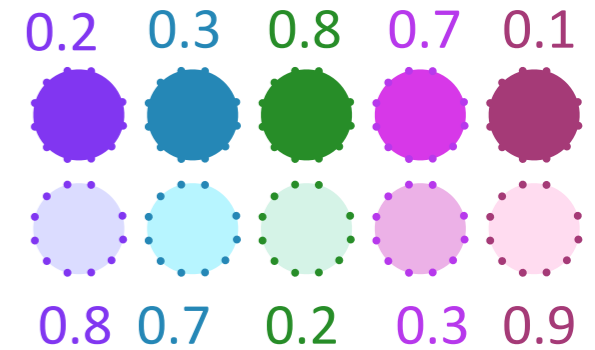


A child's mind consists of a population of grammars that are competing to analyze the data in the child's native language.



# Learning with parameters

## Variational learning

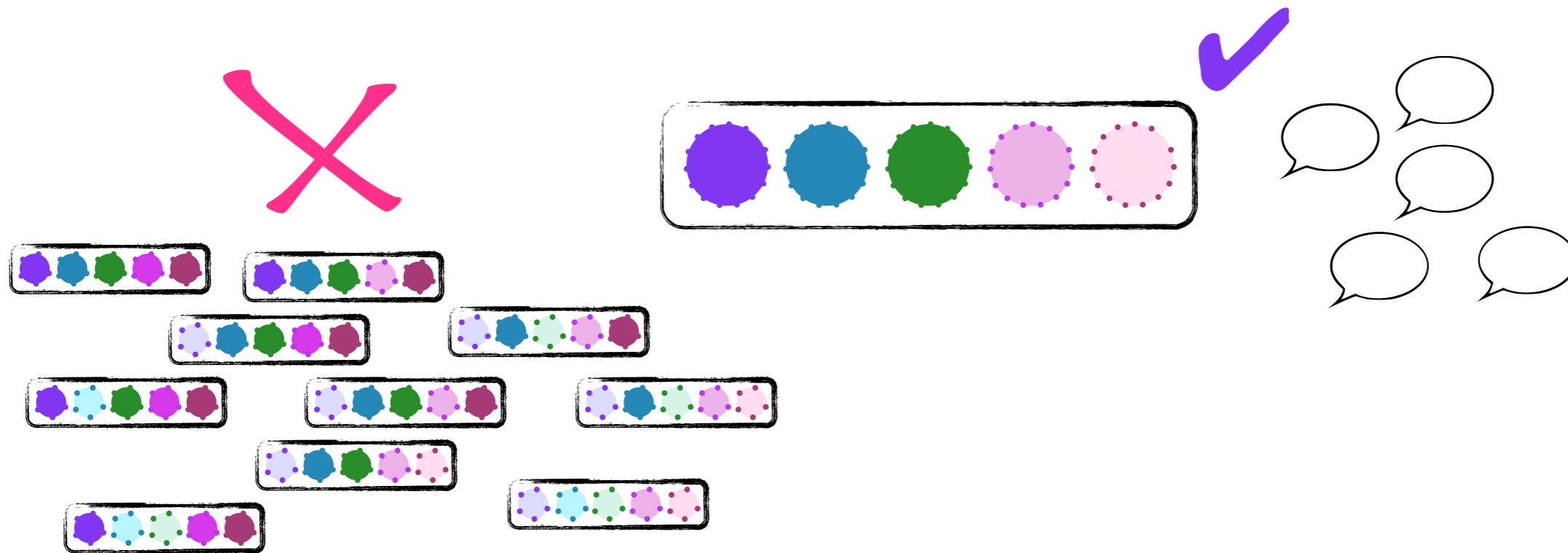
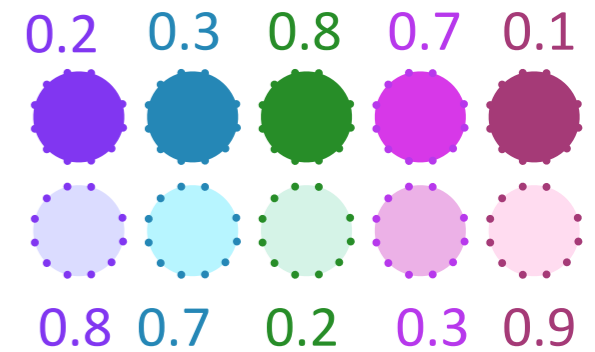


Intuition: The **most successful (fittest) grammar** will be the **native language grammar** because it can analyze all the data the child encounters. This grammar will “win”, once the child encounters enough native language data. This is because none of the other competing grammars can analyze all the data.



# Learning with parameters

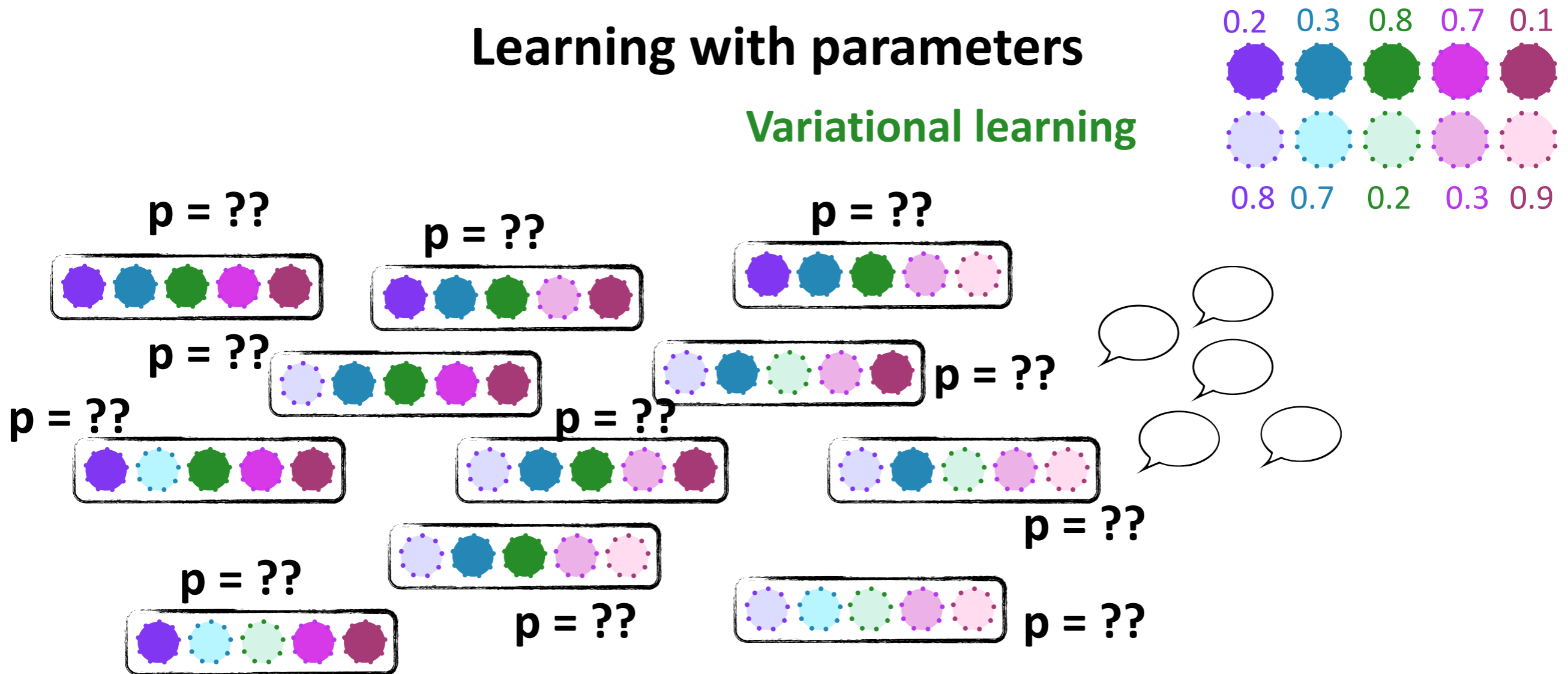
## Variational learning



If this is the native language grammar, this grammar can analyze all the intake while the others can't.

# Learning with parameters

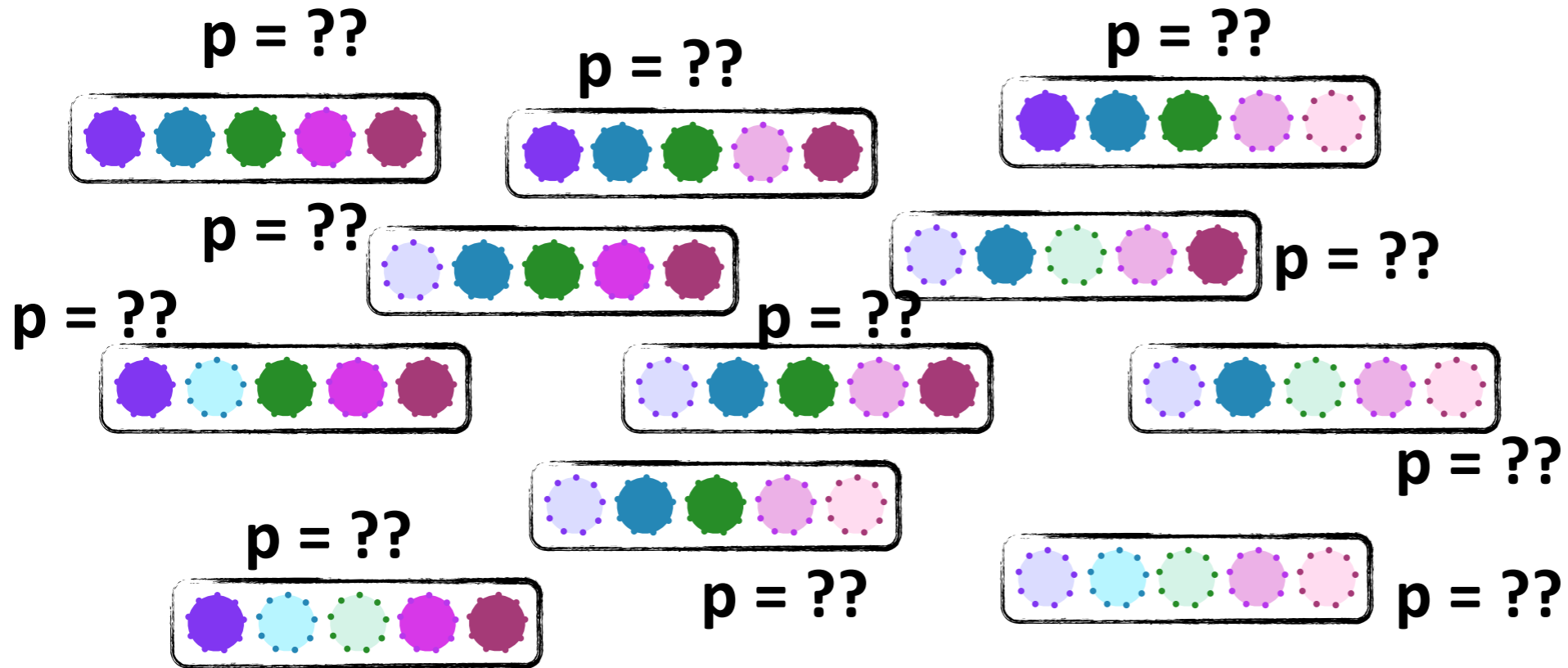
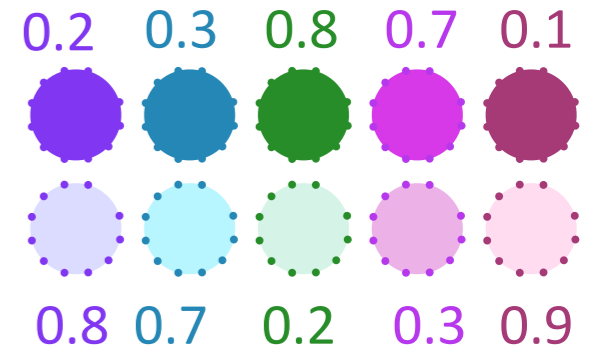
## Variational learning



At any point in time, a grammar in the population will have a **probability** associated with it. This represents the child's belief that this grammar is the correct grammar for the native language.

# Learning with parameters

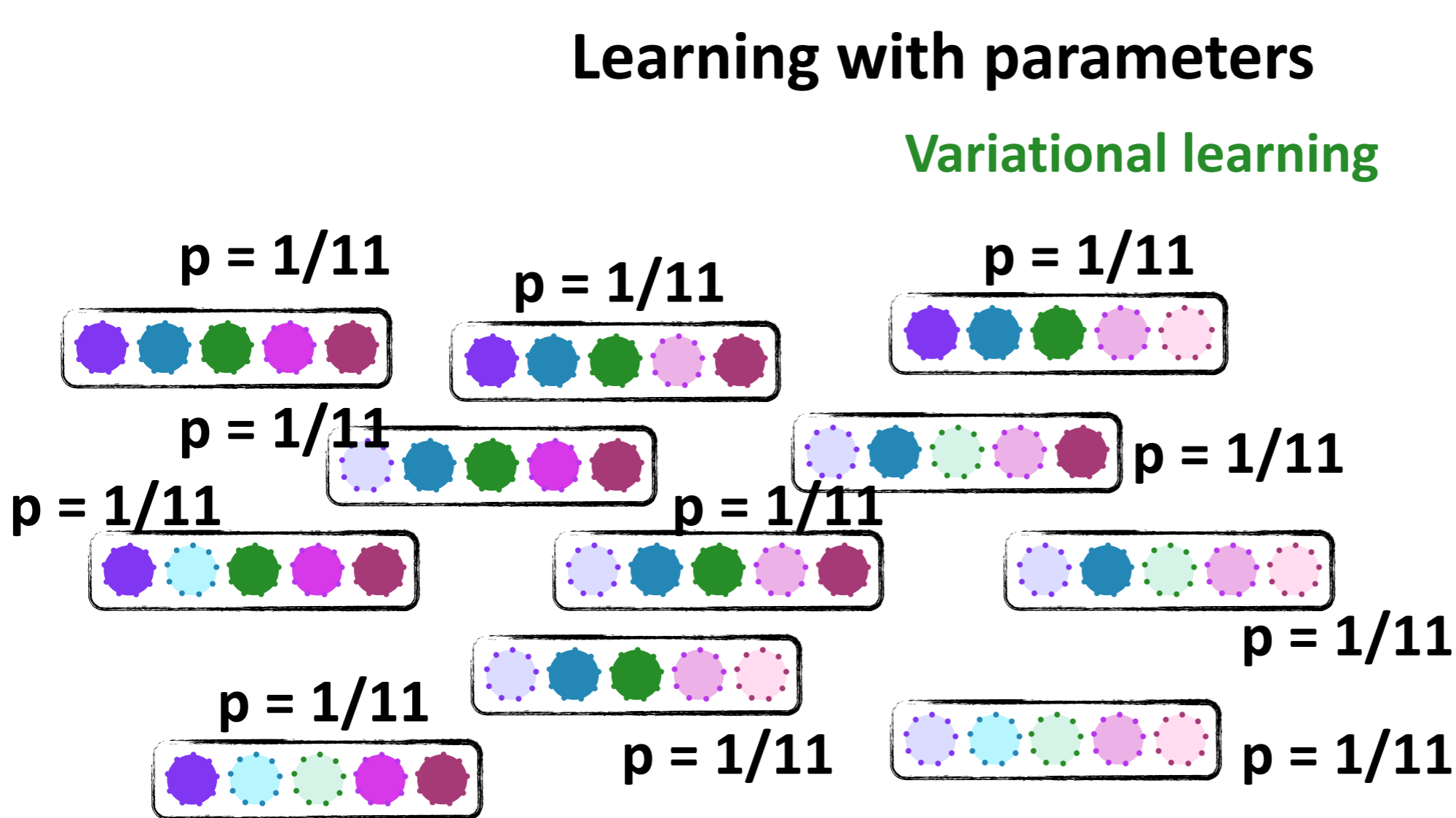
## Variational learning



Before the child has encountered any native language data, all grammars are **equally likely**. So, initially all grammars have the same probability, which is 1 divided the number of grammars available.

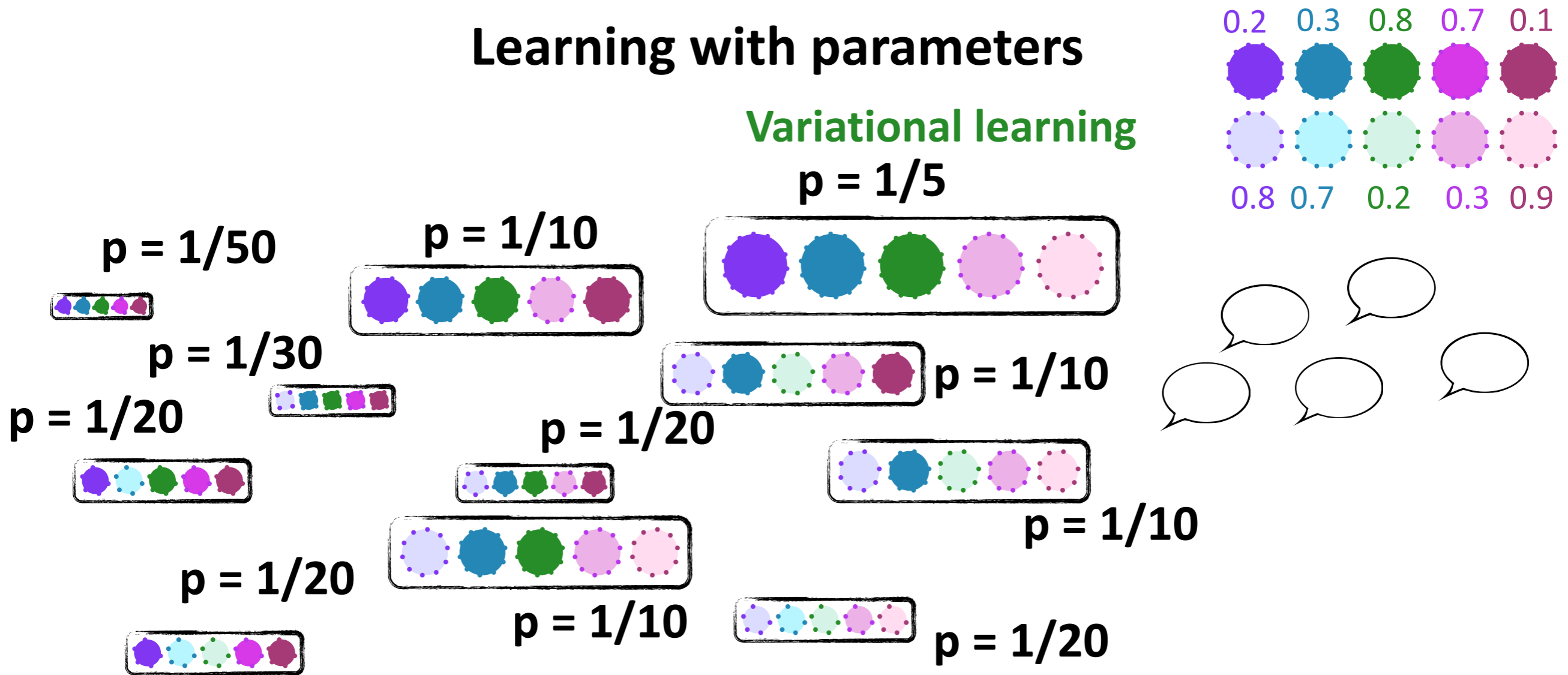
# Learning with parameters

## Variational learning



Since there are 11 grammars here, each begins with probability  $1/11$ .

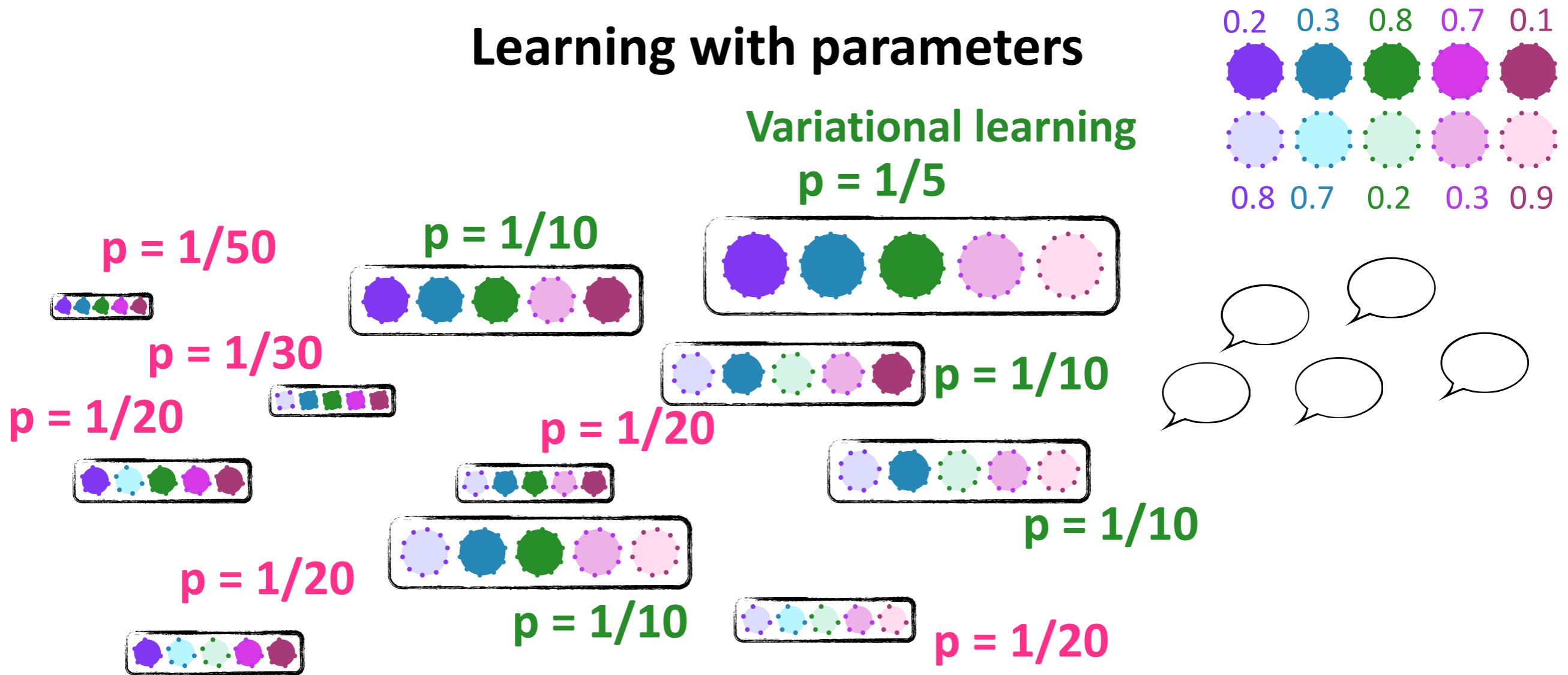
# Learning with parameters



As the child encounters data from the native language, some of the grammars will be more fit because they are better able to account for the syntactic properties of the intake.

Other grammars will be less fit because they cannot account for some of the data encountered.

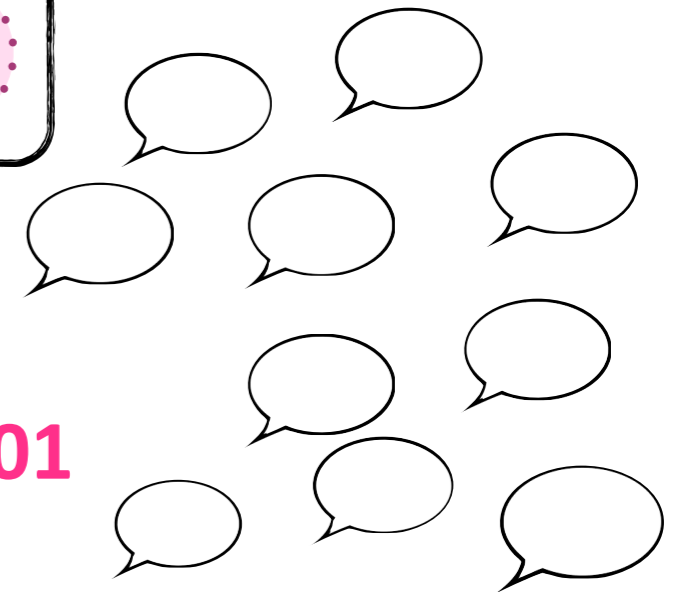
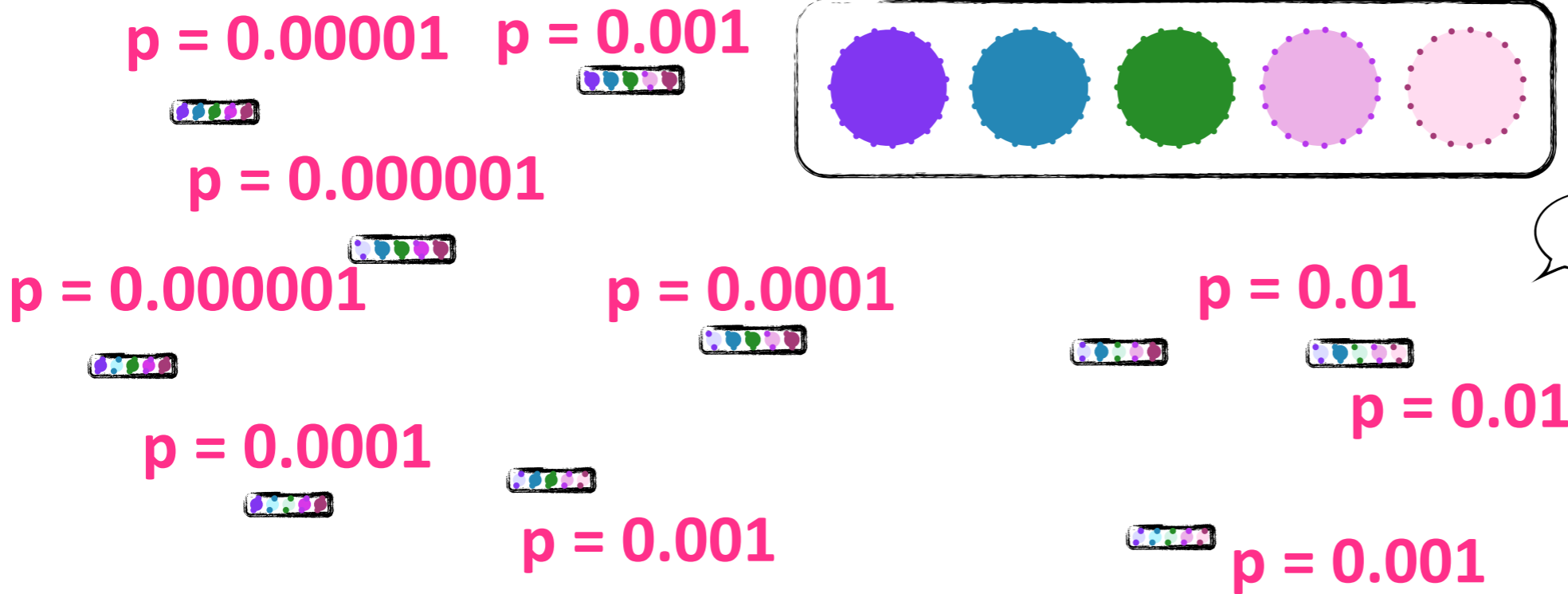
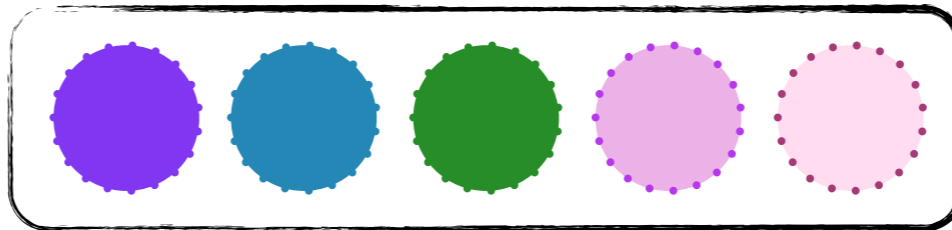
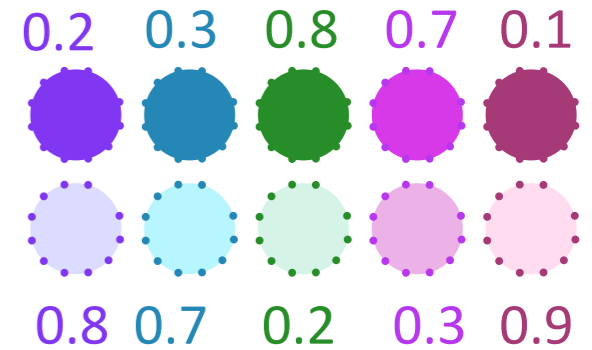
# Learning with parameters



Grammars that are more compatible with the native language data intake will have their **probabilities increased** while grammars that are less compatible will have their **probabilities decreased** over time.

# Learning with parameters

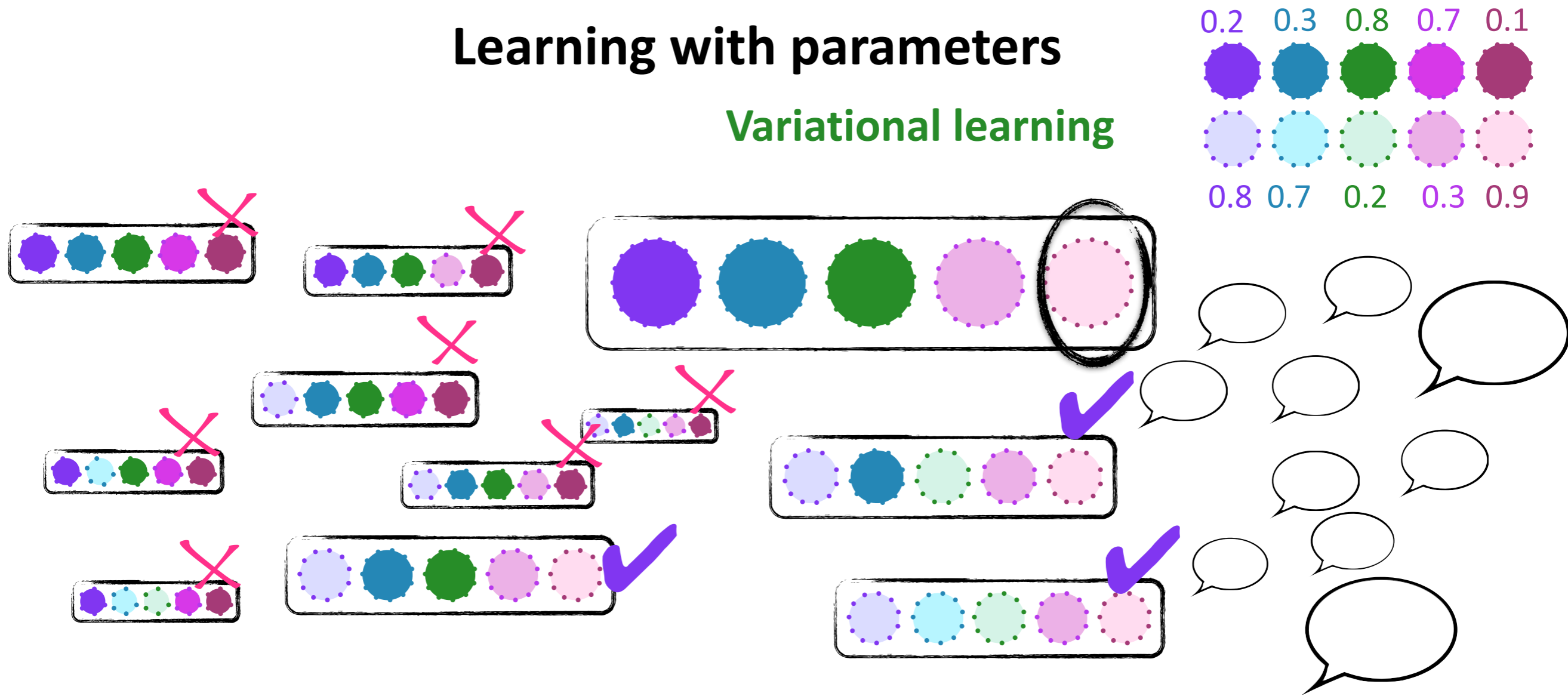
Variational learning  
 $p = 0.99$



After the child has encountered enough data from the native language, the native language grammar should have a probability near 1.0 while the other grammars have a probability near 0.0.

# Learning with parameters

## Variational learning



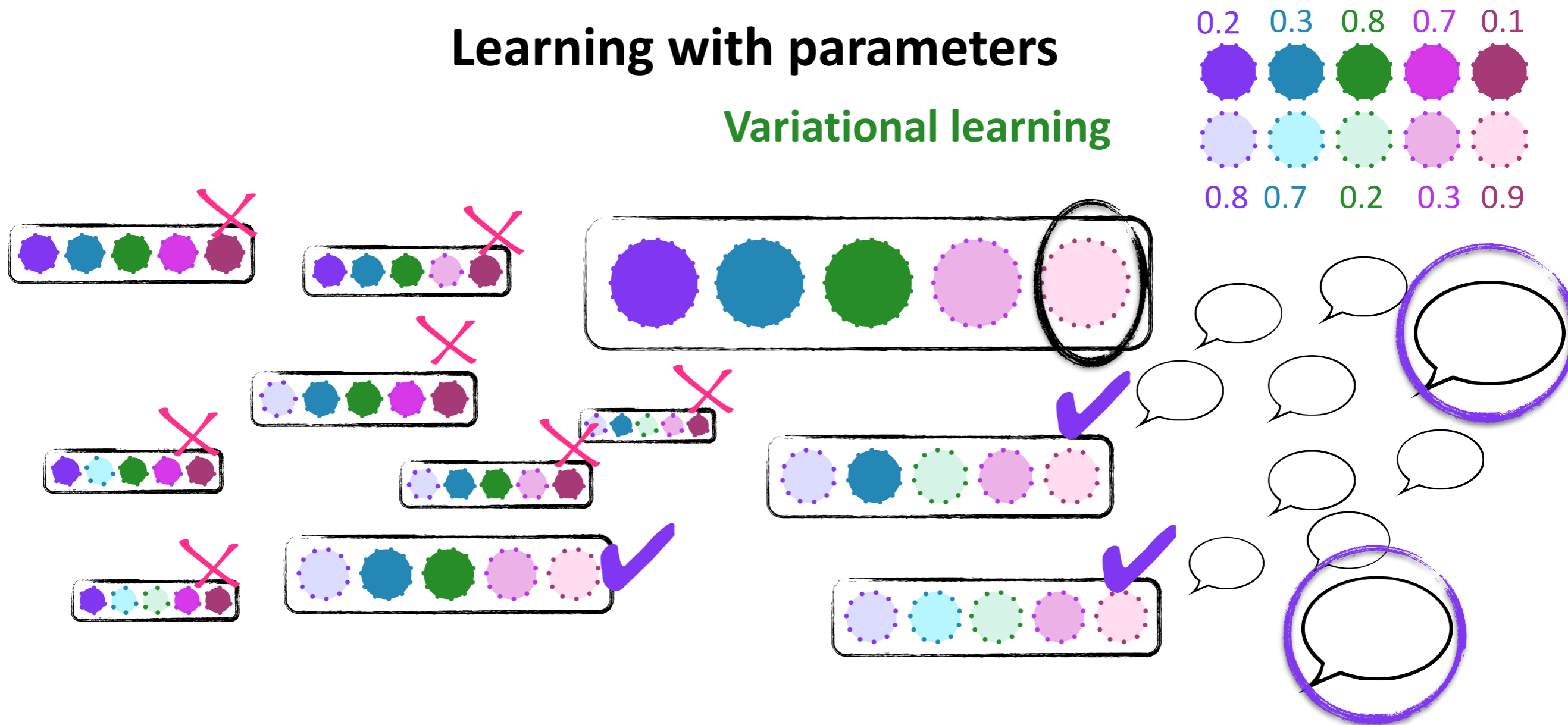
The power of **unambiguous data**:

Unambiguous data from the native language can only be analyzed by grammars that use the **native language's parameter value**.



# Learning with parameters

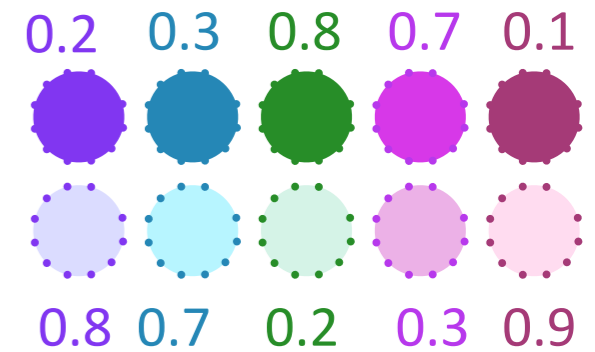
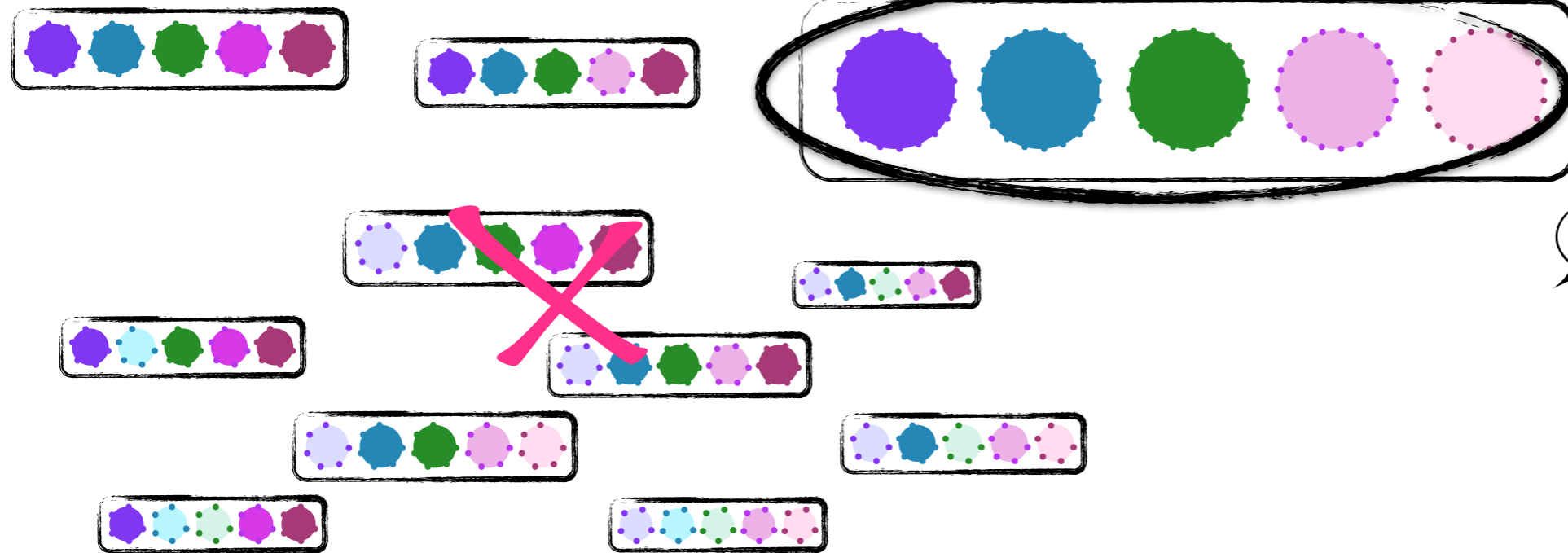
## Variational learning



This makes unambiguous data **very influential** data for the child to encounter, since these data are only compatible with the parameter value that is correct for the native language.

# Learning with parameters

## Variational learning

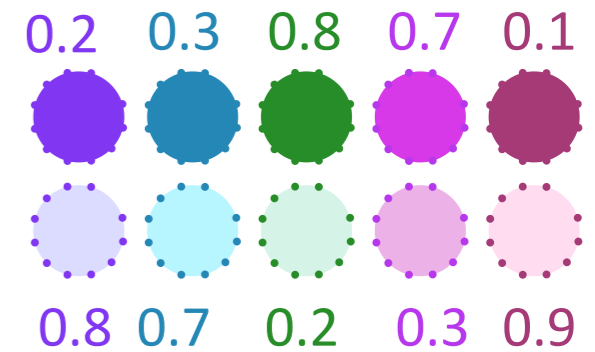
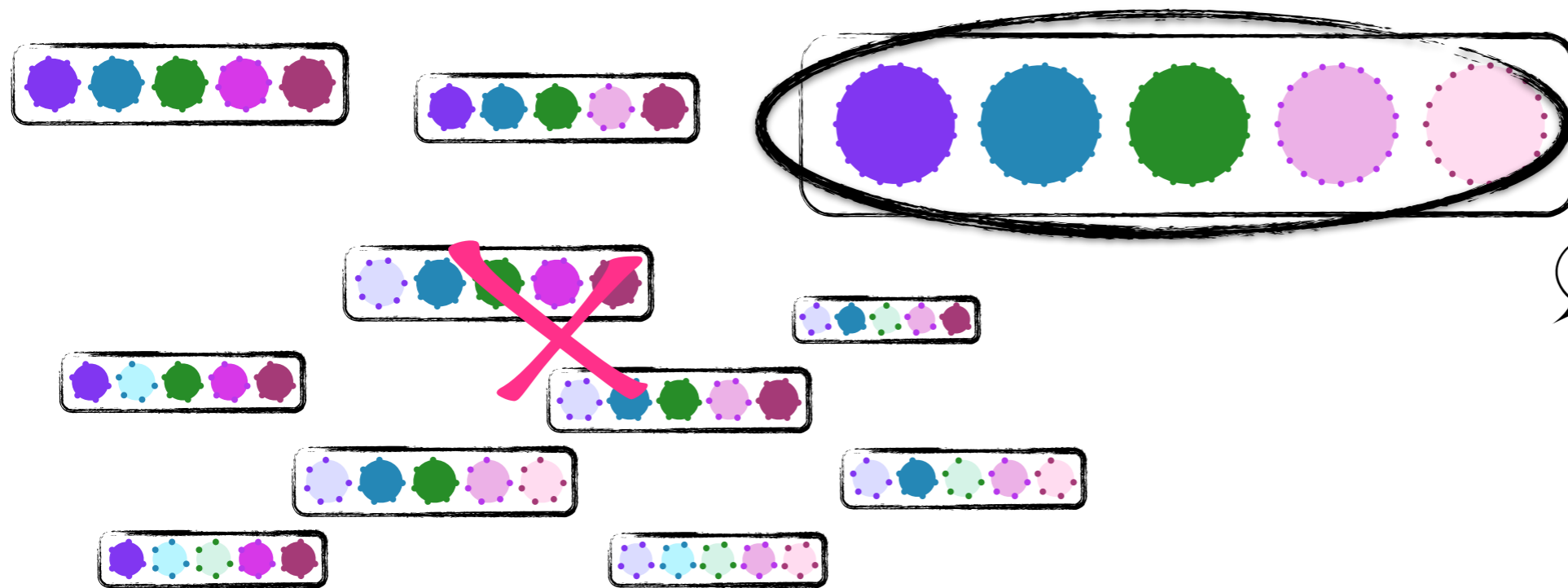


Problem: Do unambiguous data exist for entire grammars?

This requires data that are incompatible with every other possible parameter value of every other possible grammar....

# Learning with parameters

## Variational learning

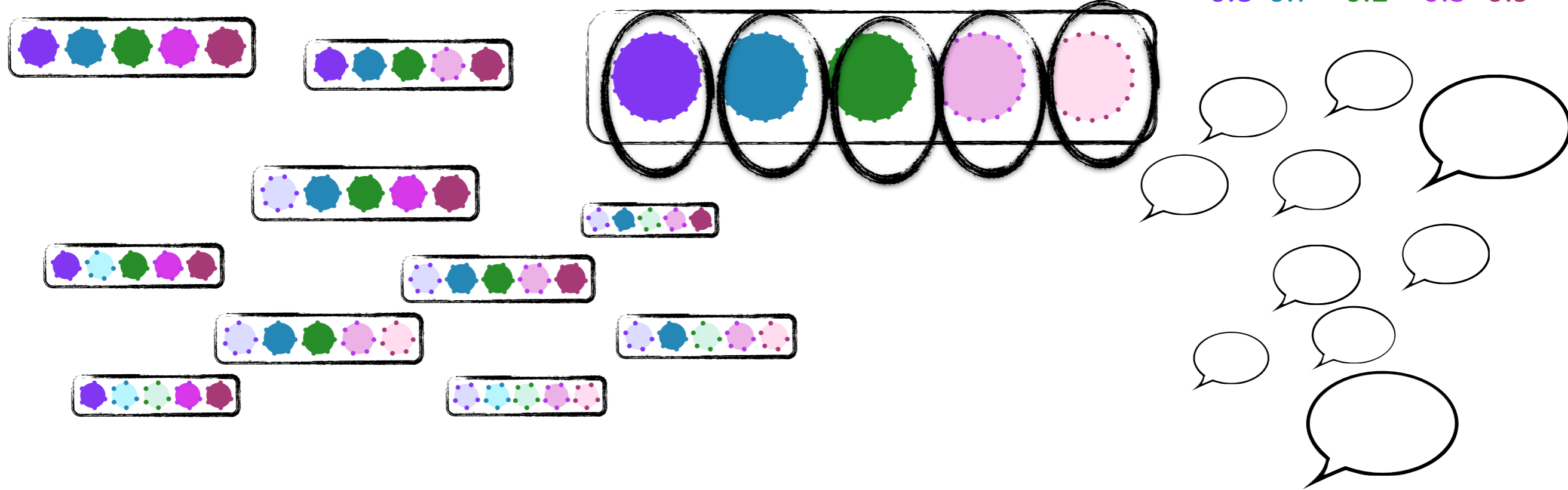


This seems unlikely for real language data because linguistic parameters connect with different types of patterns, which may have nothing to do with each other, or parameters may interact with each other.



# Learning with parameters

## Variational learning

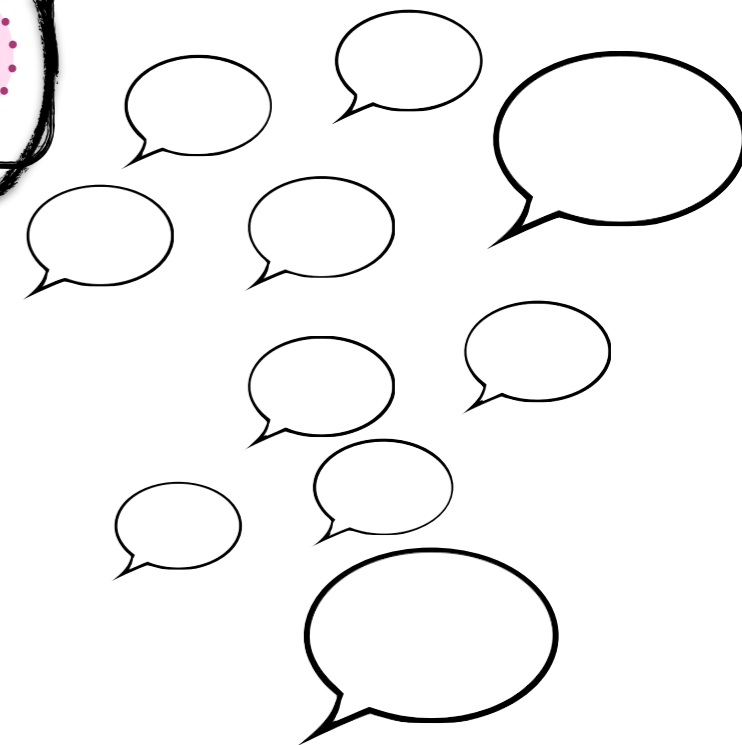
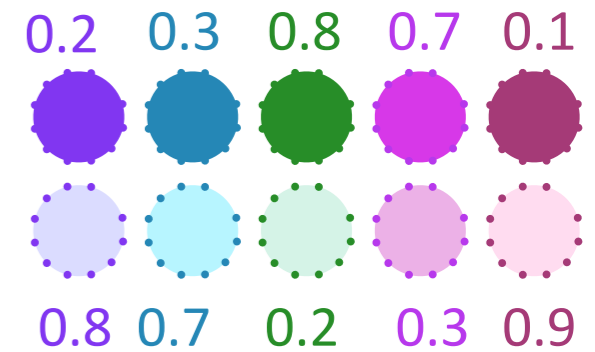
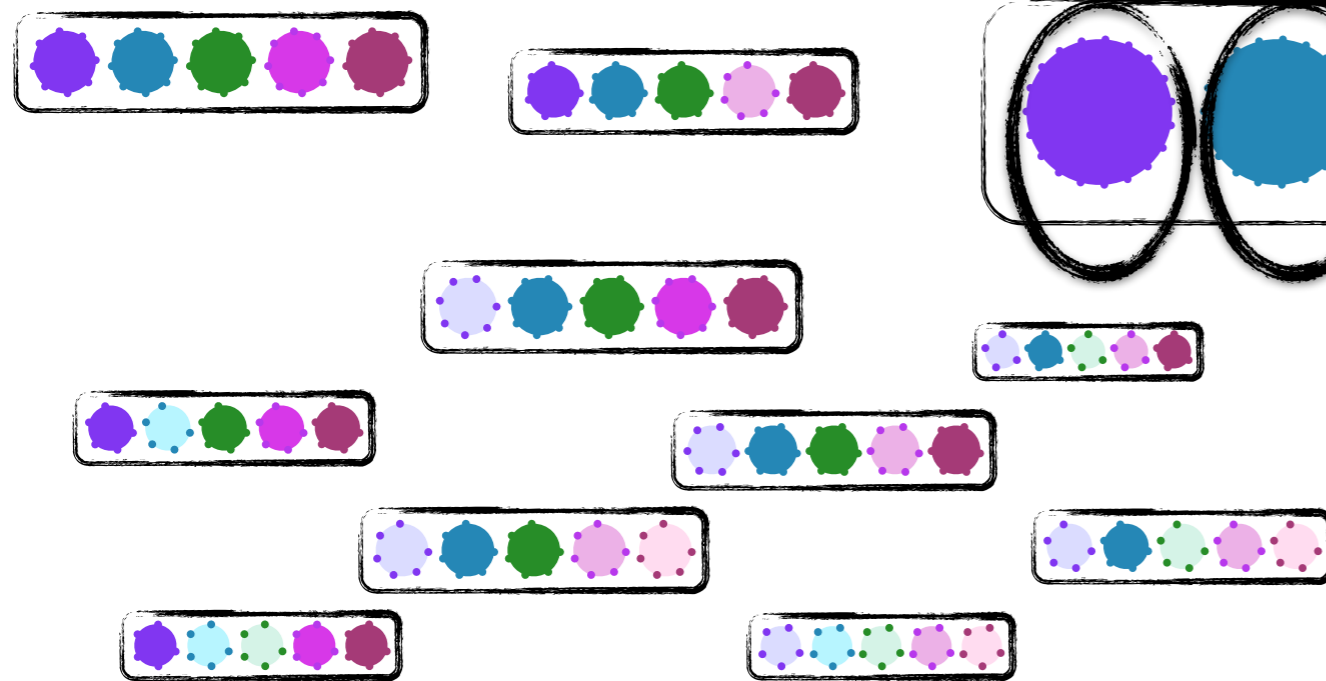


**Key: Parameters are separable components of grammars**



# Learning with parameters

## Variational learning

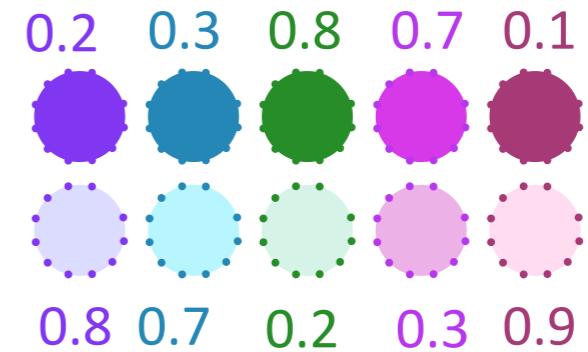
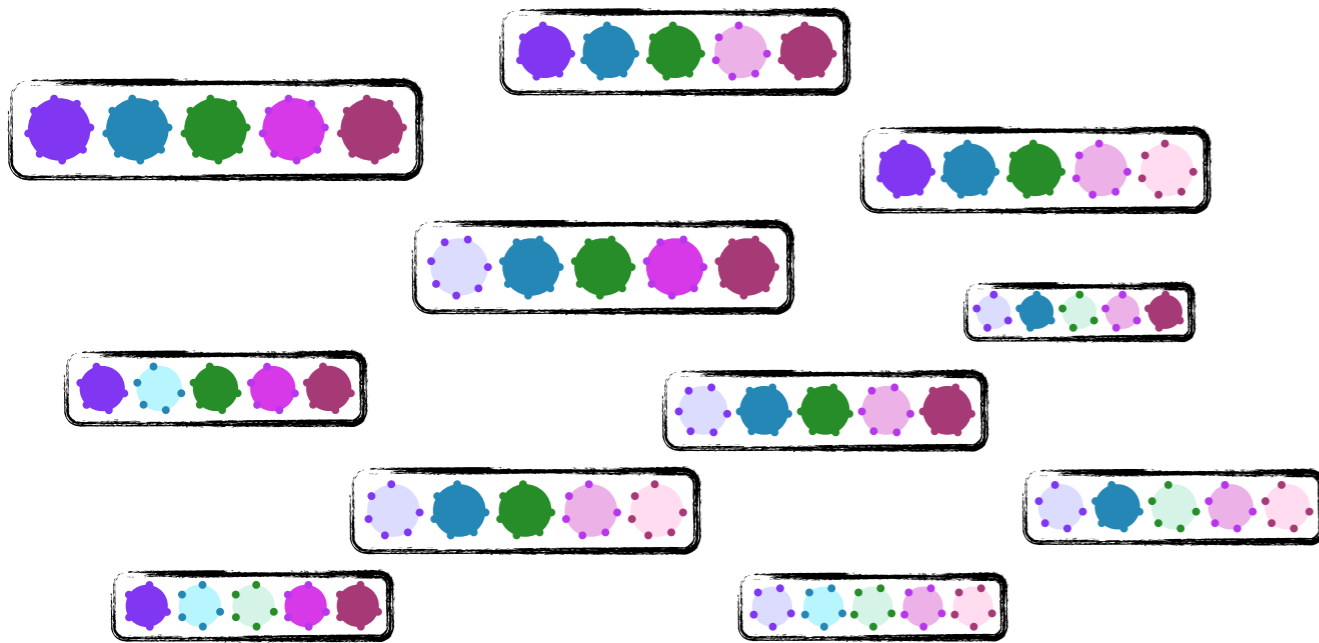


A **variational learner** can take advantage of the fact that grammars are really sets of parameter values.



# Learning with parameters

## Variational learning

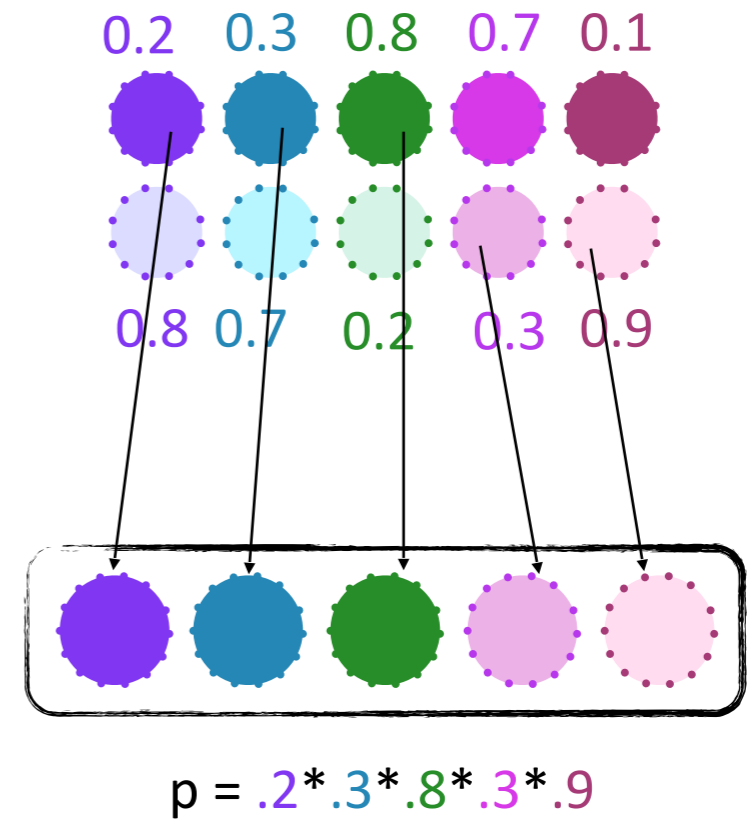
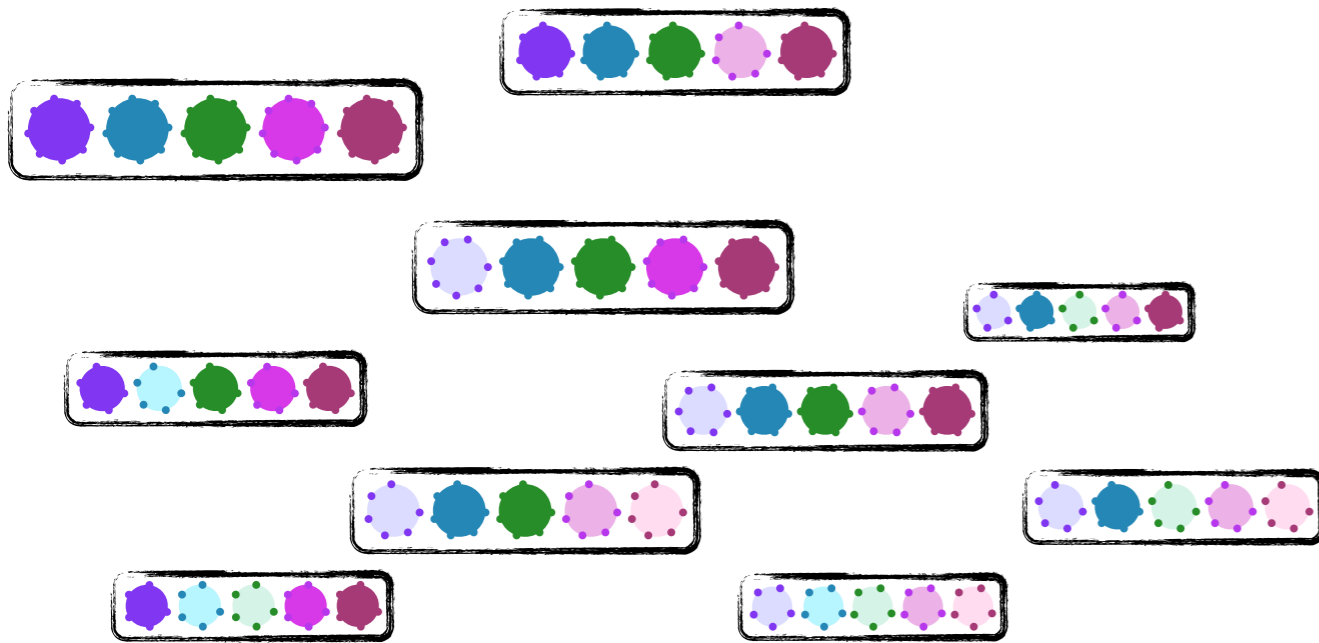


Parameter values can be probabilistically accessed, depending on the level of belief (probability) the learner currently has in each one.



# Learning with parameters

## Variational learning

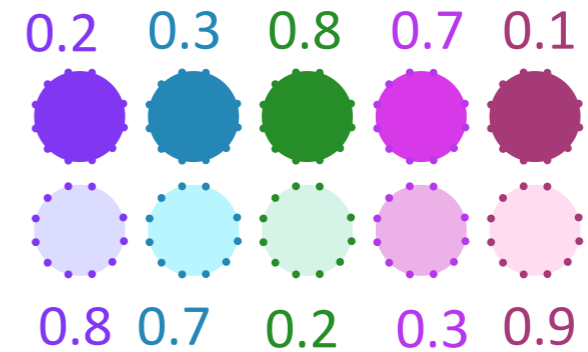
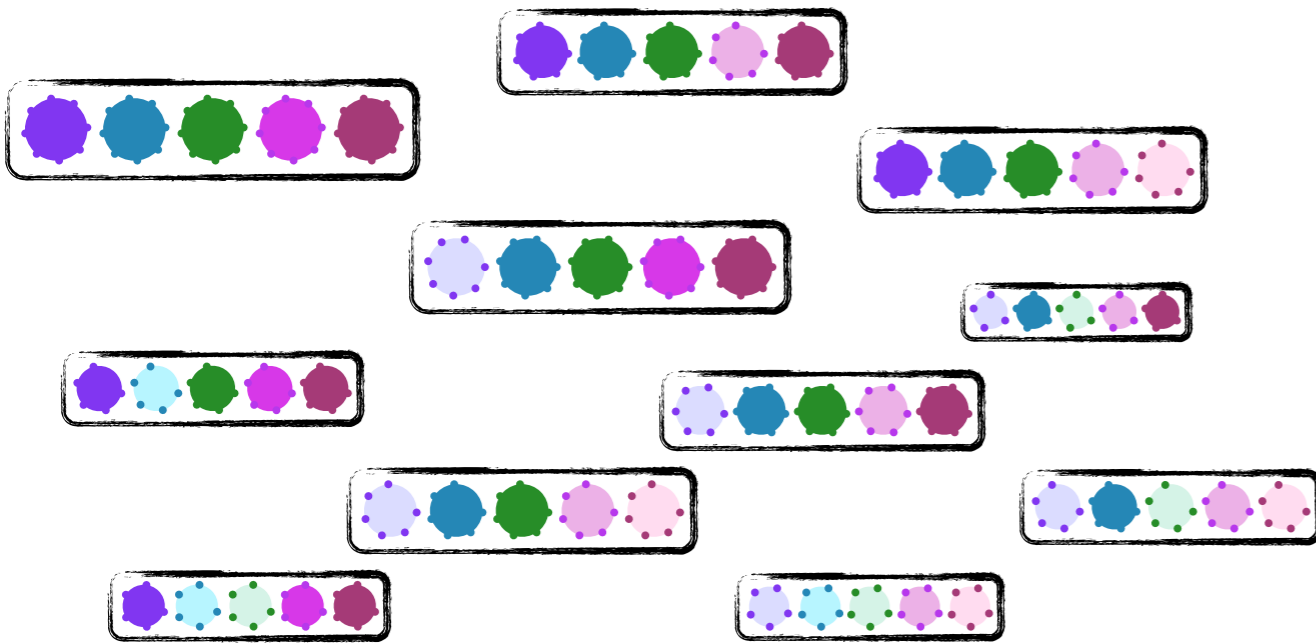


Parameter values can be probabilistically accessed, depending on the level of belief (probability) the learner currently has in each one.



# Learning with parameters

## Variational learning



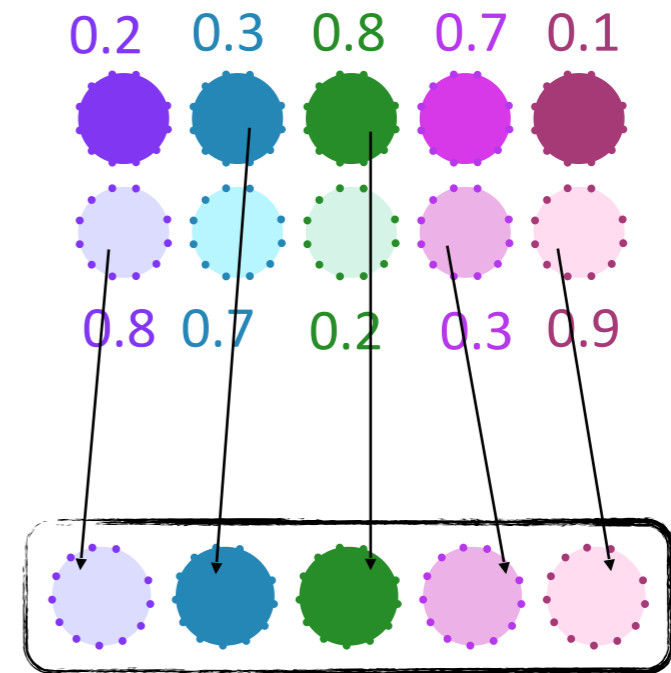
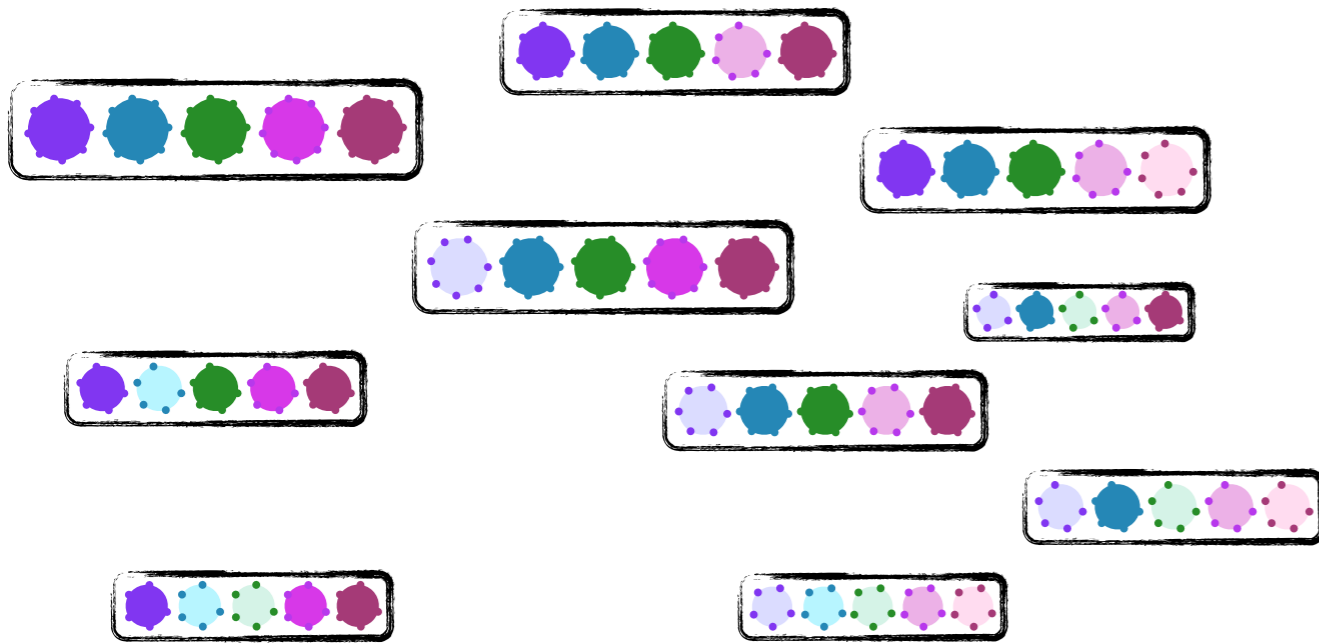
Parameter values can be probabilistically accessed, depending on the level of belief (probability) the learner currently has in each one.





# Learning with parameters

## Variational learning



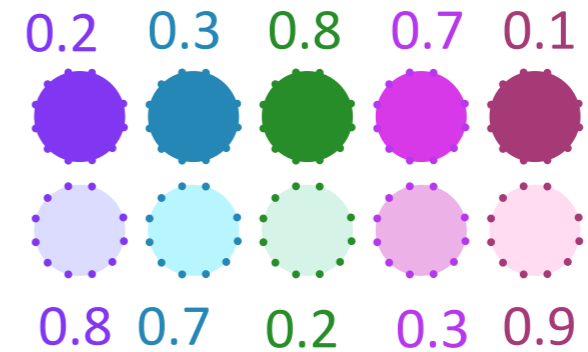
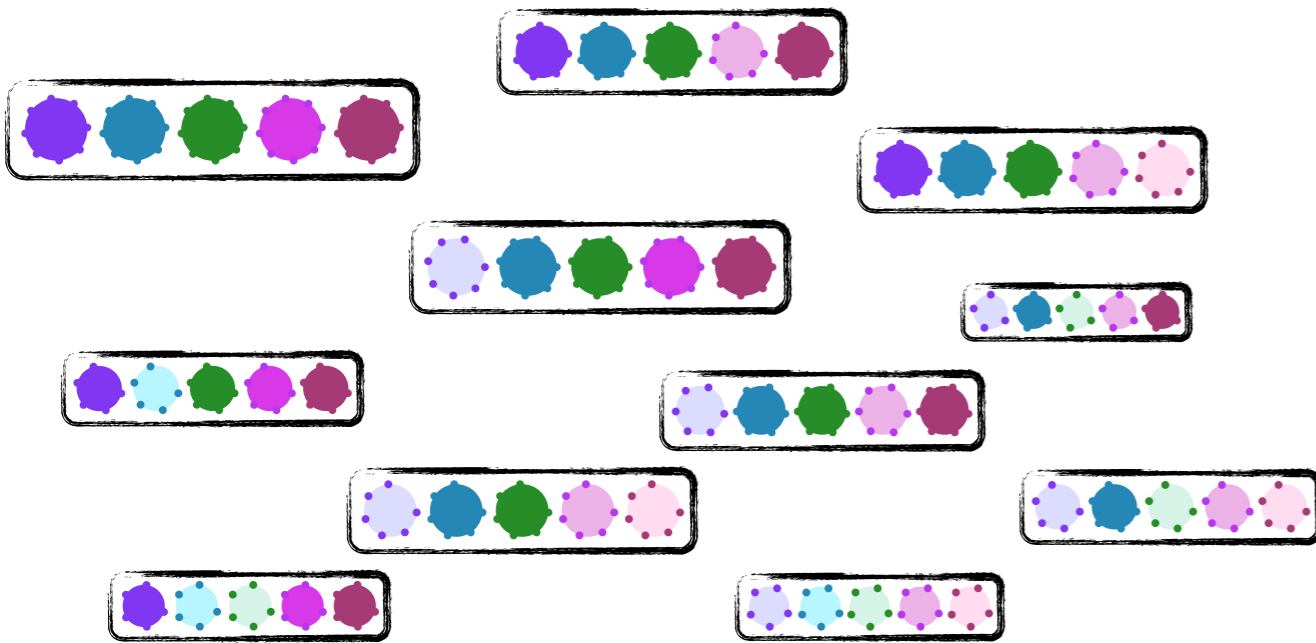
$$p = .8 * .3 * .8 * .3 * .9$$

Parameter values can be probabilistically accessed, depending on the level of belief (probability) the learner currently has in each one.



# Learning with parameters

## Variational learning

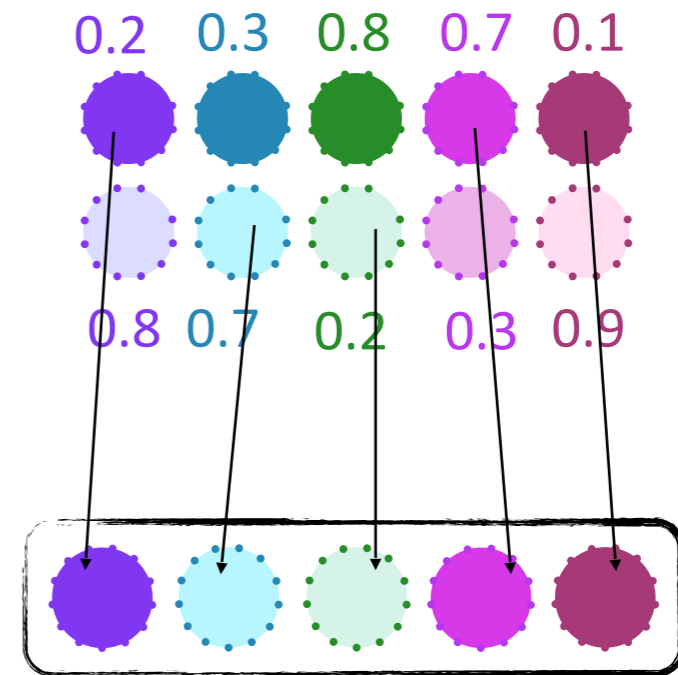
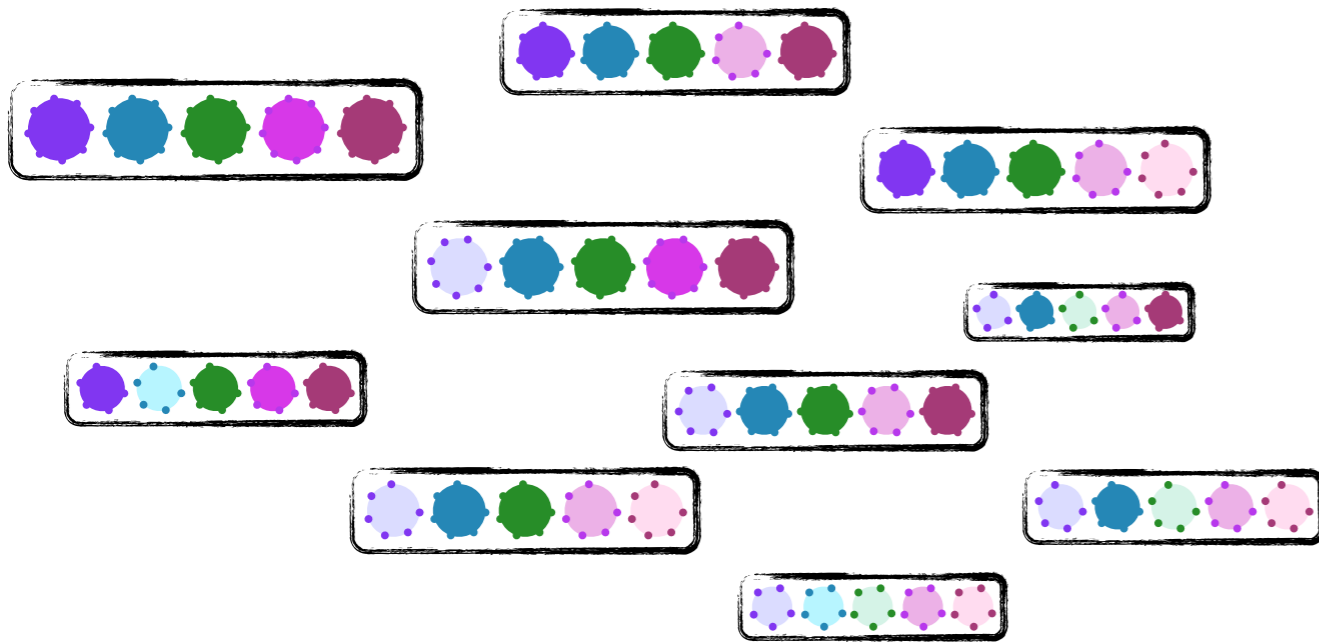


Parameter values can be probabilistically accessed, depending on the level of belief (probability) the learner currently has in each one.



# Learning with parameters

## Variational learning



$$p = .2 * .7 * .2 * .7 * .1$$

Parameter values can be probabilistically accessed, depending on the level of belief (probability) the learner currently has in each one.

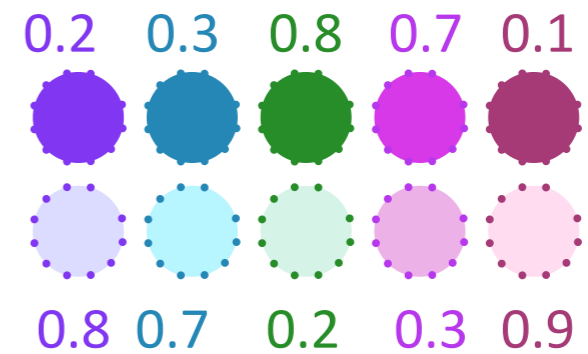
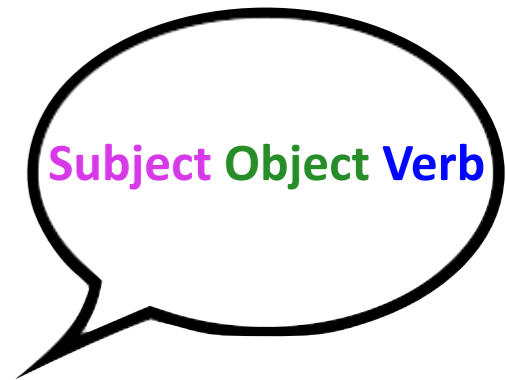


# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...



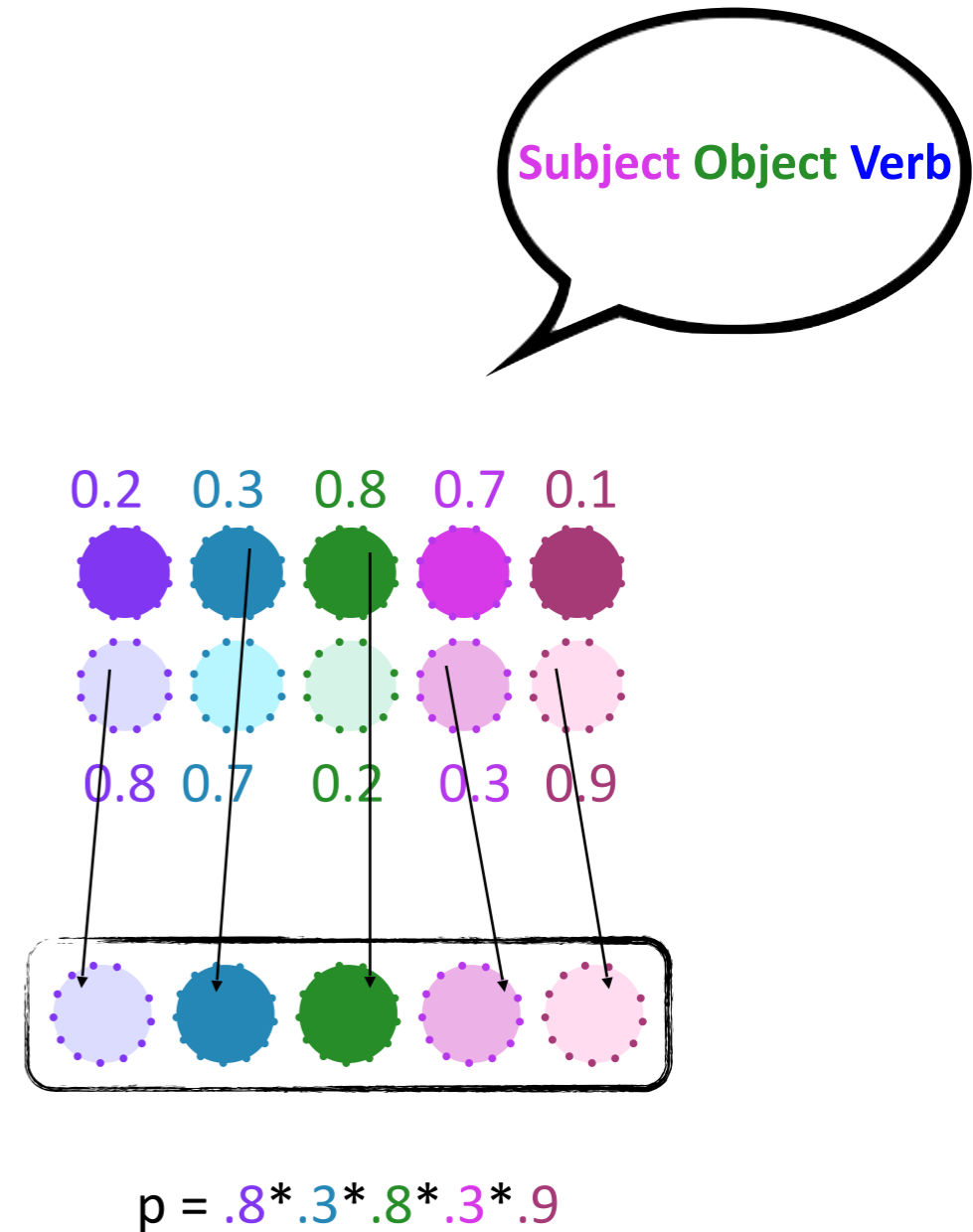
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

(1) Choose a grammar to test out on a particular data point. Select a grammar by choosing a set of parameter values, based on the probabilities associated with each parameter value.



Denison, Bonawitz, Gopnik, & Griffiths 2013:  
Experimental evidence from 4 and 5-year-olds suggests that children are sensitive to the probabilities of complex representations (which parameters are), and so this kind of **sampling** is not unrealistic.



# Learning with parameters

## The learning algorithm

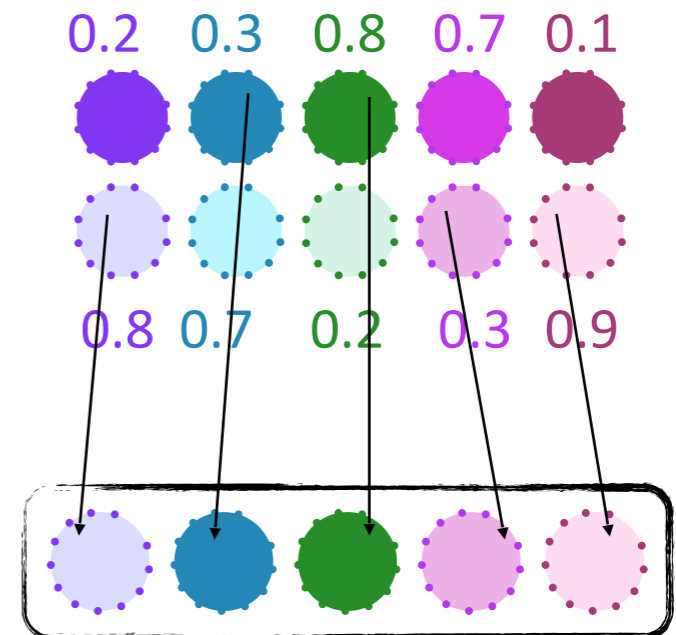
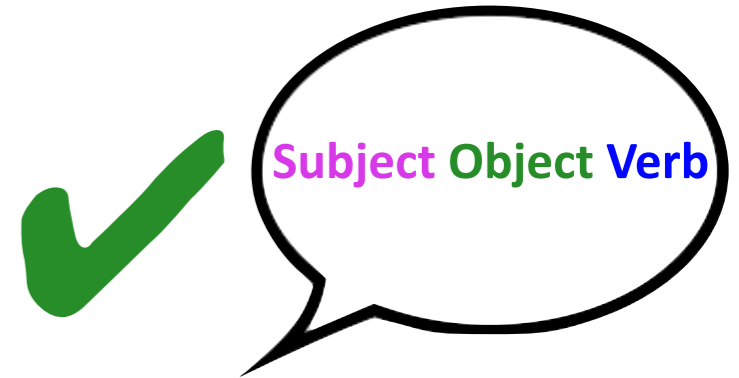
Variational learning

For each data point encountered in the input...

(1) Choose a grammar.

(2) Try to analyze the data point with this grammar.

If this grammar **can** analyze the data point, increase the probability of **all participating parameter** values slightly (**reward each value**).



$$p = .8 * .3 * .8 * .3 * .9$$

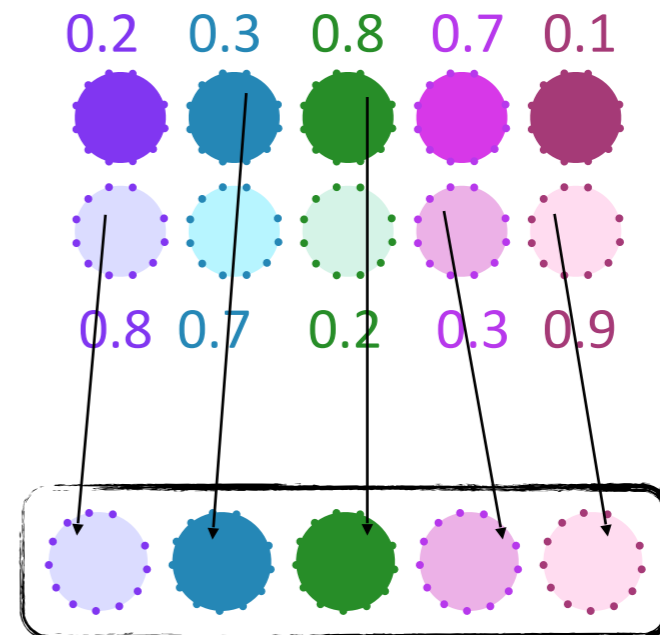
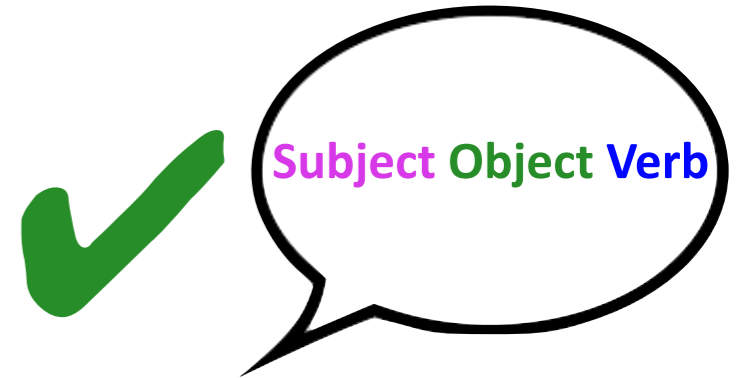
# Learning with parameters

## The learning algorithm

Variational learning


For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



1st parameter

Actual update equation for reward:  = .2

 = .8

$p_v$  = previous value of successful parameter value

$p_o$  = previous value of opposing parameter value

$$p = .8 * .3 * .8 * .3 * .9$$

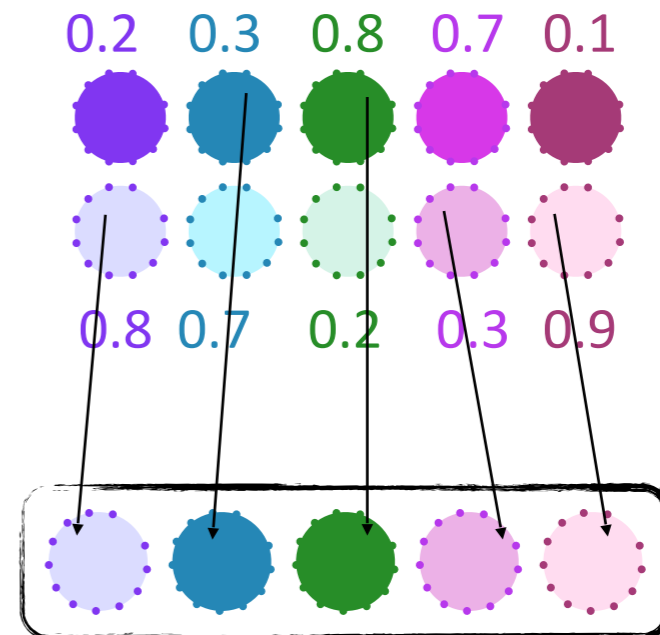
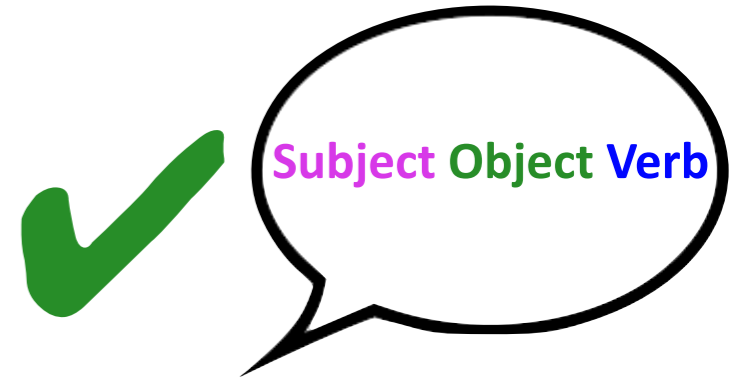
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



1st parameter

Actual update equation for reward:

$$\begin{aligned} \text{Solid purple circle} &= .2 \\ \text{Dotted purple circle} &= .8 \end{aligned}$$

$$p_v = 0.8$$

$$p_o = 0.2$$

$$p = .8 * .3 * .8 * .3 * .9$$



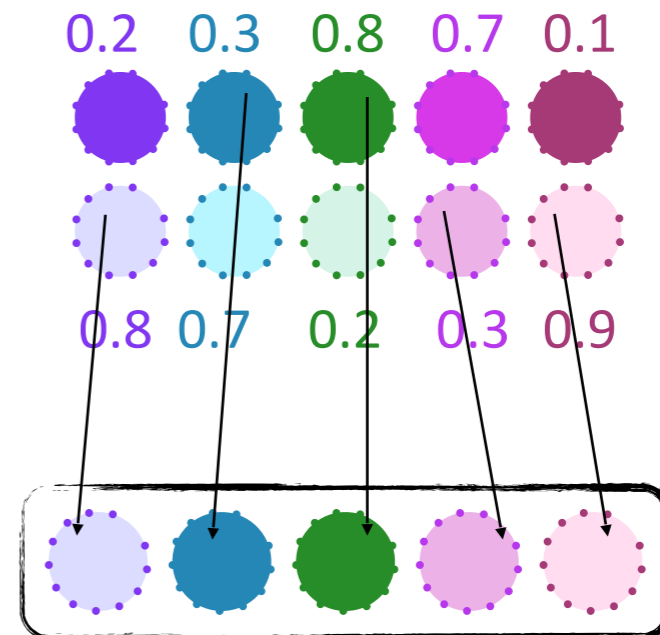
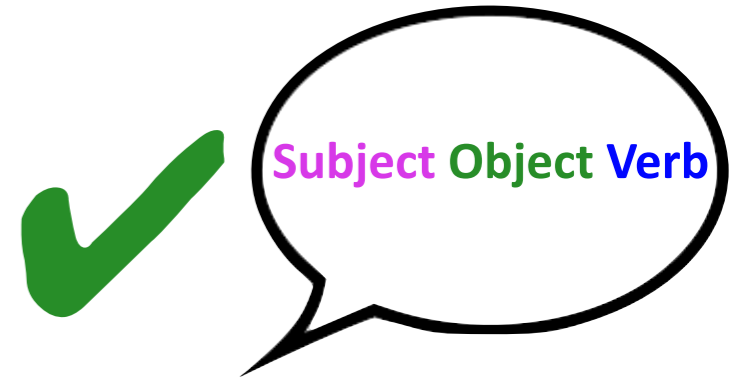
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



1st parameter

Actual update equation for reward:

$$\text{Solid purple circle} = .2$$
$$\text{Dotted purple circle} = .8$$

$$p_v = 0.8$$

$$p_o = 0.2$$

$$p_{v\_updated} = p_v + \gamma(1 - p_v)$$

$$p_{o\_updated} = (1 - \gamma)p_o$$

$\gamma$  = learning rate (ex:  $\gamma = .125$ )

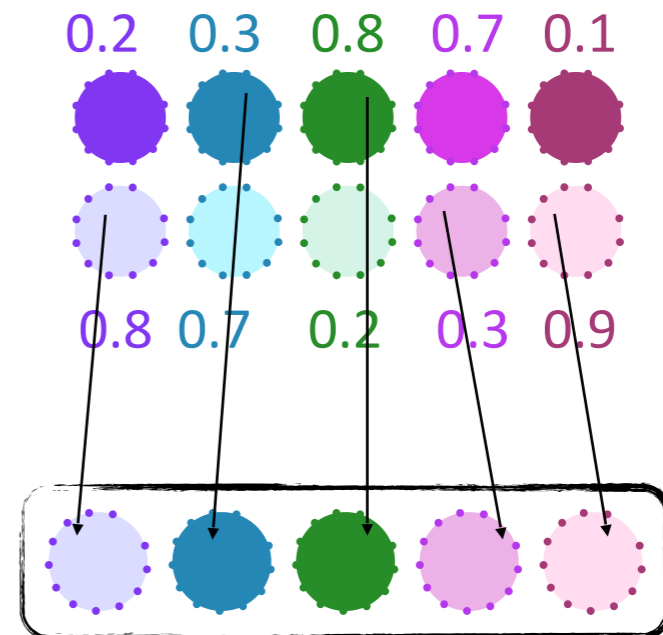
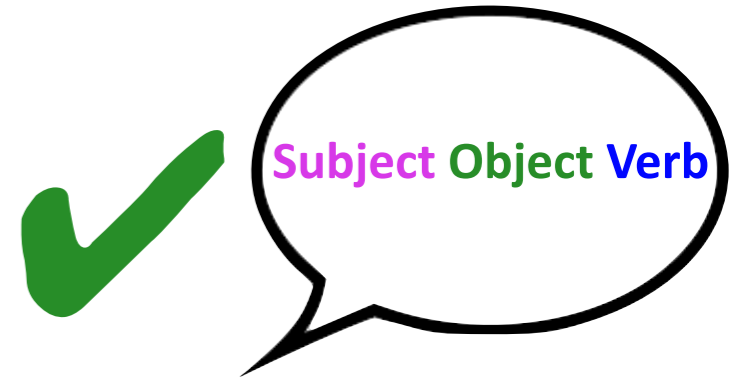
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



1st parameter

Actual update equation for reward:

$$\text{Solid purple circle} = .2$$
$$\text{Dotted purple circle} = .8$$

$$p_v = 0.8$$

$$p_o = 0.2$$

$$p_{v\_updated} = 0.8 + 0.125(1 - 0.8)$$

$$p_{o\_updated} = (1 - 0.125)0.2$$

$\gamma$  = learning rate (ex:  $\gamma = .125$ )

$$p = .8 * .3 * .8 * .3 * .9$$

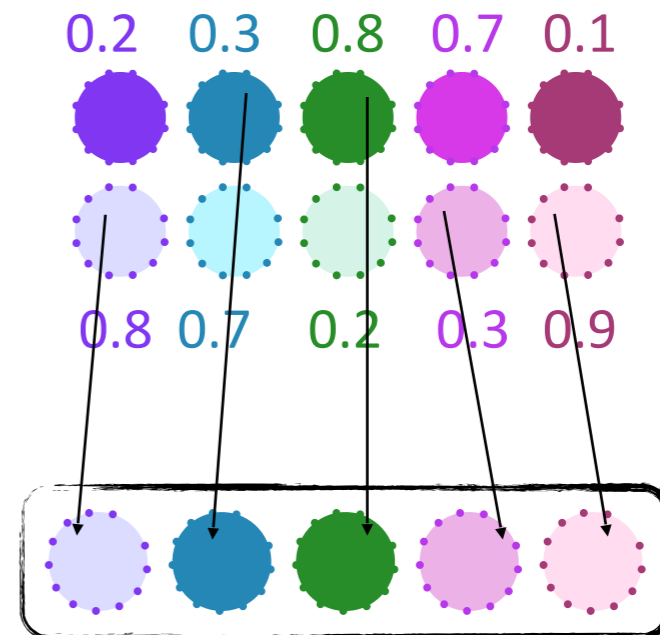
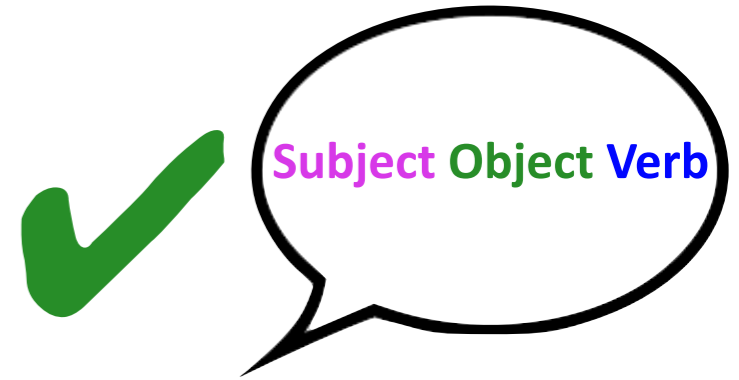
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



1st parameter

Actual update equation for reward:

$$\begin{aligned} \text{Solid purple circle} &= .2 \\ \text{Dotted purple circle} &= .8 \end{aligned}$$

$$p_v = 0.8$$

$$p_o = 0.2$$

$$p_{v\_updated} = 0.825$$

$$p_{o\_updated} = 0.175$$

$$p = .8 * .3 * .8 * .3 * .9$$

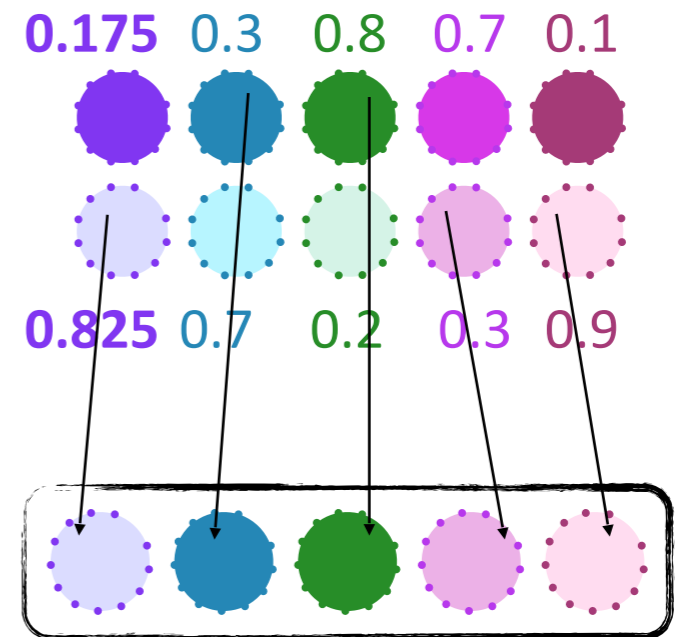
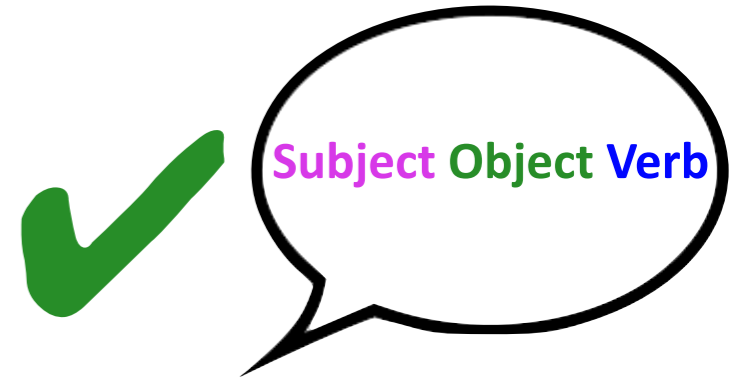
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



1st parameter

Actual update equation for reward:

$$\text{Solid circle} = .2$$
$$\text{Dotted circle} = .8$$

$$p_v = 0.8$$

$$p_o = 0.2$$

$$p_{v\_updated} = 0.825$$

$$p_{o\_updated} = 0.175$$

$$p = .8 * .3 * .8 * .3 * .9$$

Do this for all the other parameters, too.

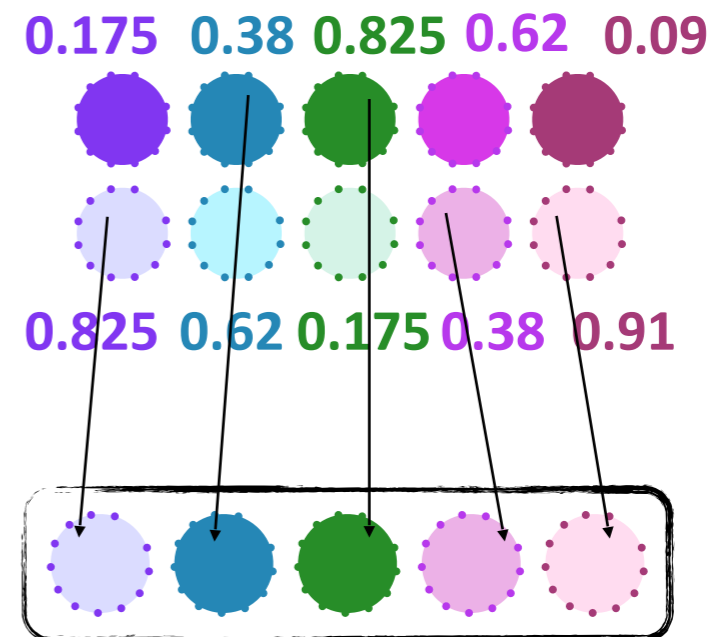
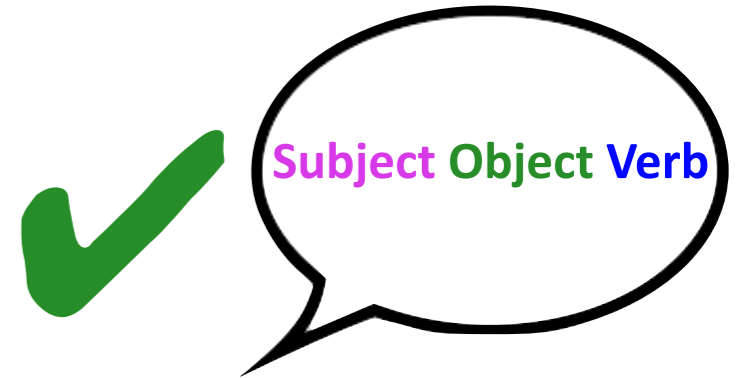
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



$$p = .8 * .3 * .8 * .3 * .9$$

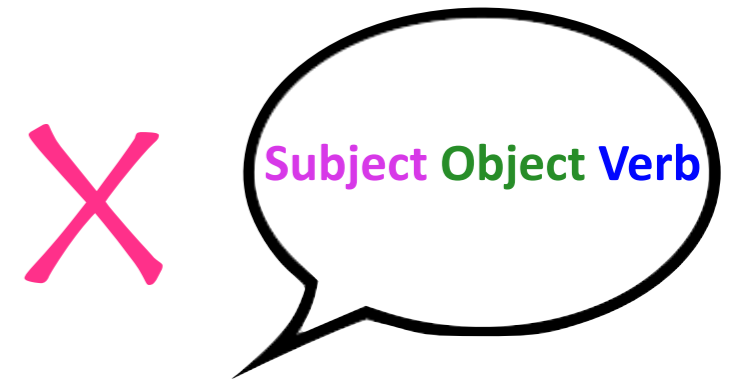
# Learning with parameters

## The learning algorithm

Variational learning

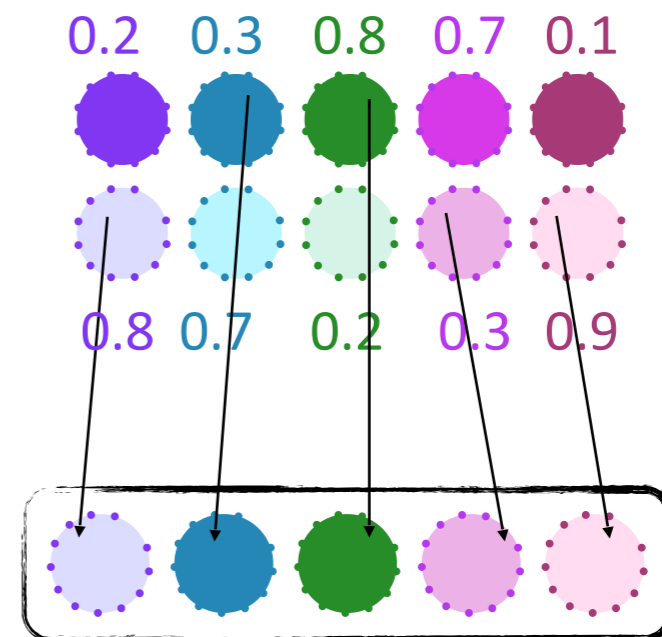
For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



**But what happens if the selected grammar can't account for the data point?**

Then all the participating parameter values are **punished**.



$$p = .8 * .3 * .8 * .3 * .9$$

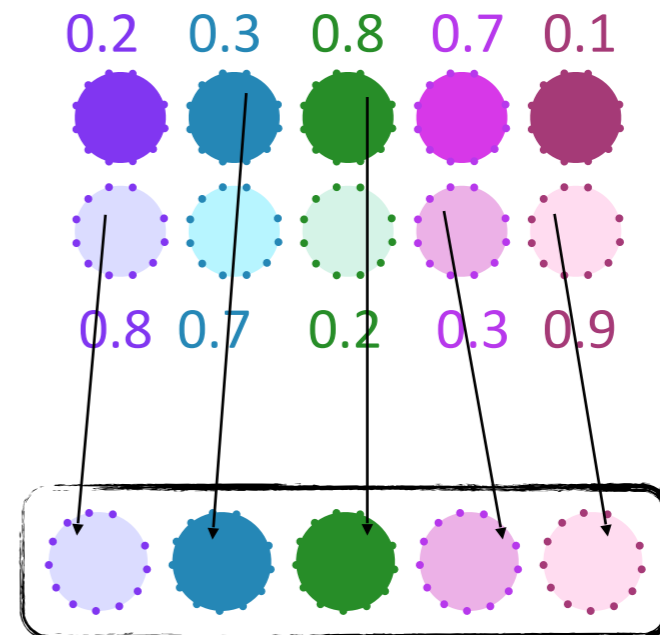
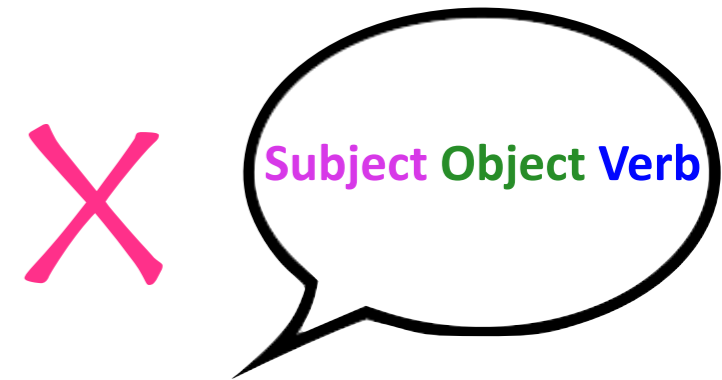
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



1st parameter

Actual update equation for **punishment**: = .2  
 = .8

$p_v$  = previous value of unsuccessful parameter value  
 $p_o$  = previous value of opposing parameter value

$$p = .8 * .3 * .8 * .3 * .9$$

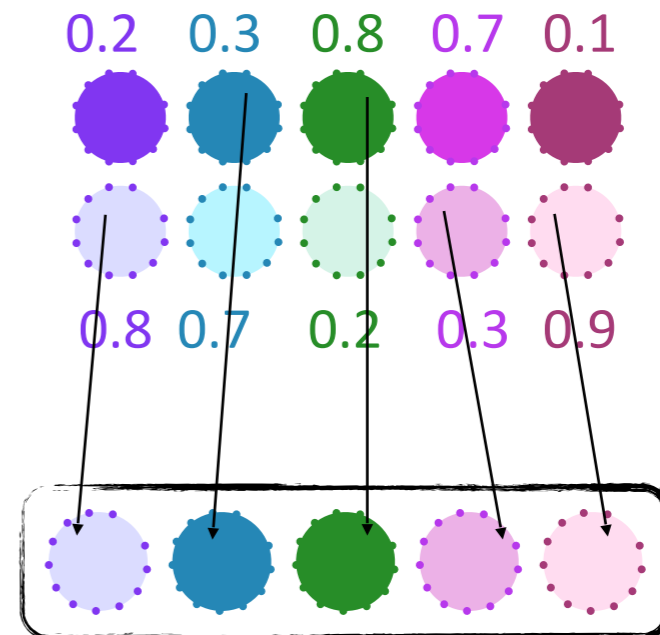
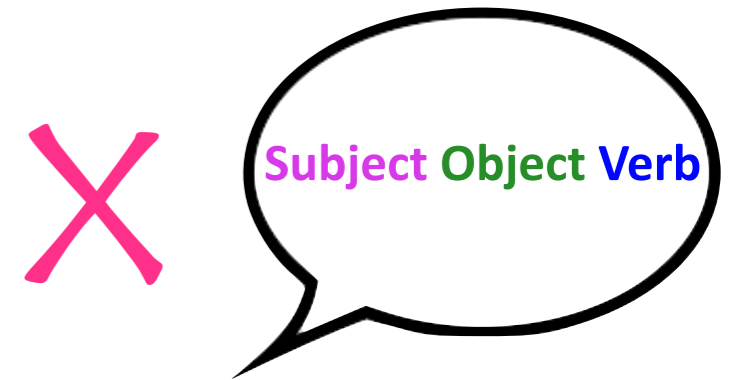
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



1st parameter

Actual update equation for **punishment**: ● = .2

$$p_v = 0.8$$
$$p_o = 0.2$$

● = .8

$$p = .8 * .3 * .8 * .3 * .9$$



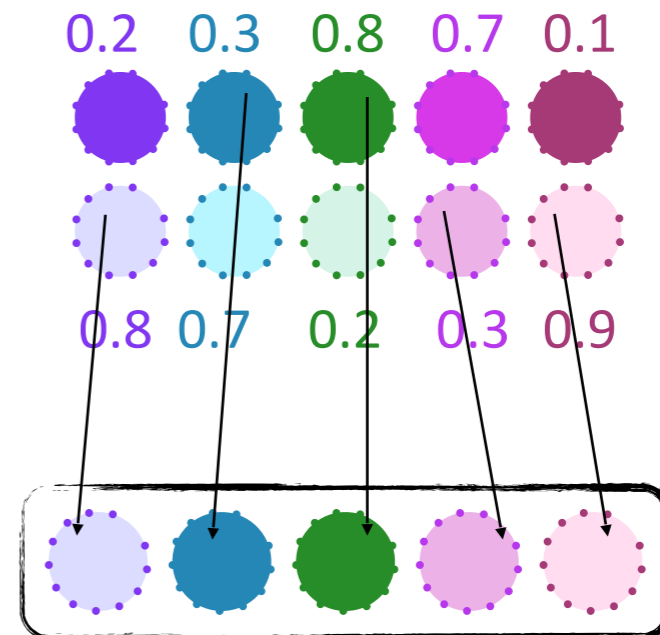
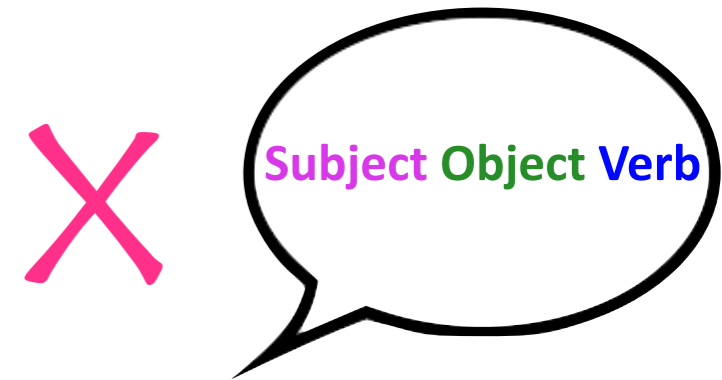
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



1st parameter

Actual update equation for **punishment**: = .2

= .8

$$p_v = 0.8$$

$$p_o = 0.2$$

$$p_{v\_updated} = (1-\gamma)p_v$$

$$p_{o\_updated} = \gamma + (1-\gamma)p_o$$

$\gamma$  = learning rate (ex:  $\gamma = .125$ )

$$p = .8 * .3 * .8 * .3 * .9$$

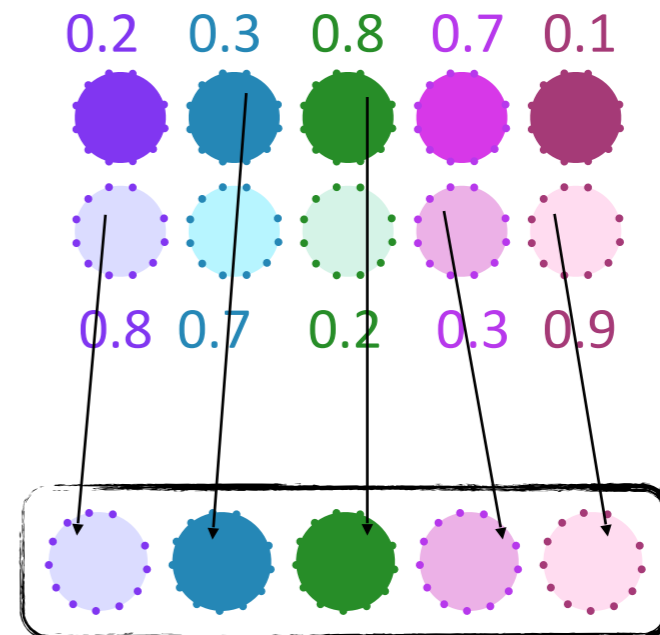
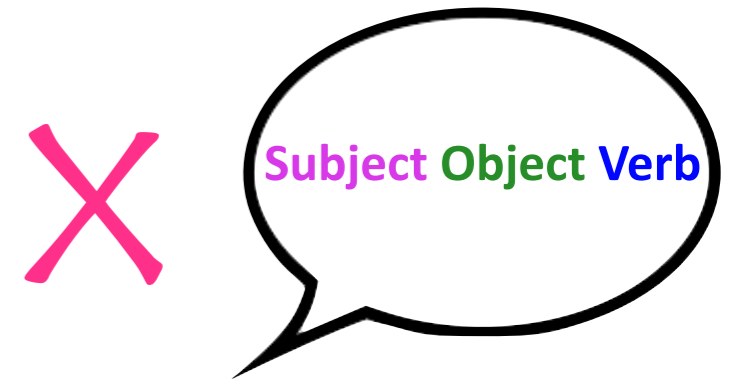
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



1st parameter

Actual update equation for **punishment**:  = .2

 = .8

$$p_v = 0.8$$

$$p_o = 0.2$$

$$p_{v\_updated} = (1-0.125)0.8$$

$$p_{o\_updated} = 0.125 + (1-0.125)0.2$$

$$p = .8*.3*.8*.3*.9$$

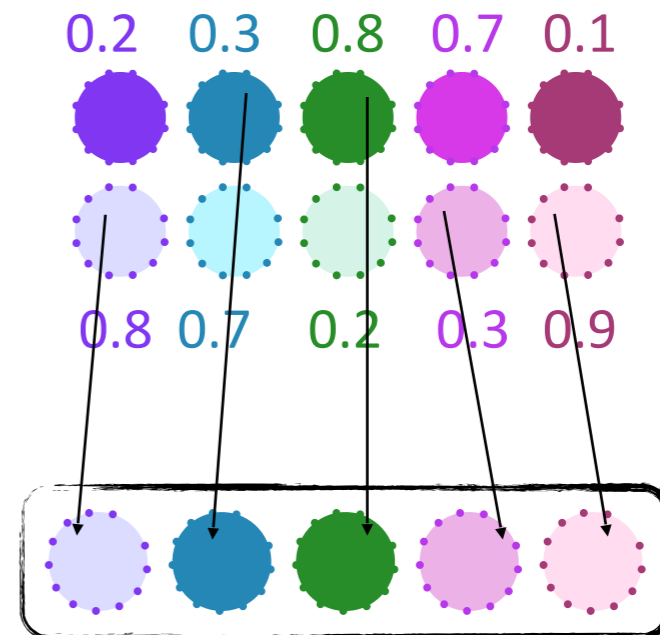
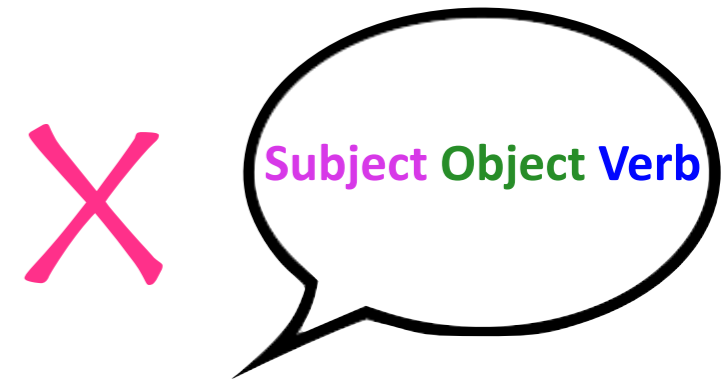
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



1st parameter

Actual update equation for **punishment**:  = .2

 = .8

$$p_v = 0.8$$

$$p_o = 0.2$$

$$p_{v\_updated} = 0.70$$

$$p_{o\_updated} = 0.30$$

$$p = .8 * .3 * .8 * .3 * .9$$

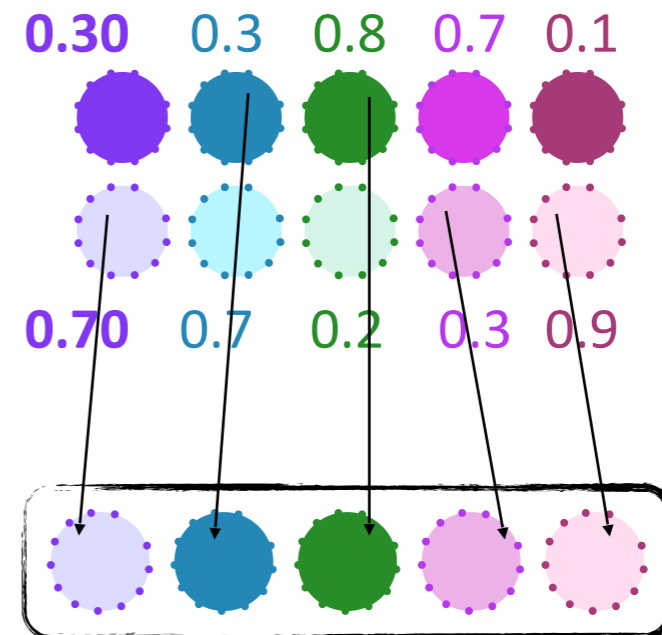
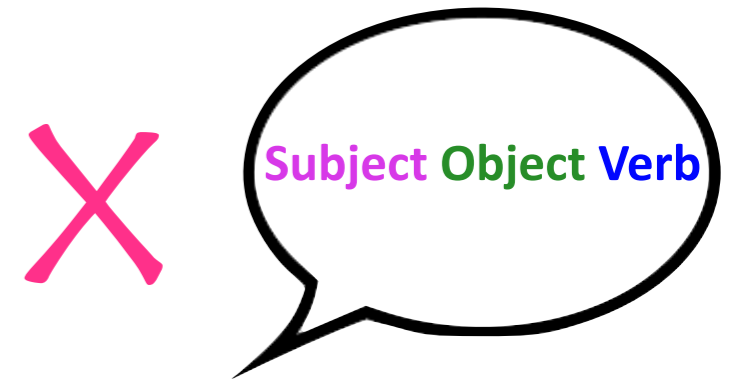
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



1st parameter

Actual update equation for **punishment**: = .2

= .8

$$p_v = 0.8$$
$$p_o = 0.2$$

$$p_{v\_updated} = 0.70$$
$$p_{o\_updated} = 0.30$$

Do this for all the other parameters, too.

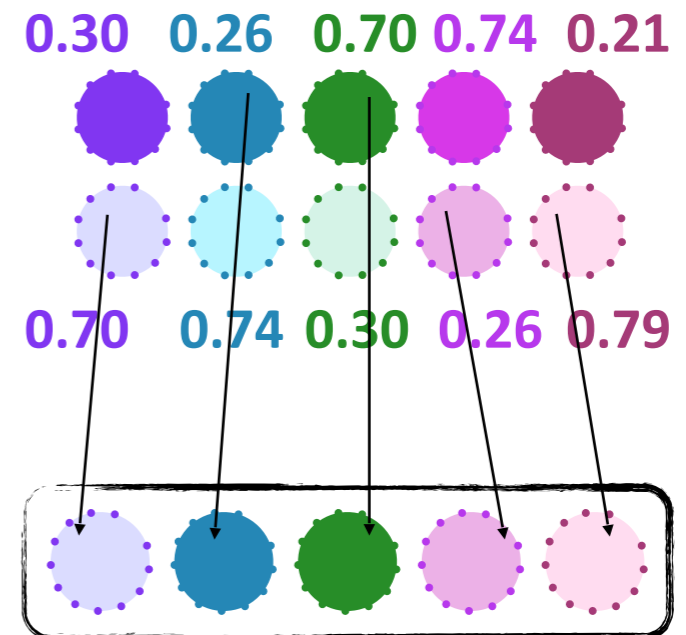
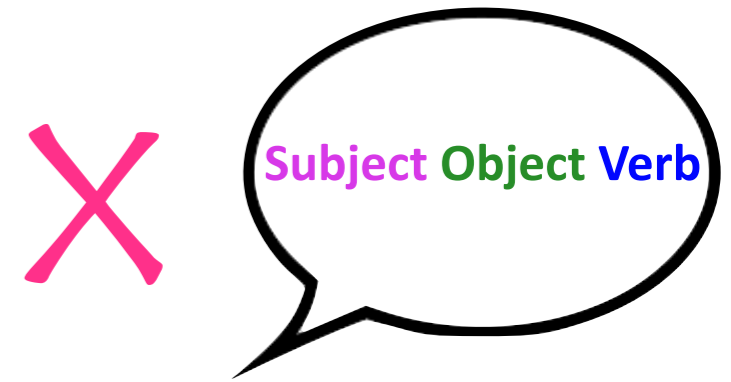
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



$$p = .8 * .3 * .8 * .3 * .9$$

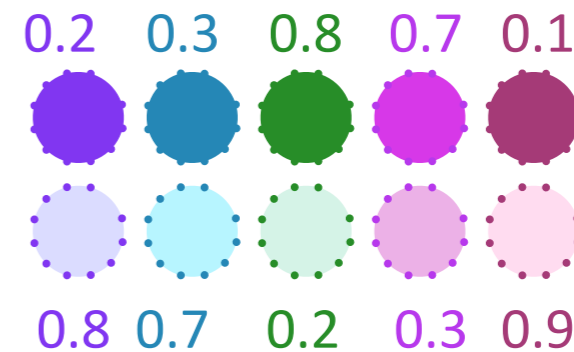
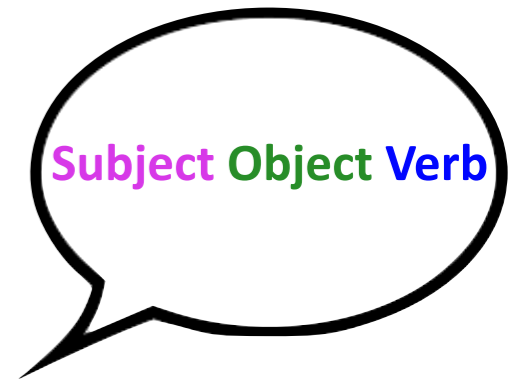
# Learning with parameters

## The learning algorithm

Variational learning

For each data point encountered in the input...

- (1) Choose a grammar.
- (2) Try to analyze the data point with this grammar.
- (3) Update parameter value probabilities.



Problem ameliorated!

**Unambiguous data** are much more likely to exist for **individual parameter values** instead of entire grammars.

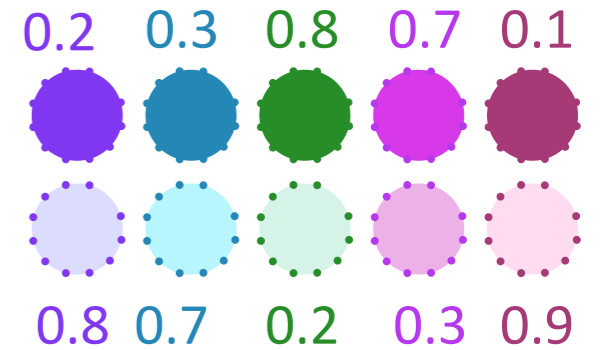




# Learning with parameters

## The learning algorithm

### Variational learning



Unambiguous data are much more likely to exist for individual parameter values instead of entire grammars.



Head-directionality    Subject drop (subj-drop)



“...dass **ich**  
**Kätzchen liebe.**”  
*...that I Kitties love*

Subject    Object    Verb

**G2** Head-final   
+subj-drop

**G4** Head-final  
-subj-drop

**G1** Head-first   
+subj-drop

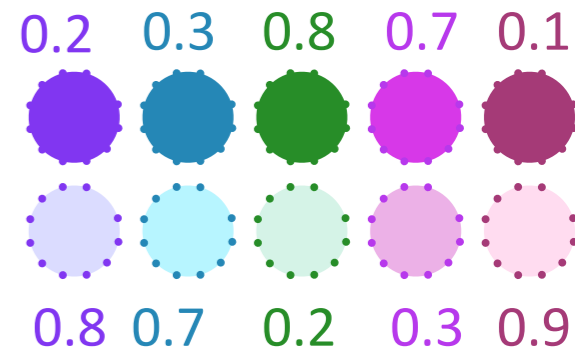
**G3** Head-first   
-subj-drop



# Learning with parameters

## The learning algorithm

### Variational learning



In this case, if either G2 or G4 were selected, head-final would be rewarded (in addition to whichever subj-drop value was used).



Head-directionality    Subject drop (subj-drop)



“...dass **ich**  
**Kätzchen liebe.**”  
...that *I Kitties love*

**Subject    Object    Verb**

**G2** Head-final   
+subj-drop

**G4** Head-final  
-subj-drop

**G1** Head-first   
+subj-drop

**G3** Head-first   
-subj-drop

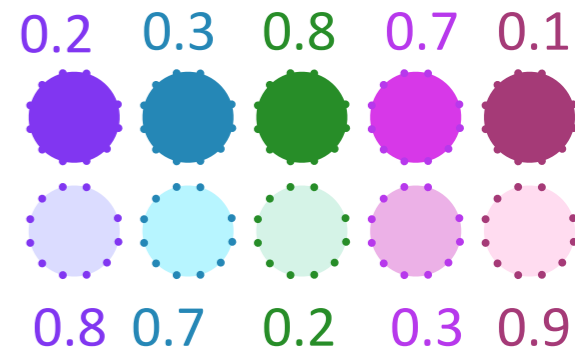




# Learning with parameters

## The learning algorithm

### Variational learning



In this case, if either G1 or G3 were selected, head-first would be punished (in addition to whichever subj-drop value was used).



Head-directionality    Subject drop (subj-drop)



“...dass **ich**  
**Kätzchen liebe.**”  
...that *I Kitties love*

**Subject**    **Object**    **Verb**

~~G1~~ Head-first +subj-drop

~~G3~~ Head-first -subj-drop

**G2** Head-final +subj-drop

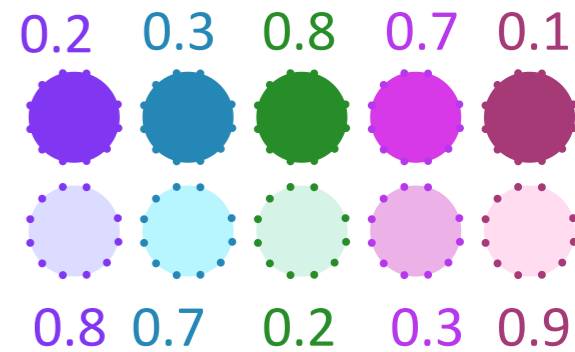
**G4** Head-final -subj-drop



# Learning with parameters

## The learning algorithm

### Variational learning



Because this data point is unambiguous for **head-final**, grammars using that value would be rewarded and its probability as a parameter value would become 1.0 over time.



Head-directionality    Subject drop (subj-drop)

“...dass **ich**  
**Kätzchen liebe.**”  
...that *I Kitties love*

**G2** ✓ Head-final +subj-drop

Subject    Object    Verb

**G4** ✓ Head-final -subj-drop

~~**G1**~~ Head-first +subj-drop

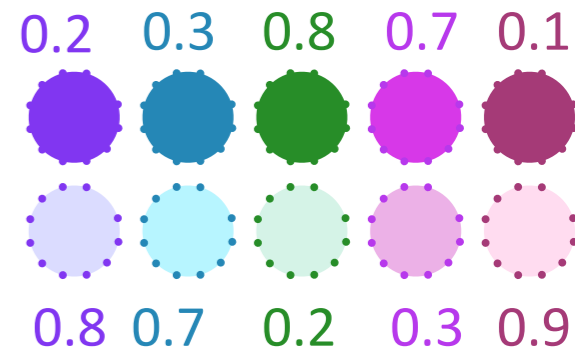
~~**G3**~~ Head-first -subj-drop



# Learning with parameters

## The learning algorithm

### Variational learning



Meanwhile, grammars using **head-first** would be punished every time, and its probability as a parameter value would approach 0.0 over time.



Head-directionality    Subject drop (subj-drop)

“...dass **ich**  
**Kätzchen liebe.**”  
...that *I Kitties love*

**Subject    Object    Verb**

~~G1~~ Head-first +subj-drop

~~G3~~ Head-first -subj-drop

✓ G2 Head-final +subj-drop

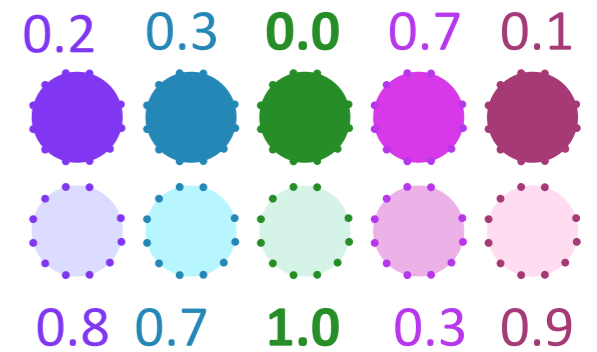
✓ G4 Head-final -subj-drop



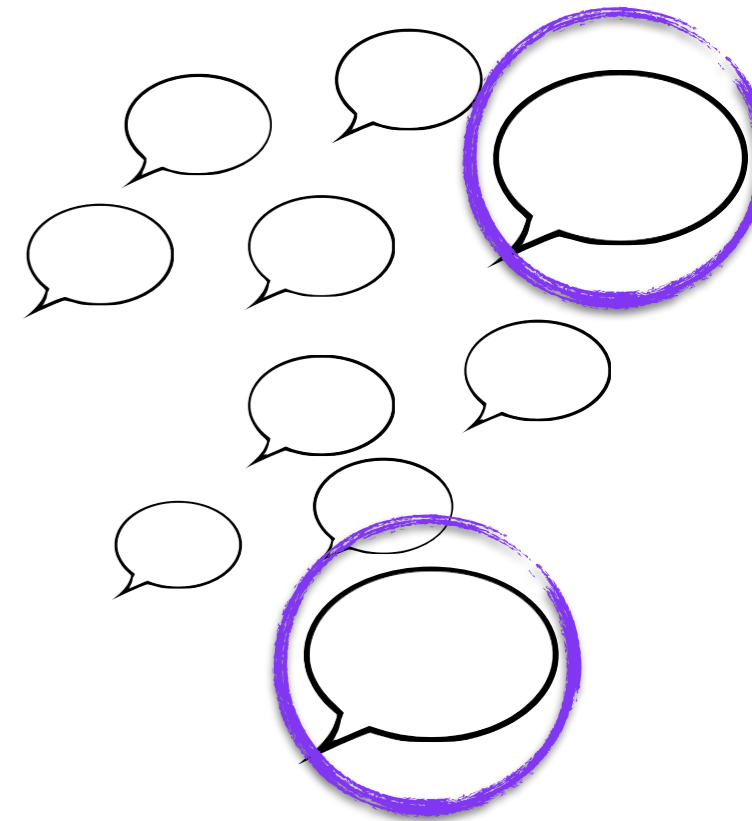
# Learning with parameters

The learning algorithm

**Variational learning**



Implication: The more **unambiguous data** there are, the faster the native language's parameter value will "win" (reach a probability near 1.0). This means that the child will learn the associated structural pattern faster.

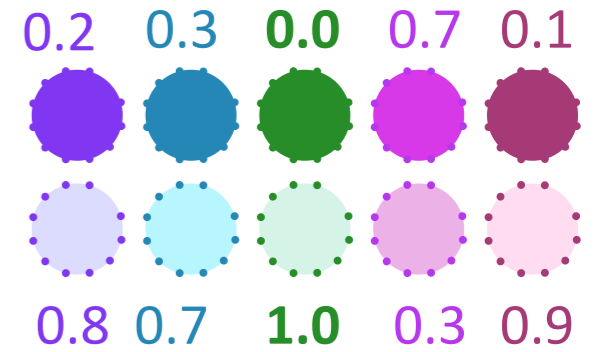




# Learning with parameters

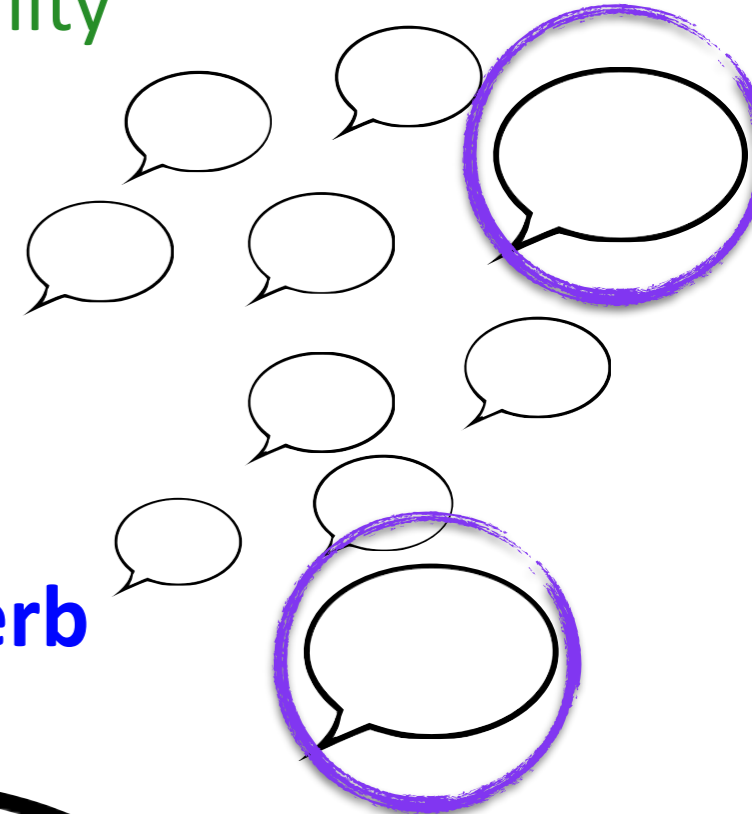
## The learning algorithm

### Variational learning



### Head-directionality

Example: the more unambiguous head-final data the child encounters, the faster a child should learn that the native language prefers objects before verbs as the basic order.



**Subject**

**Object**

**Verb**

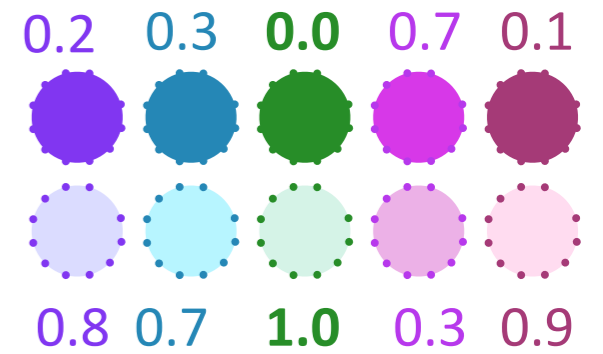


“...dass **ich**  
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*...that I Kitties love*

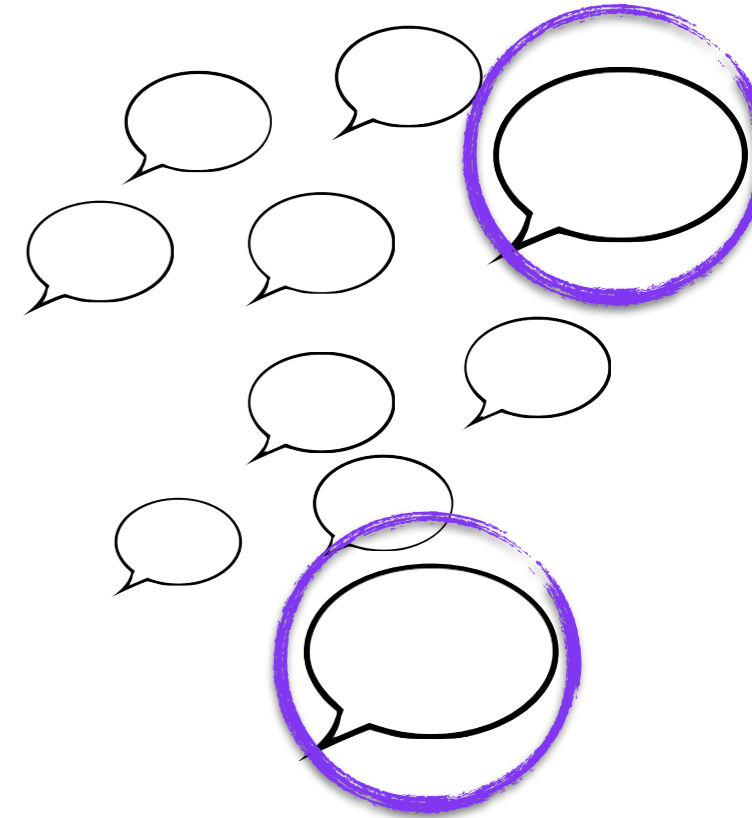
# Learning with parameters

The learning algorithm

Variational learning



**Is it true that the amount of unambiguous data the child encounters for a particular parameter strongly impacts when the child learns that structural property of the language?**



# Learning with parameters

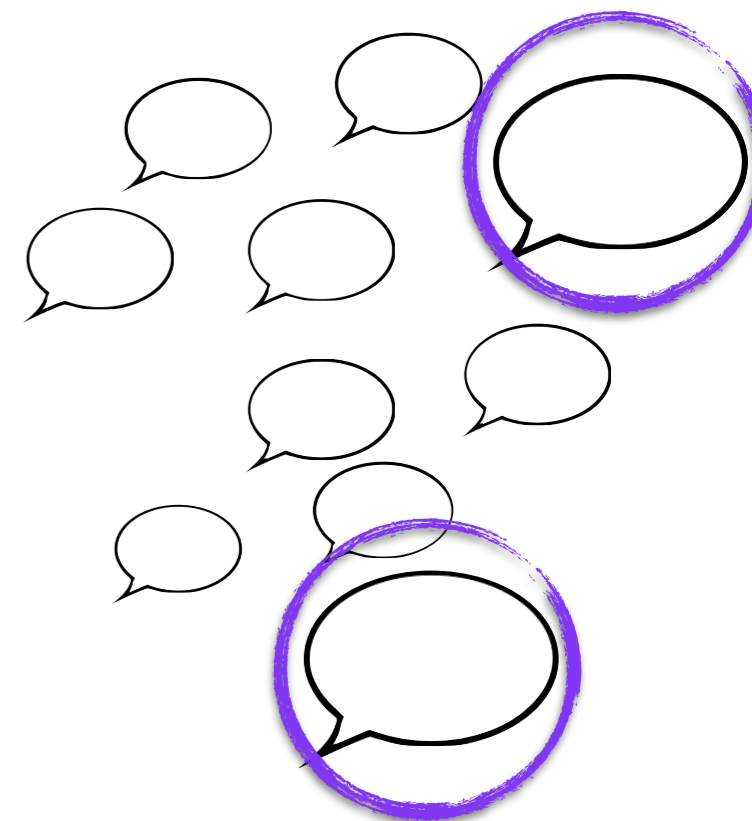
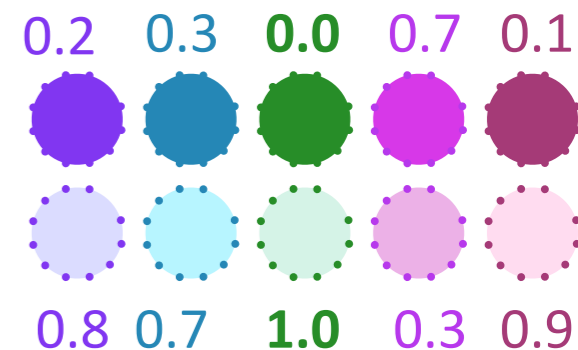
## The learning algorithm

### Variational learning

## Striking evidence that this is true

Table 1: The qualitative fit Yang discovered between the unambiguous data advantage (Adv) perceived by a VarLearner in its acquisitional intake and the observed age of acquisition (AoA) in children for six parameter values across different languages.

Param Value	Language	Unambiguous Form	Unambiguous Ex	Adv	AoA
+ <i>wh</i> -fronting	English	<i>wh</i> -fronting in questions	<i>Who did you see?</i>	25%	<1;8
+topic-drop	Chinese	null objects	<i>Wǒ méi kànjiàn</i> <i>I not see</i> “I didn’t see (him)”	12%	<1;8
+pro-drop	Italian	null subjects in questions	<i>Chi hai visto</i> <i>who have seen</i> “Who have you seen?”	10%	<1;8
+verb-raising	French	<i>Verb Adverb</i>	<i>Jean voit souvent Marie</i> <i>Jean sees often Marie</i> “Jean often sees Marie”	7%	1;8
-pro-drop	English	expletive subjects	There’s a penguin on the ice.	1.2%	3;0
+verb-second	German Dutch	<i>Object Verb Subject</i>	<i>Pinguine liebe ich.</i> <i>penguins like I</i> “I like penguins”	1.2%	3;0-3;2
-scope-marking	English	long-distance <i>wh</i> questions without medial- <i>wh</i>	<i>Who do you think is on the ice?</i>	0.2%	>4.0



# Learning with parameters

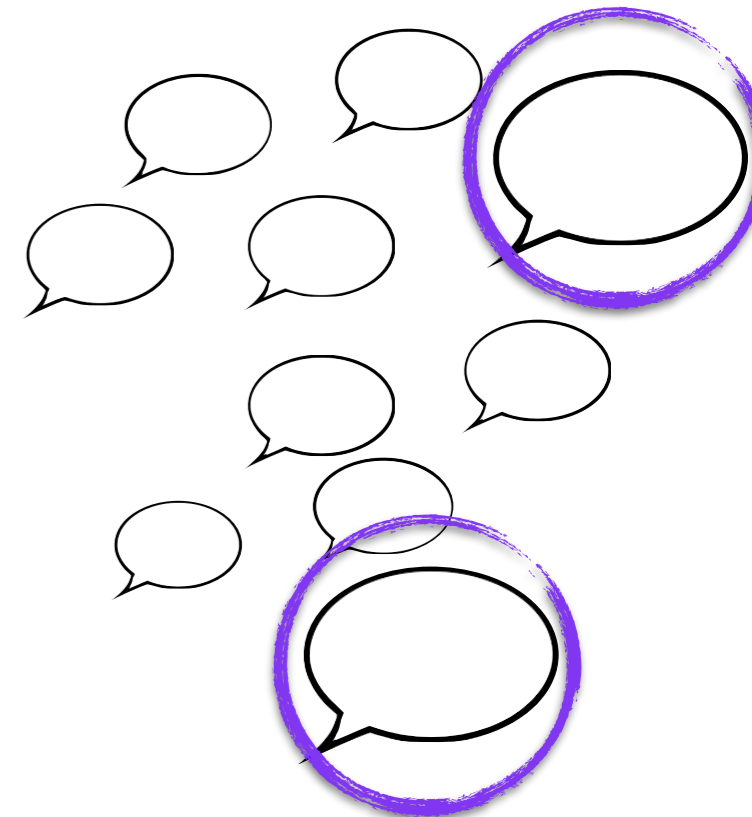
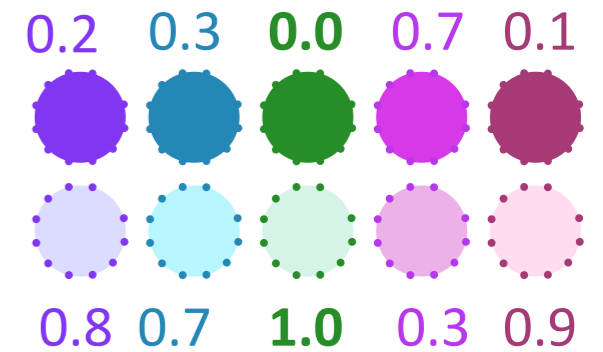
## The learning algorithm

### Variational learning

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The **more unambiguous data** there are for one value over another (its advantage)...





# Learning with parameters

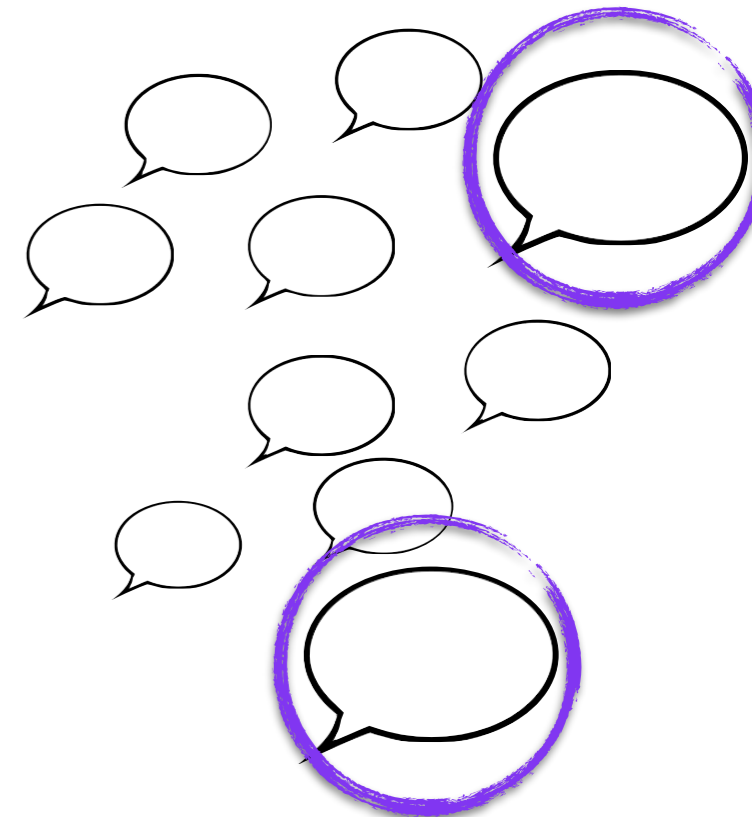
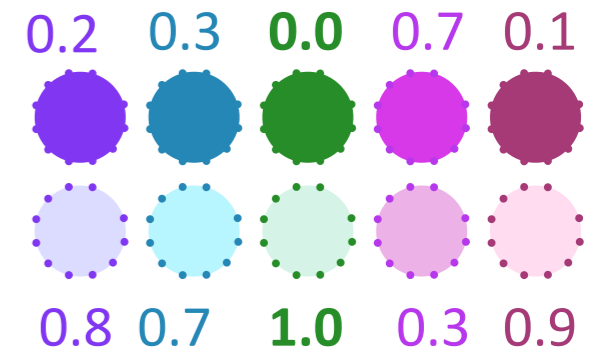
## The learning algorithm

### Variational learning

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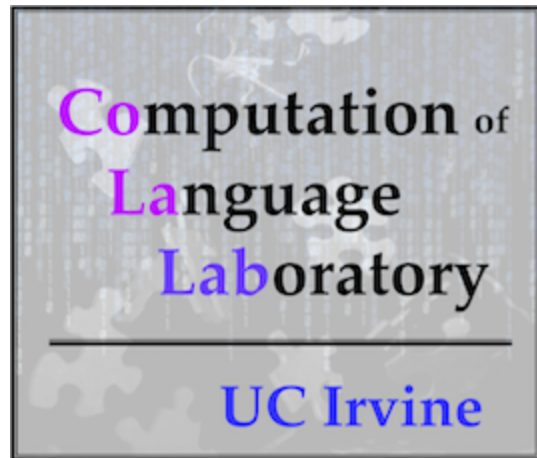
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The more unambiguous data there are for one value over another (its advantage), the earlier it seems to be **learned**.



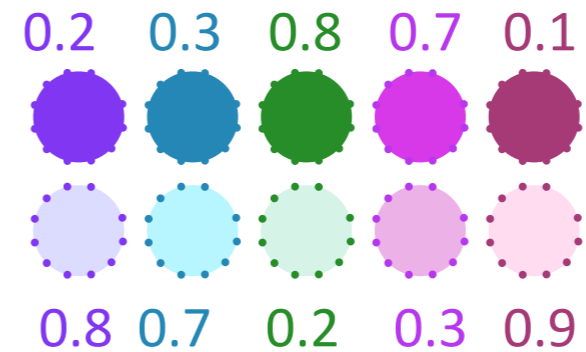
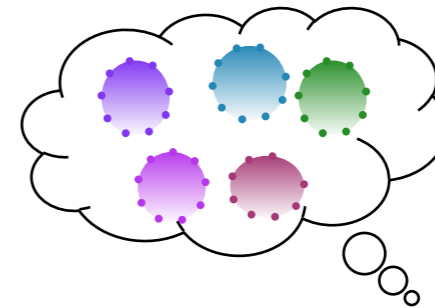
# Thank you!



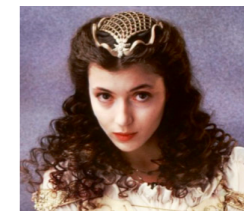
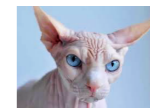
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This work was supported in part by NSF grants BCS-0843896 and BCS-1347028.



*another one*



*Who does... is pretty?*